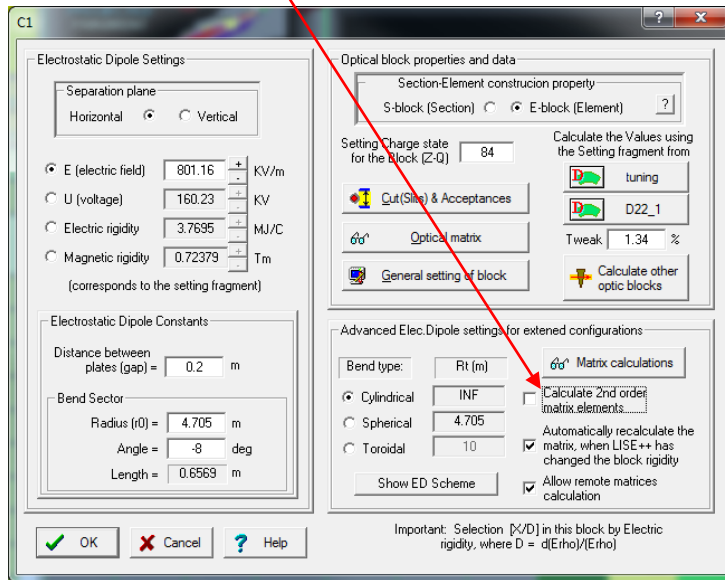


Version 9.10.298
from 06/06/2016

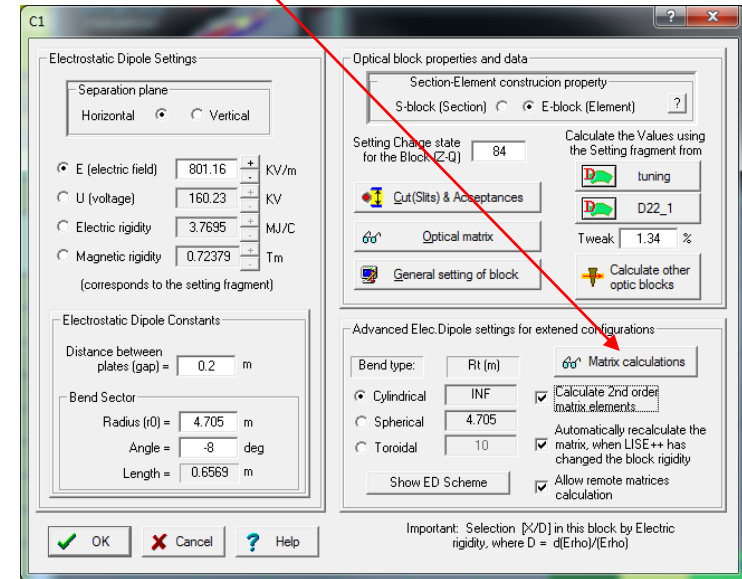
The 2nd order approximation equations in C-format were provided by **Robert Hipple** (Department of Physics and Astronomy, Michigan State University) based on **H.Wollnik's** work NIM 34 (1965) 213-221

- 2nd order settings for already existed configuration
- Comparison between COSY & LISE calculations for electric dipoles
- Using 2nd order electrostatic dipoles in EMMA @ TRIUMF
- Using 2nd order electrostatic dipoles in SHELS @ FLNR/JINR
- Outlook

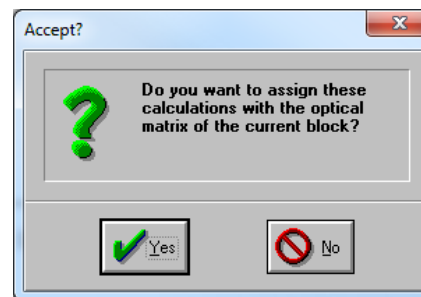
1st step: set "checked" the 2nd order box



2nd step: click "Matrix calculations" button



3rd step: Accept calculations



“Cylindrical” type; Radius = 1 m; Angle = 20 deg

LISE

COSY

Block: "ElecDipole" Matrices: "LOCAL" transport format [cm-mrad]

```

* TRANSFORM 1 *
1 [X]: +8.8064e-01 +3.3510e-02 0 0 0 +1.1936e-01
2 [T]: -6.6995e+00 +8.8064e-01 0 0 0 +6.6995e+00
3 [Y]: 0 0 +1.0000e+00 +3.4910e-02 0 0
4 [F]: 0 0 +1.0000e+00 0 0 0
5 [L]: -6.6995e-01 -1.1940e-02 0 0 +1.0000e+00 -2.8000e-02
6 [D]: 0 0 0 0 0 +1.0000e+00

* TRANSFORM 2 *
1 1: -2.8189e-03
1 2: +5.7678e-04 +5.1381e-06
1 3: 0 0 0
1 4: 0 0 0 -5.9697e-06
1 5: 0 0 0 0
1 6: +5.6350e-03 +9.3310e-05 0 0 -1.6237e-03

2 1: -8.9888e-02
2 2: -4.3966e-03 -5.3350e-05
2 3: 0 0 0
2 4: 0 0 0 -3.3506e-04
2 5: 0 0 0 0
2 6: +1.5725e-01 +4.3938e-03 0 0 -1.2329e-01

3 1: 0
3 2: 0 0
3 3: 0 0 0
3 4: +6.7013e-04 +1.1939e-05 0 0
3 5: 0 0 0 0
3 6: 0 0 0 +2.8004e-05 0 0

4 1: 0
4 2: 0 0
4 3: 0 0 0
4 4: -1.1936e-03 +3.3506e-04 0 0
4 5: 0 0 0 0
4 6: 0 0 0 +1.1936e-03 0 0

5 1: 0
5 2: 0 0
5 3: 0 0 0
5 4: 0 0 0 0
5 5: 0 0 0 0
5 6: 0 0 0 0 0 0
    
```

Block: "ElecDipole" Matrices: "LOCAL" transport format [cm-mrad]

```

* TRANSFORM 1 *
1 [X]: +8.8073e-01 +3.3510e-02 0 0 0 +1.1927e-01
2 [T]: -6.6943e+00 +8.8073e-01 0 0 0 +6.6943e+00
3 [Y]: 0 0 +1.0000e+00 +3.4910e-02 0 0
4 [F]: 0 0 +1.0000e+00 0 0 0
5 [L]: -6.6943e-01 -1.1930e-02 0 0 +1.0000e+00 -2.7950e-02
6 [D]: 0 0 0 0 0 +1.0000e+00

* TRANSFORM 2 *
1: -2.8145e-03
2: +5.7693e-04 +5.1394e-06
3: 0 0 0
4: 0 0 0 -5.9698e-06
5: 0 0 0 0
6: +5.6290e-03 +9.3219e-05 0 0 -1.6231e-03

1: -3.0744e-02
2: -1.0955e-03 -3.4837e-04
3: 0 0 0
4: 0 0 0 -3.3507e-04
5: 0 0 0 0
6: +1.9537e-01 +1.0955e-03 0 0 -9.7759e-02

1: 0
2: 0 0
3: 0 0 0
4: +6.7015e-04 +1.1939e-05 0 0
5: 0 0 0 0
6: 0 0 0 +2.7982e-05 0 0

1: 0
2: 0 0
3: 0 0 0
4: 0 0 0 0
5: 0 0 0 0
6: 0 0 0 0 0 0

1: -6.0224e-03
2: -3.3386e-04 -2.0081e-05
3: 0 0 0
4: 0 0 0 -1.6054e-05
5: 0 0 0 0
6: +5.3647e-03 -2.3688e-05 0 0 +3.8585e-04
    
```

“Cylindrical” type; Radius = 4 m; Angle = 20 deg

LISE

COSY

Block: "ElecDipole" Matrices: "LOCAL"

transport format [cm-mrad]

```

* TRANSFORM 1 *
1 [X]: +8.8064e-01 +3.3510e-02 0 0 0 0 +1.1936e-01
2 [Y]: -6.6995e+00 +8.8064e-01 0 0 0 0 +6.6995e+00
3 [Z]: 0 0 +1.0000e+00 +3.4910e-02 0 0 0
4 [F]: 0 0 0 +1.0000e+00 0 0 0
5 [L]: -6.6995e-01 -1.1940e-02 0 0 0 +1.0000e+00 -2.8000e-02
6 [D]: 0 0 0 0 0 0 +1.0000e+00
    
```

```

* TRANSFORM 2 *
1 1: -2.8189e-03
1 2: +5.7678e-04 +5.1381e-06
1 3: 0 0 0
1 4: 0 0 0 -5.9697e-06
1 5: 0 0 0 0
1 6: +5.6350e-03 +9.3310e-05 0 -1.6237e-03
2 1: -8.9888e-02
2 2: -4.3966e-03 -5.3350e-05
2 3: 0 0 0
2 4: 0 0 0 -3.3506e-04
2 5: 0 0 0 0
2 6: +1.5725e-01 +4.3938e-03 0 -1.2329e-01
3 1: 0
3 2: 0 0 0
3 3: 0 0 0
3 4: +6.7013e-04 +1.1939e-05 0 0
3 5: 0 0 0 0
3 6: 0 0 0 +2.8004e-05 0 0
4 1: 0
4 2: 0 0 0
4 3: 0 0 0
4 4: -1.1936e-03 +3.3506e-04 0 0
4 5: 0 0 0 0
4 6: 0 0 0 +1.1936e-03 0 0
5 1: 0
5 2: 0 0 0
5 3: 0 0 0
5 4: 0 0 0 0
5 5: 0 0 0 0
5 6: 0 0 0 0 0 0
    
```

