

Neutron Spectroscopic Factors from Transfer Reactions

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Abstract

In the present paper, we examine past measurements of ground state to ground state (d,p) and (p,d) transfers that were performed on targets with $Z=3-24$. We describe a procedure that we have utilized to extract a consistent set of spectroscopic factors. Most of the 80 spectroscopic factors that we extract are in good agreement with large-basis shell model predictions. We evaluate the consistency of this method by comparing the spectroscopic factors obtained separately in (p,d) and (d,p) reactions. For nuclei where Endt has compiled values, our results and those of Endt are strongly correlated. We apply our method to more reactions and more nuclei than Endt had, and our comparisons between spectroscopic factors obtained in (d,p) and (p,d) reactions display more consistency than do the corresponding comparisons in Endt.

I. Introduction

Mathematically, a spectroscopic factor is defined by a matrix element between the initial state in the entrance channel and the final state in the exit channels [1-5]. For an $A(d,p)B$ reaction, for example, this matrix element evaluates the degree to which the wavefunction of the final nucleus B can be described by the initial nucleus A plus a neutron in a specific single particle orbit. Measurements of spectroscopic factors therefore provide quantitative information about the single particle structure of nuclei in the shell model.

In the past four decades, (d,p) , (p,d) and other single nucleon transfer reactions have been extensively used to extract spectroscopic information for single nucleon orbits [1-6]. In practice, one extracts spectroscopic factors by taking the ratios of the experimental cross-sections to the cross-sections calculated within a reaction model. In our analysis, we employ a variant of the Distorted Wave Born Approximation (DWBA) theory [3-5] as our reaction model. For (p,d) and (d,p) transfer reactions, the effects from deuteron break up can be significant at energies above 15 MeV per nucleon [7]. We take deuteron break up into account by using the Johnson-Soper adiabatic approximation [8] to construct the deuteron potential. As this approach is not strictly DWBA, we label this as the JS adiabatic three-body model.

Many of the published spectroscopic factors are not consistent. For example, it is not unusual to find published spectroscopic factors for a particular nucleus