Block: "ElecDipole" Matrices: "LOCAL"

transport format [cm-mrad]

```

* TRANSFORM 1 *
K]: +8.8073e-01 +3.3510e-02 0 0 0 0 +1.1927e-01
T]: -6.6943e+00 +8.8073e-01 0 0 0 0 +6.6943e+00
Y]: 0 0 +1.0000e+00 +3.4910e-02 0 0 0
F]: 0 0 0 +1.0000e+00 0 0 0
L]: -6.6943e-01 -1.1930e-02 0 0 0 +1.0000e+00 -2.7950e-02
D]: 0 0 0 0 0 0 +1.0000e+00
    
```

```

* TRANSFORM 2 *
1: -2.8145e-03
2: +5.7693e-04 +5.1394e-06
3: 0 0 0
4: 0 0 0 -5.9698e-06
5: 0 0 0 0
6: +5.6290e-03 +9.3219e-05 0 -1.6231e-03
1: -3.0744e-02
2: -1.0955e-03 -3.4837e-04
3: 0 0 0
4: 0 0 0 -3.3507e-04
5: 0 0 0 0
6: +1.9537e-01 +1.0955e-03 0 -9.7759e-02
1: 0
2: 0 0 0
3: 0 0 0
4: +6.7015e-04 +1.1939e-05 0 0
5: 0 0 0 0
6: 0 0 0 +2.7982e-05 0 0
1: 0
2: 0 0 0
3: 0 0 0
4: 0 0 0 0
5: 0 0 0 0
6: 0 0 0 0 0 0
1: -6.0224e-03
2: -3.3386e-04 -2.0081e-05
3: 0 0 0
4: 0 0 0 -1.6054e-05
5: 0 0 0 0
6: +5.3647e-03 -2.3688e-05 0 +3.8585e-04
    
```

“Spherical” type; Radius = 4 m; Angle = 45 deg

LISE

COSY

Block: "ElecDipole" Matrices: "LOCAL" transport format [cm-mrad]

```

* TRANSFORM 1 *
1 [X]: +7.0717e-01 +2.8285e-01 0 0 0 +2.3429e+00
2 [T]: -1.7674e+00 +7.0717e-01 0 0 0 +1.4141e+01
3 [Y]: 0 0 +7.0711e-01 +2.8284e-01 0 0
4 [F]: 0 0 -1.7678e+00 +7.0711e-01 0 0
5 [L]: -1.4141e+00 -2.3429e-01 0 0 +1.0000e+00 -1.2524e+00
6 [D]: 0 0 0 0 0 +1.0000e+00

* TRANSFORM 2 *
1 1: -1.2502e-03
1 2: +1.0000e-03 +8.2843e-05
1 3: 0 0 +2.5889e-04
1 4: 0 0 +2.0711e-04 -1.0000e-04
1 5: 0 0 0 0 0
1 6: +1.9997e-02 +3.3133e-03 0 0 0 -2.1418e-02

2 1: -5.0031e-02
2 2: -7.0730e-03 -8.2863e-04
2 3: 0 0 +9.1533e-04
2 4: 0 0 +1.7678e-03 -5.0001e-04
2 5: 0 0 0 0 0
2 6: +1.9990e-01 +5.6557e-02 0 0 0 -1.9997e-01

3 1: 0
3 2: 0 0
3 3: -5.1780e-04 -2.0711e-04 0
3 4: +1.2071e-03 +2.0000e-04 0 0
3 5: 0 0 0 0 0
3 6: 0 0 +4.1417e-03 +1.6567e-03 0 0

4 1: 0
4 2: 0 0
4 3: +2.0708e-02 -8.2846e-03 0
4 4: -4.9995e-03 +2.0001e-03 0 0
4 5: 0 0 0 0 0
4 6: 0 0 +2.4997e-02 +9.9990e-03 0 0

5 1: 0
5 2: 0 0
5 3: 0 0 0
5 4: 0 0 0 0
5 5: 0 0 0 0
5 6: 0 0 0 0 0
    
```

Block: "ElecDipole" Matrices: "LOCAL" transport format [cm-mrad]

```

* TRANSFORM 1 *
[X]: +7.0717e-01 +2.8285e-01 0 0 0 +2.3429e+00
[T]: -1.7674e+00 +7.0717e-01 0 0 0 +1.4141e+01
[Y]: 0 0 +7.0711e-01 +2.8284e-01 0 0
[F]: 0 0 -1.7678e+00 +7.0711e-01 0 0
[L]: -1.4141e+00 -2.3429e-01 0 0 +1.0000e+00 -1.2524e+00
[D]: 0 0 0 0 0 +1.0000e+00

* TRANSFORM 2 *
1: -1.2498e-03
2: +1.0001e-03 +8.2851e-05
3: 0 0 +2.5896e-04
4: 0 0 +2.0712e-04 -1.0000e-04
5: 0 0 0 0 0
6: +1.9998e-02 +3.3133e-03 0 0 0 -2.1421e-02


1: 0
2: 0 -7.0712e-04
3: 0 0 +9.1571e-04
4: 0 0 +1.7679e-03 -5.0000e-04
5: 0 0 0 0 0
6: +7.0698e-02 -1.1922e-06 0 0 0 -2.1212e-01

1: 0
2: 0 0
3: -5.1766e-04 -2.0709e-04 0
4: +1.2071e-03 +2.0001e-04 0 0
5: 0 0 0 0 0
6: 0 0 +4.1417e-03 +1.6567e-03 0 0


1: 0
2: 0 0
3: +4.4203e-03 +7.3237e-04 0
4: -7.3210e-04 +3.0634e-08 0 0
5: 0 0 0 0 0
6: 0 0 +3.5352e-02 +5.8574e-03 0 0

1: -1.8747e-03
2: -1.4999e-03 -2.6567e-04
3: 0 0 -1.1426e-03
4: 0 0 -8.5730e-05 -1.0000e-04
5: 0 0 0 0 0
6: +1.7175e-03 -2.0584e-03 0 0 0 +1.2124e-02
    
```

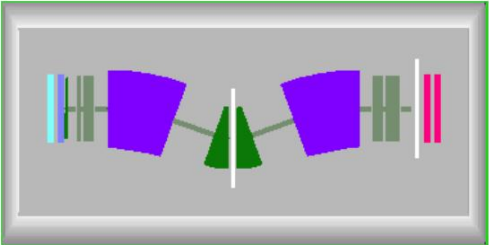
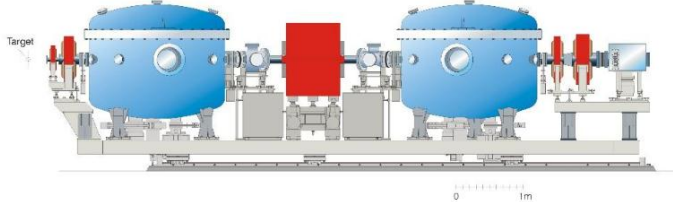
http://lise.nsci.msu.edu/9_10/EMMA.pdf



EMMA (ElectroMagnetic Mass Analyzer) @ TRIUMF



Version 9.10.207 from 11/17/2015 [Link: Separator "EMMA" @ TRIUMF](#)

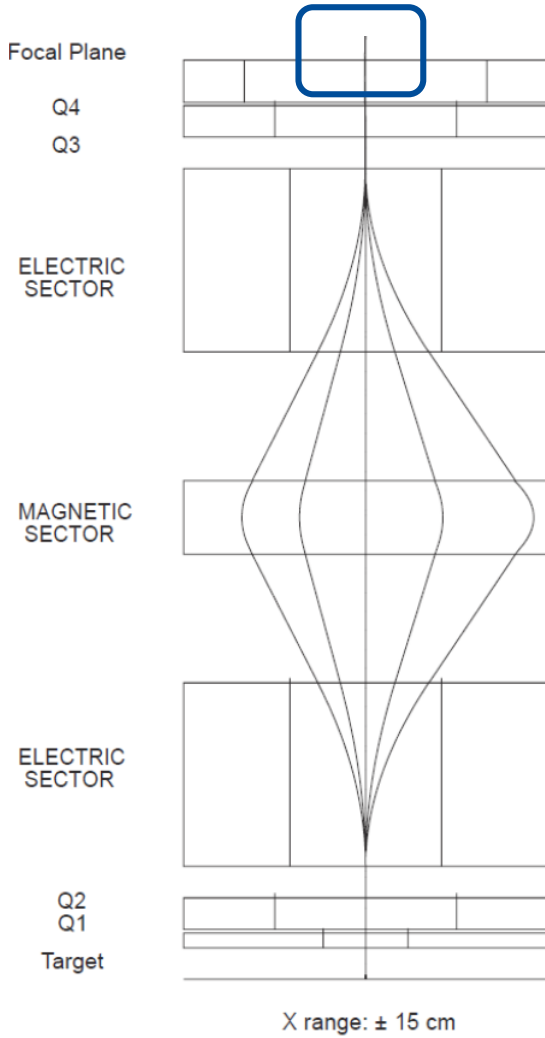



The new version with 2nd order electrostatic dipoles :

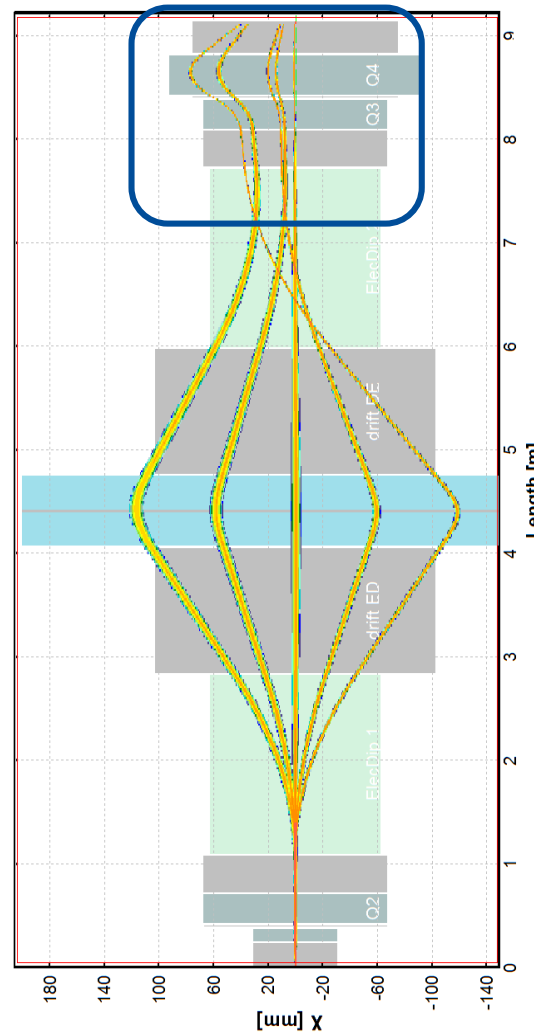
http://lise.nsci.msu.edu/9_10/ED/EMMA_2016.lpp

Or in the LISE++ package "files\examples\TRIUMF\EMMA_2016.lpp"

NIM A544 (2005) 565

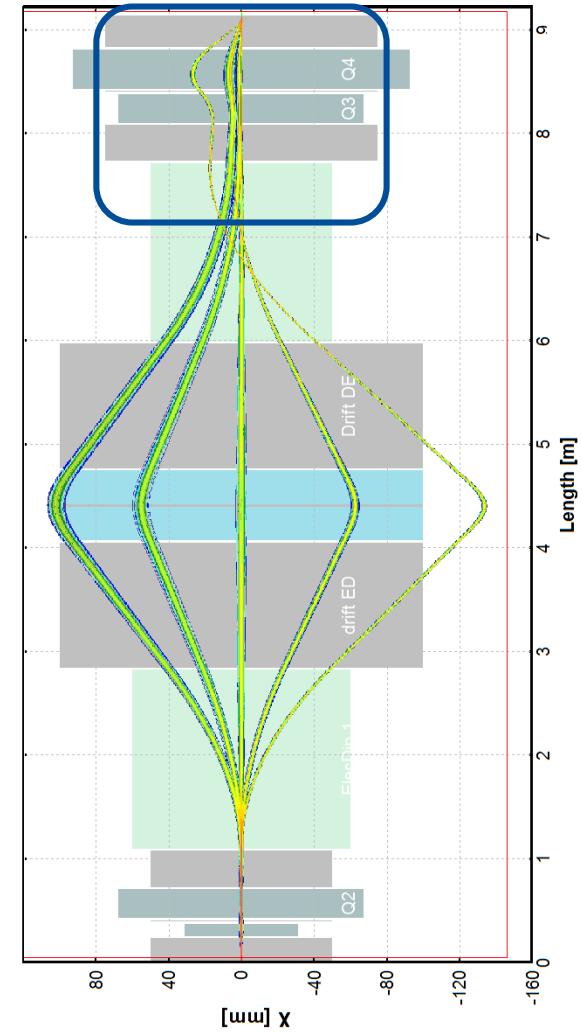


LISE++ v.9.10.207



2nd order

LISE++ v.9.10.296



2nd order

NIM A544 (2005) 565

LISE++ v.9.10.296

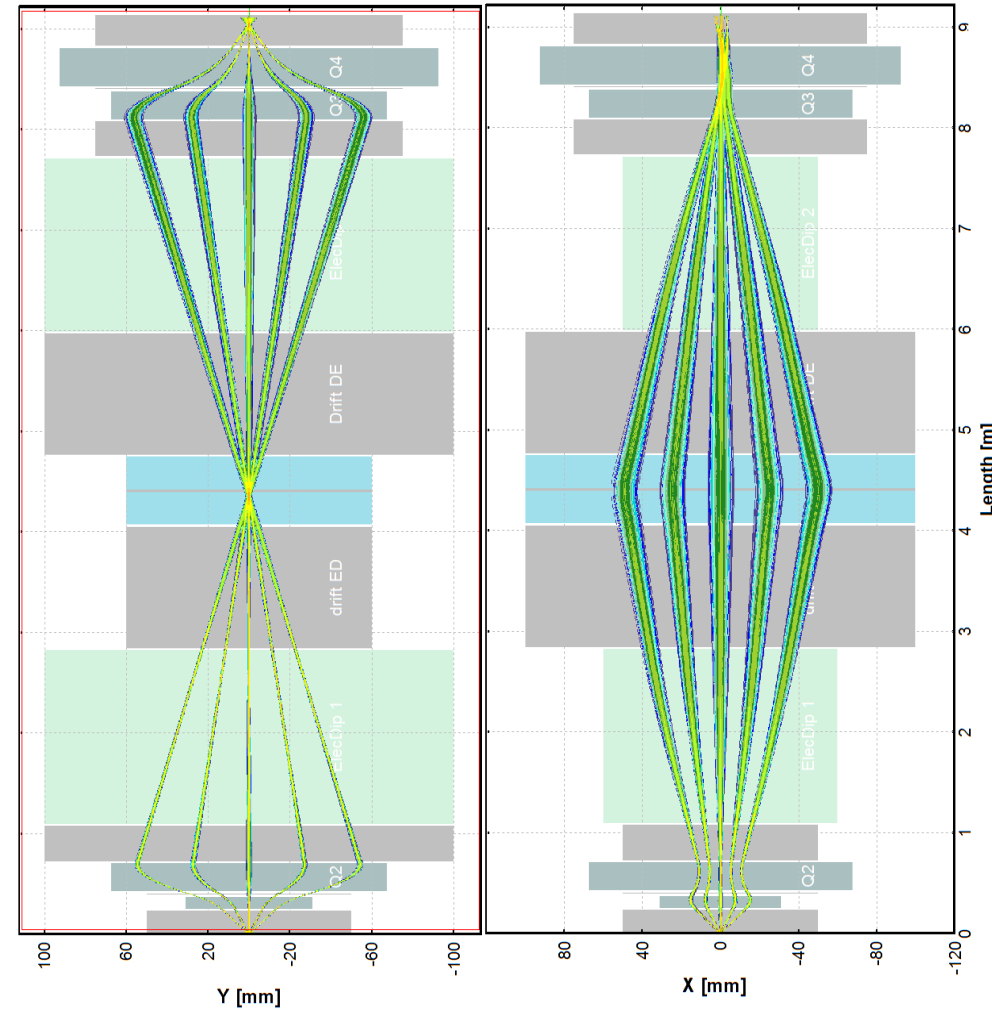
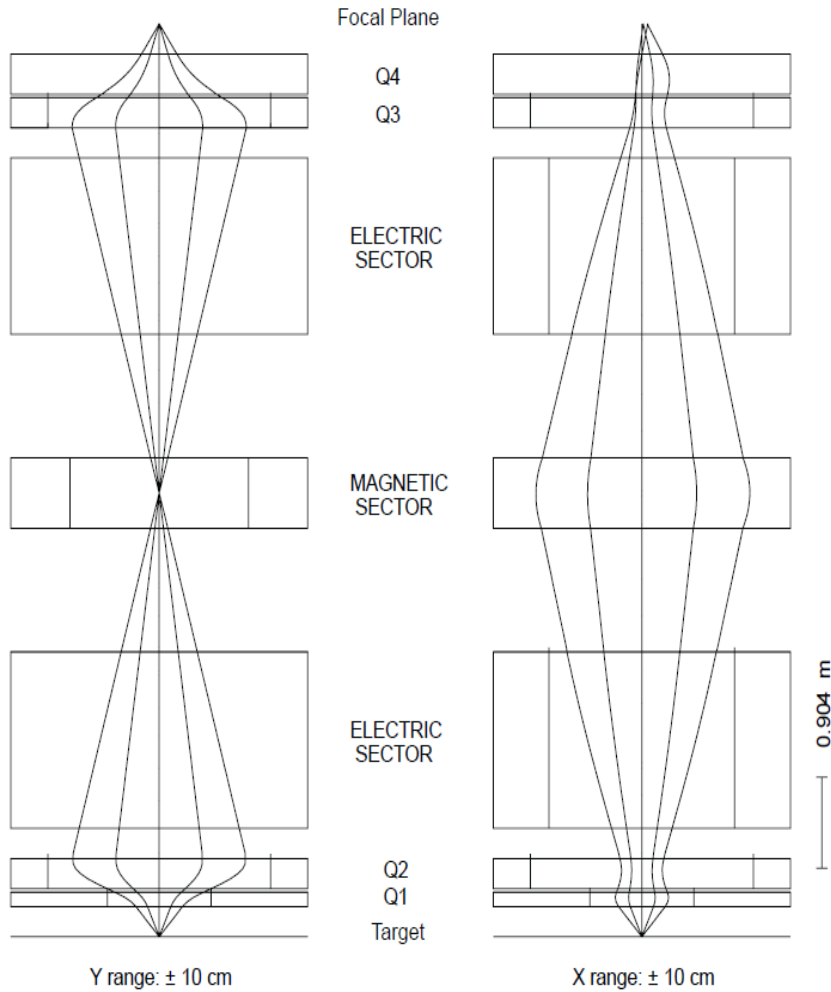


Fig. 4. Calculated spatial focus of EMMA, showing rays corresponding to a single mass emitted from the target with angles of 0° , $\pm 1.5^\circ$, and $\pm 3^\circ$ in the vertical and horizontal directions. The dominant geometric aberration in the dispersive direction, proportional to the square of the horizontal angle, is evident in the horizontal extent of the final focus.

2nd order

2nd order

NIM A544 (2005) 565

LISE++ v.9.10.296

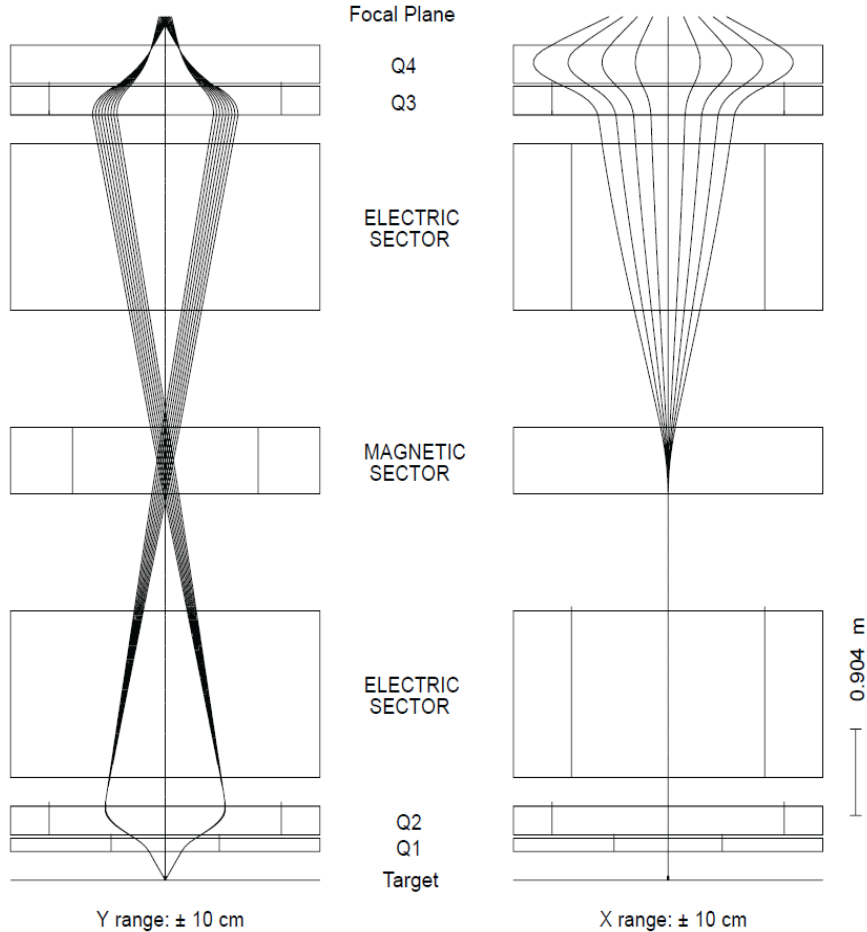
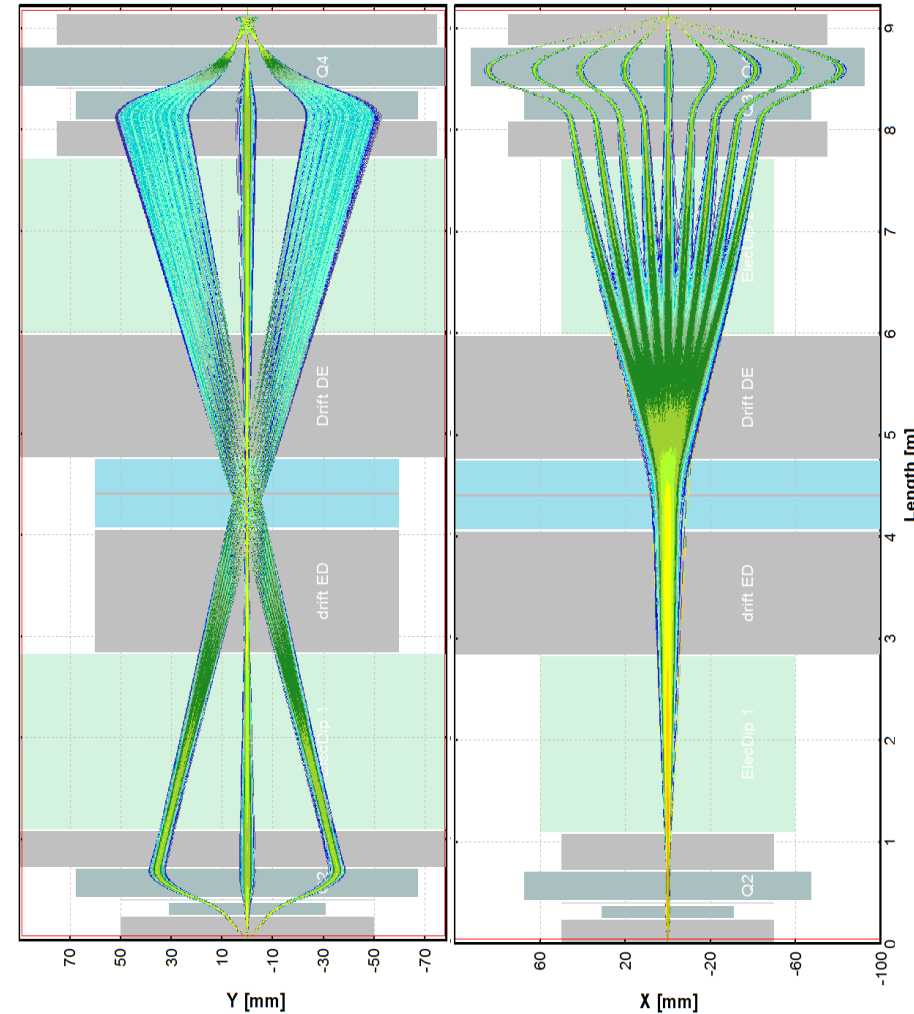


Fig. 2. Calculated mass focus of EMMA, showing rays corresponding to 9 adjacent masses emitted from the target with vertical angles of -2° , 0° , and 2° . At the focal plane, the 9 masses are seen to be dispersed horizontally and focussed vertically. Angular focussing in the horizontal direction is shown in Fig. 4.



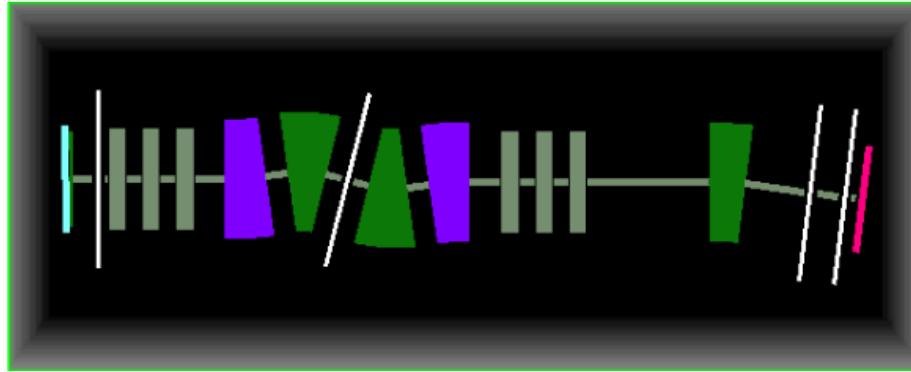
2nd order

2nd order

with $\sigma(X)=0.02\text{mm}$ & $\sigma(Y')=1\text{mrad}$

v.9.8.166
from 11/23/14

http://lise.nsci.msu.edu/9_8/SHELS/SHELSinLISE.pdf



Preparation to the experiment

Transmission : Analytical

²⁵⁵Lr^{All+} transmission Analytical : 44.7%

²⁵⁵Lr¹⁹⁺ transmission Analytical : 53.1%

statistics: 255Lr

255Lr Alpha and Beta decay (Z=103, N=152) Lawrencium

All reactions total isotope rate: 1.19e+0 pps
and Overall isotope transmission: 44.653 %

9.098 / 17.15 * 100%

Reaction	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes
Q1 (tuning)	25	24	23	22	21	20	19	18	17	16	15	14	
Q2 (C1)	25	24	23	22	21	20	19	18	17	16	15	14	
Q3 (D22_1)	25	24	23	22	21	20	19	18	17	16	15	14	
Q4 (D22_2)	25	24	23	22	21	20	19	18	17	16	15	14	
Q5 (C2)	25	24	23	22	21	20	19	18	17	16	15	14	
Q6 (D8)	25	24	23	22	21	20	19	18	17	16	15	14	
Ion Production Rate (pps)	6.1e-3	1.99e-2	4.92e-2	1.01e-1	1.67e-1	2.34e-1	3.19e-1	1.96e-1	1.1e-1	4.77e-2	1.44e-2	2.71e-3	
Total ion transmission (%)	0.229	0.745	1.847	3.776	6.264	8.783	9.098	7.335	4.14	1.789	0.541	0.102	
Total: this reaction (pps)	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	1.19e+0	
X-Section in target (mb)	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	1.41e-4	

How 2nd order optics calculations are important for transmission value in the case of the SHELS separator ?

The new version with 2nd order electrostatic dipoles :

http://lise.nsci.msu.edu/9_10/ED/SHELS_2016_o2.lpp

Or in the LISE++ package “files\examples\Dubna\SHELS_2016_o2.lpp”

Overall transmission = transmission through a separator of given isotope created in a target

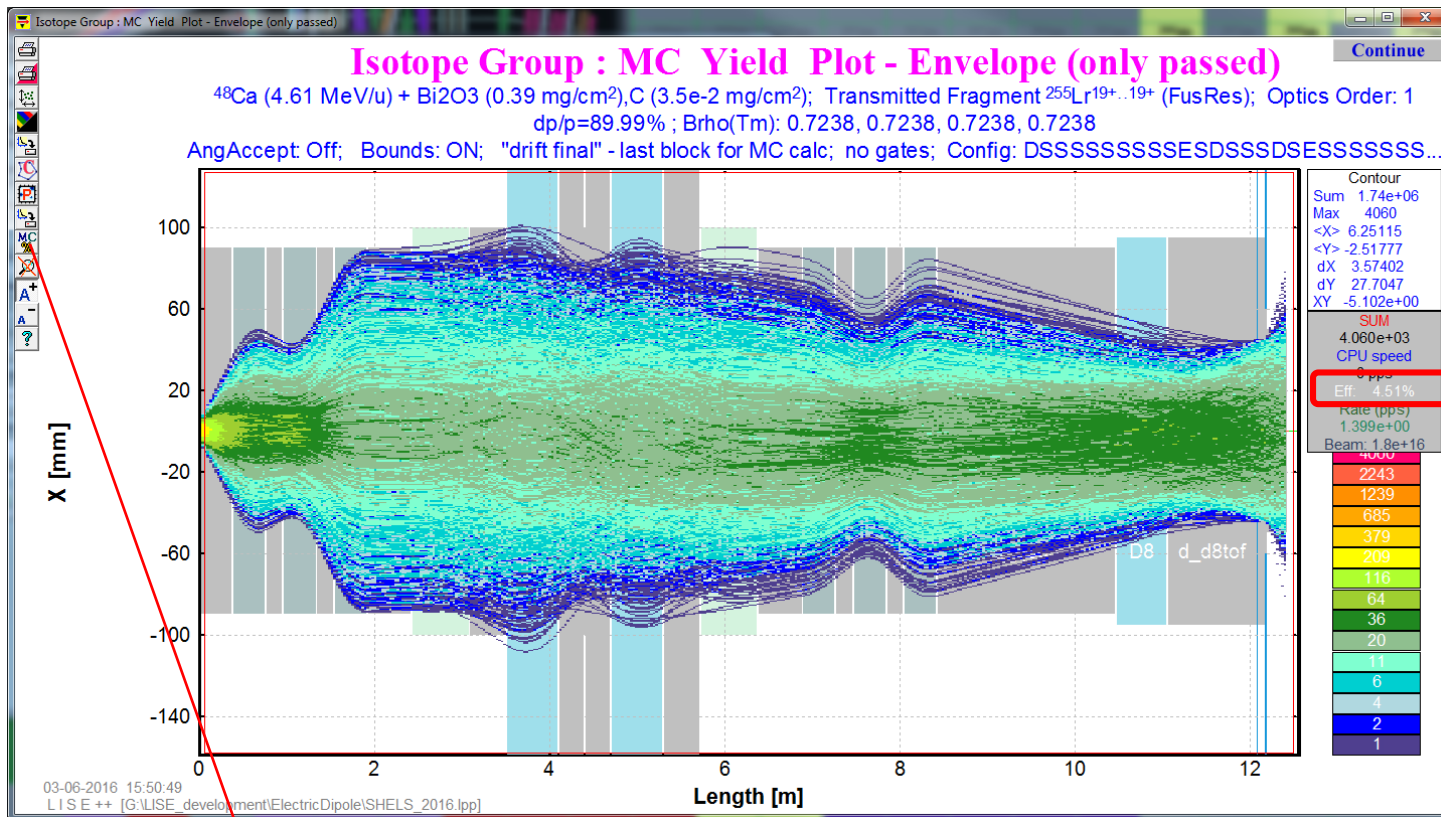
1st order; Analytical solution

statistics: 255Lr

255Lr Alpha and Beta+ decay (Z=103, N=152) ²⁵⁵Lr All overall ²⁵⁵Lr¹⁹⁺ transmission

All reactions total isotope rate 1.37e+0 pps and Overall isotope transmission 52.914 % **transmission 52.9%** **10.325% / 0.171 = 60.4%**

Reaction	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes	FusRes
Q1 (tuning)	25	24	23	22	21	20	19	18	17	16	15	14
Q2 (C1)	25	24	23	22	21	20	19	18	17	16	15	14
Q3 (D22_1)	25	24	23	22	21	20	19	18	17	16	15	14
Q4 (D22_2)	25	24	23	22	21	20	19	18	17	16	15	14
Q5 (C2)	25	24	23	22	21	20	19	18	17	16	15	14
Q6 (D8)	25	24	23	22	21	20	19	18	17	16	15	14
Ion Production Rate (pps)	7.5e-3	2.33e-2	5.97e-2	1.24e-1	2.07e-1	2.64e-1	2.67e-1	2.2e-1	1.29e-1	5.39e-2	1.26e-2	9.83e-4
Total ion transmission (%)	0.29	0.903	2.311	4.786	7.995	10.208	10.325	8.509	4.975	2.086	0.488	0.038
Total: this reaction (pps)	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0	1.37e+0
X-Section in target (mb)	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4	1.62e-4
Target (%)	100	99.57	100	100	100	100	100	100	100	100	99.57	100
Unreacted in material (%)	100	100	100	100	100	100	100	100	100	100	100	100
Unstopped in material (%)	100	99.57	100	100	100	100	100	100	100	100	99.57	100
Stripper (%)	0.922	2.41	5.22	9.34	13.81	16.89	17.08	14.28	9.87	5.64	2.66	1.04
Unreacted in material (%)	100	100	100	100	100	100	100	100	100	100	100	100
Q (Charge) ratio (%)	0.922	2.41	5.22	9.34	13.82	16.89	17.08	14.28	9.87	5.64	2.66	1.04
Unstopped in material (%)	100	100	100	100	100	100	100	100	100	100	100	100



²⁵⁵Lr transmission
 4.51%
 Including charge
 state contribution

Monte Carlo transmission statistics by blocks

Isotope Group : MC Yield Plot - Envelope (only passed)

⁴⁸Ca (4.61 MeV/u) + Bi2O3 (0.39 mg/cm²), C (3.5e-2 mg/cm²); Transmitted Frag
 dp/p=89.99%; Brho(Tm): 0.7238, 0.7238, 0.7238, 0.7238
 AngAccept: Off; Bounds: ON; "drift final" - last block for MC calc; no

#	Ion	N of Passed	N of Initial	Transmission	Z	N	Reac- tion	Q1	Q
All		4060	90000	4.51%					
0	²⁵⁵ Lr	0	8997	0%	(+/-0.01%)	103	152	R1	25+ 2
1	²⁵⁵ Lr	0	9157	0%	(+/-0.01%)	103	152	R1	24+ 2
2	²⁵⁵ Lr	0	8999	0%	(+/-0.01%)	103	152	R1	23+ 2
3	²⁵⁵ Lr	0	9006	0%	(+/-0.01%)	103	152	R1	22+ 2
4	²⁵⁵ Lr	0	8937	0%	(+/-0.01%)	103	152	R1	21+ 2
5	²⁵⁵ Lr	0	8937	0%	(+/-0.01%)	103	152	R1	20+ 2
6	²⁵⁵ Lr	0	9067	0%	(+/-0.01%)	103	152	R1	19+ 1
7	²⁵⁵ Lr	0	8757	0%	(+/-0.01%)	103	152	R1	18+ 1
8	²⁵⁵ Lr	0	8823	0%	(+/-0.01%)	103	152	R1	17+ 1
9	²⁵⁵ Lr	0	9043	0%	(+/-0.01%)	103	152	R1	16+ 1
10	²⁵⁵ Lr	0	9013	0%	(+/-0.01%)	103	152	R1	15+ 1
11	²⁵⁵ Lr	0	8942	0%	(+/-0.01%)	103	152	R1	14+ 1

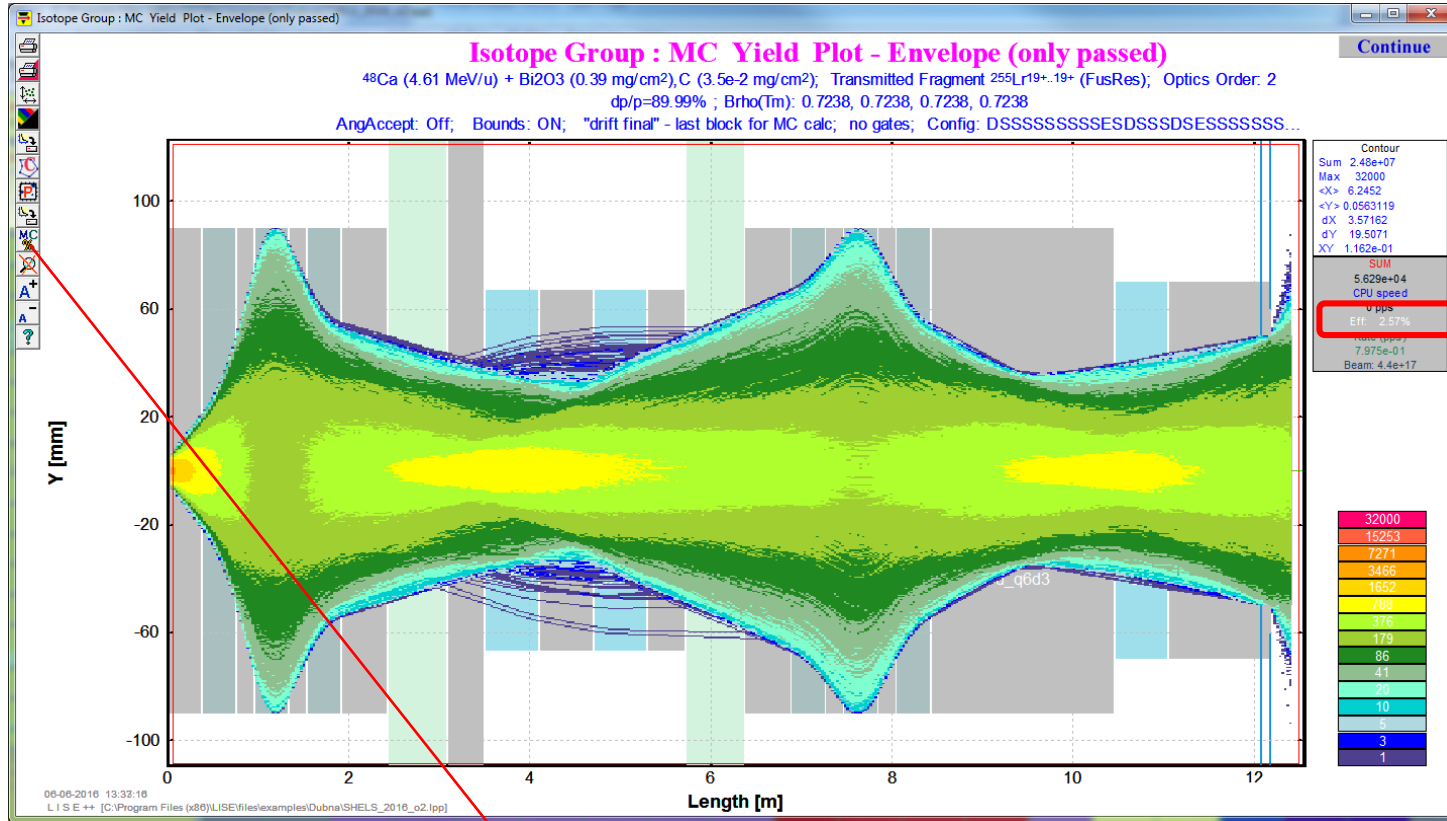
Target 100.0%

Stripper 8.26%

Q-state 8.26%

²⁵⁵Lr transmission
 Q-state = 8.26%

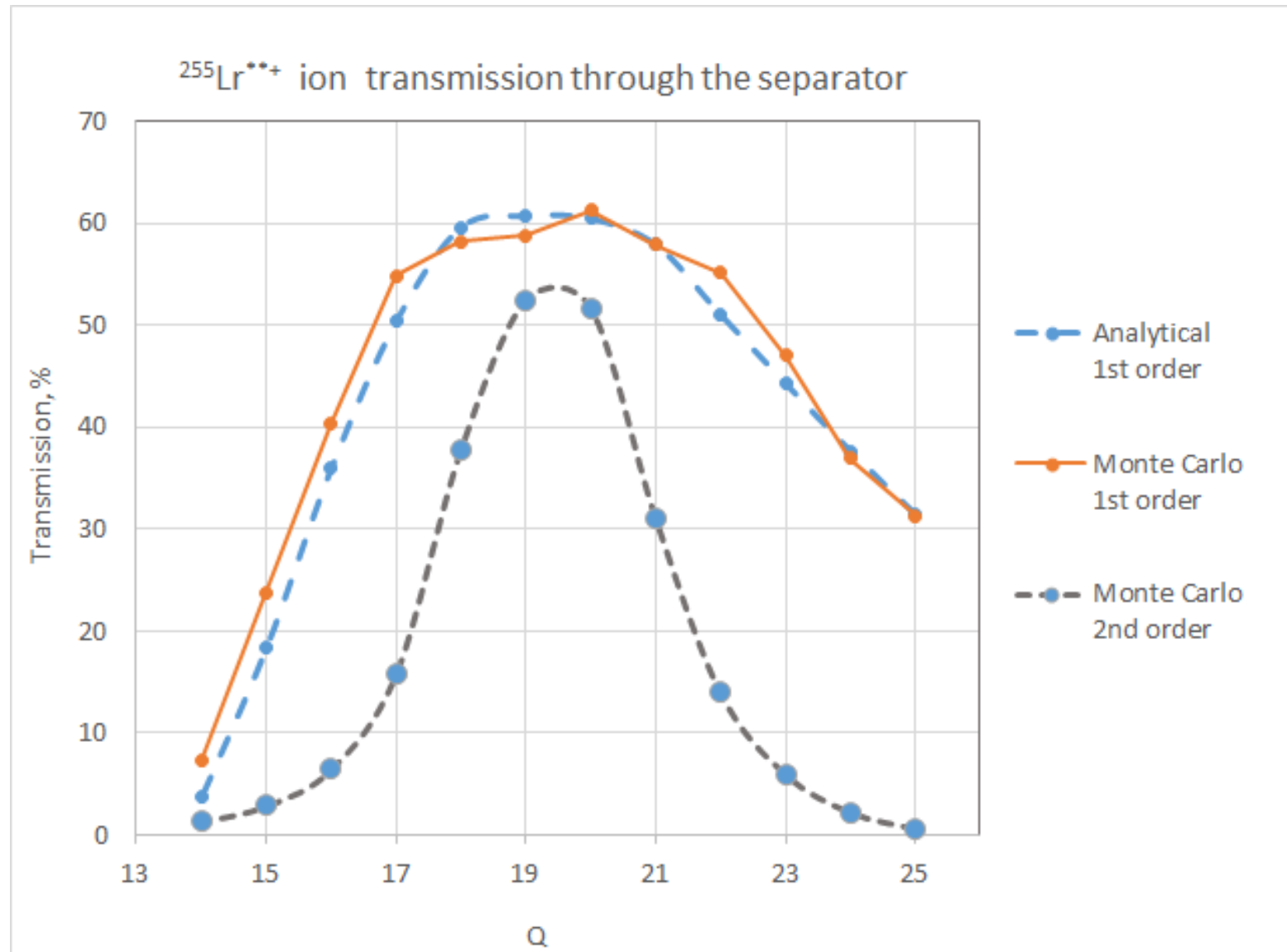
**²⁵⁵Lr^{All} overall
 transmission 54.6%**



²⁵⁵Lr transmission
2.57%
Including charge state contribution

²⁵⁵Lr transmission
Q-state = 8.24%

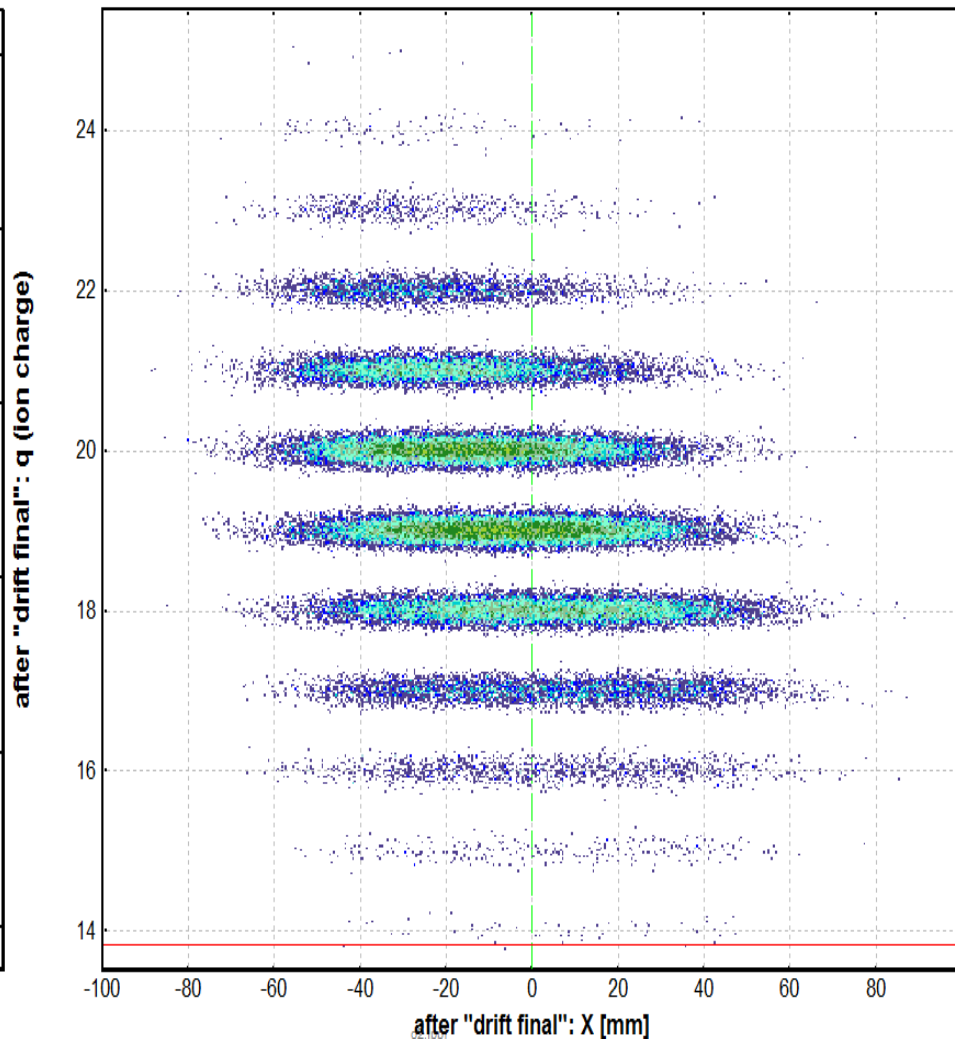
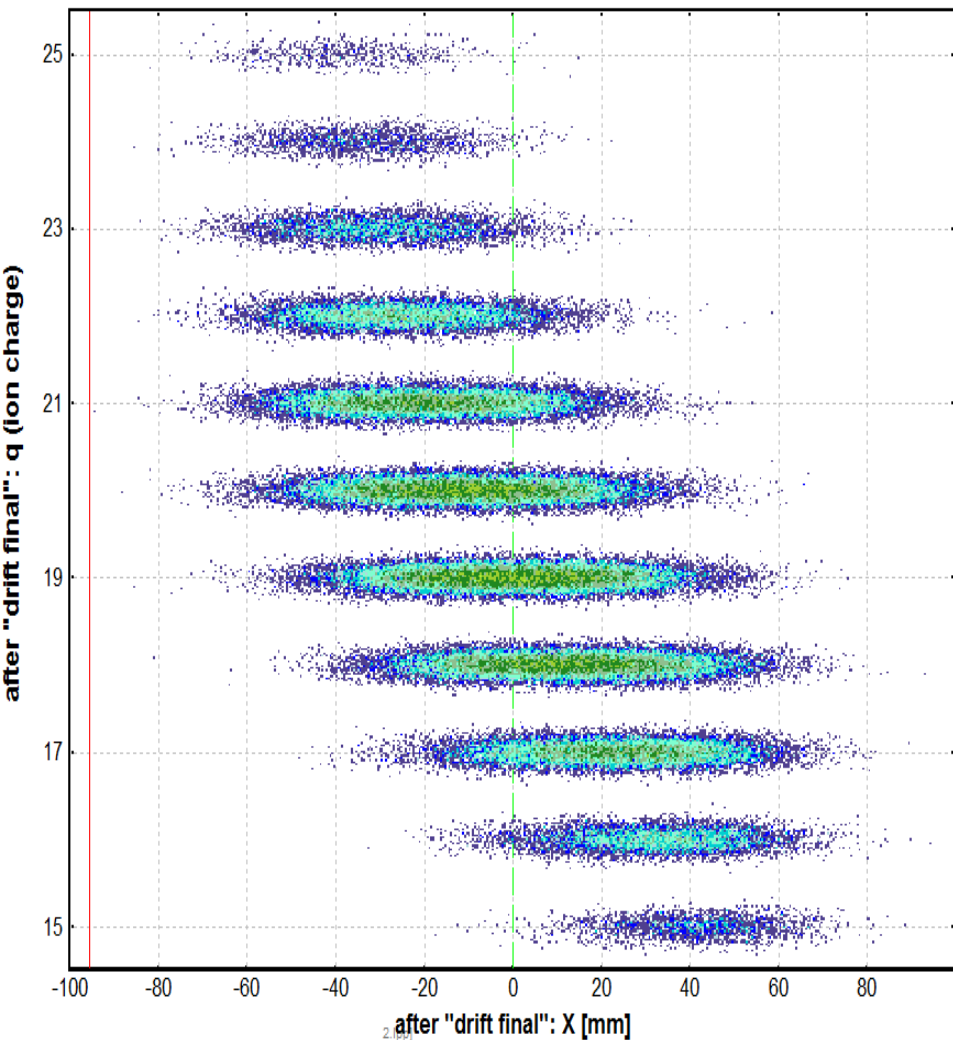
²⁵⁵Lr^{All} overall transmission 31.2%

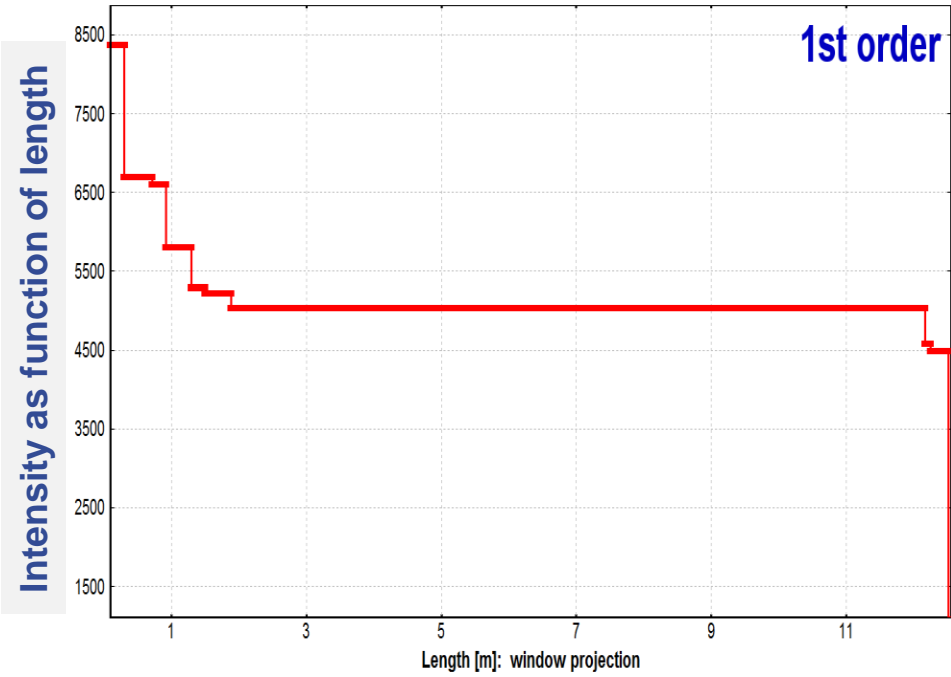
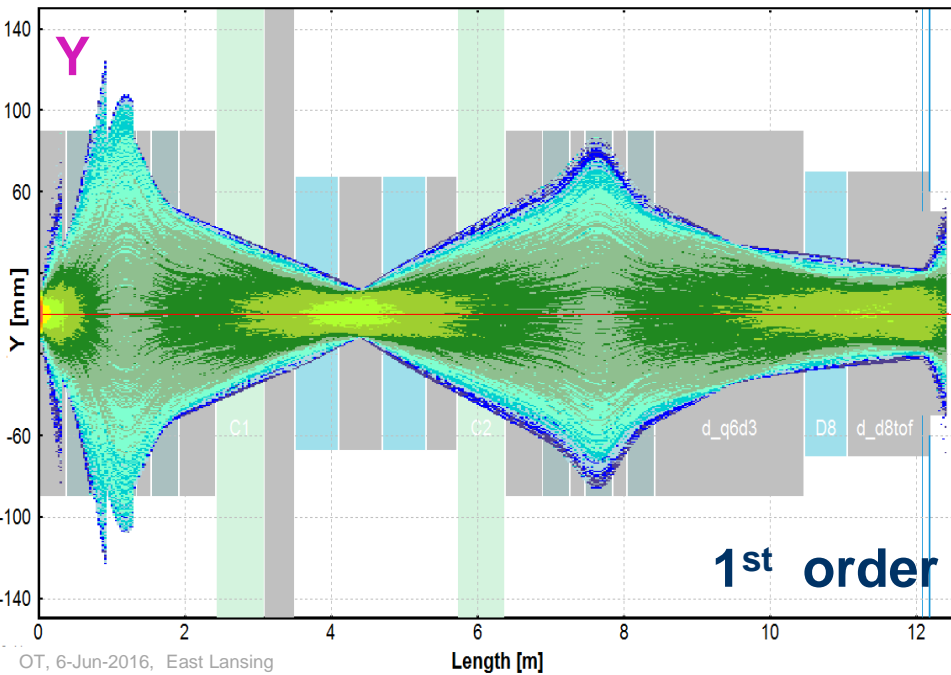
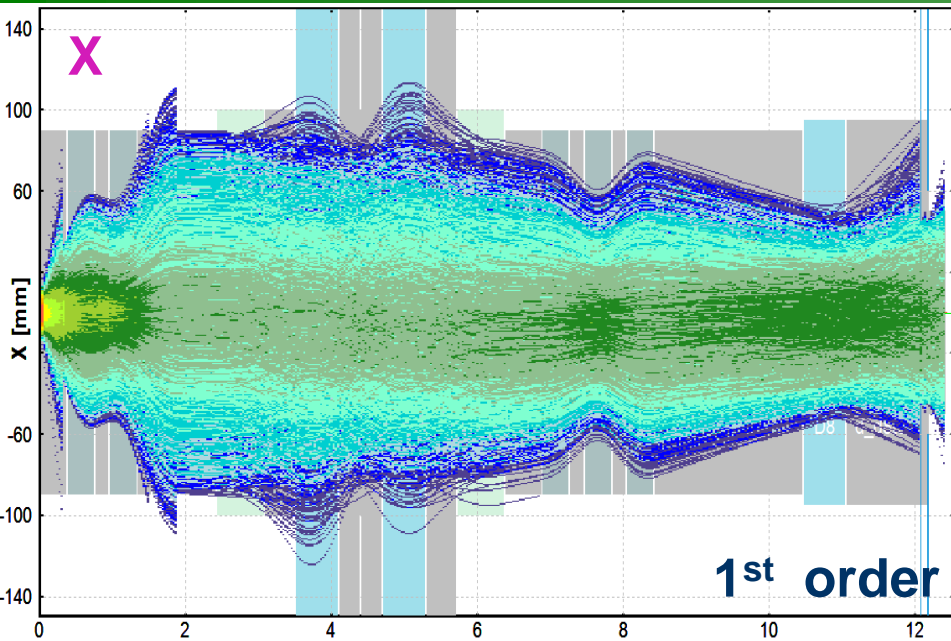


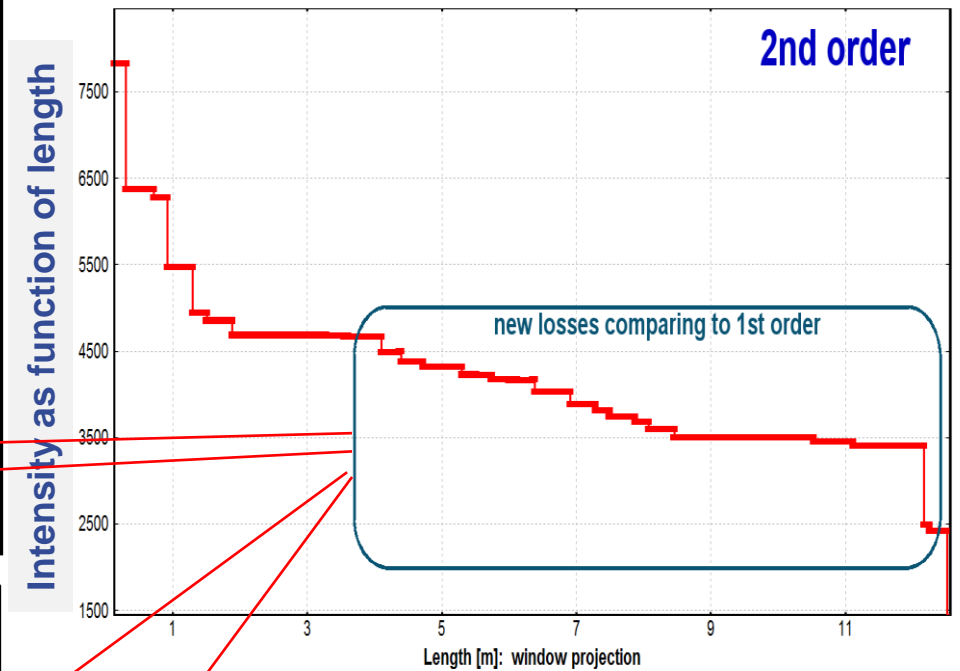
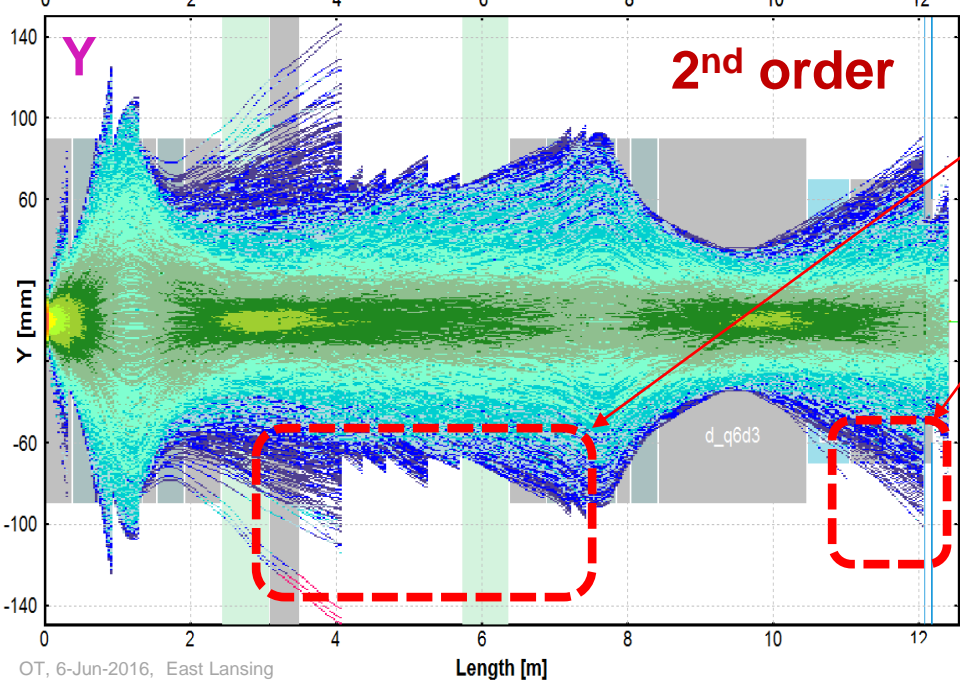
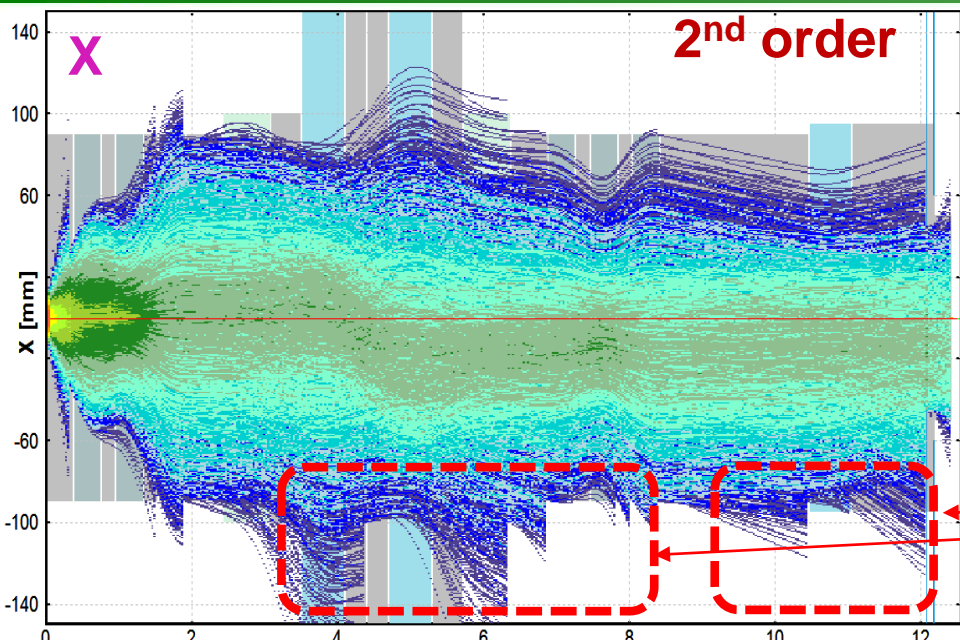
Q	Transmission including charge state production			Q-Production		Pure transmission through the separator		
	Analytical 1st order	Monte Carlo 1st order	Monte Carlo 2nd order	q-state Analyt.	q-state Monte Carlo	Analytical 1st order	Monte Carlo 1st order	Monte Carlo 2nd order
	%	%	%	%	%	%	%	%
25	0.29	0.194	0.00385	0.922	0.62	31.45	31.29	0.62
24	0.91	0.66	0.04	2.41	1.79	37.63	36.87	2.23
23	2.31	1.8	0.228	5.22	3.83	44.27	47.00	5.95
22	4.77	4.28	1.08	9.34	7.76	51.03	55.15	13.92
21	8.00	7.1	3.8	13.82	12.27	57.88	57.86	30.97
20	10.21	9.53	8.02	16.89	15.56	60.44	61.25	51.54
19	10.37	10.4	9.26	17.08	17.69	60.72	58.79	52.35
18	8.51	9.08	5.9	14.28	15.61	59.59	58.17	37.80
17	4.97	6.31	1.82	9.87	11.51	50.40	54.82	15.81
16	2.03	2.99	0.476	5.64	7.4	35.96	40.41	6.43
15	0.49	0.898	0.108	2.66	3.79	18.35	23.69	2.85
14	0.04	0.118	0.0206	1.04	1.63	3.65	7.24	1.26
Overall isotope production						52.9	54.6	31.2
(how many passed through the separator to how many produced in the target)								

1st order

2nd order







To find out why the difference between
H.Wollnik (used in LISE++) and COSY
calculations for θ^{**} & φ^{**} elements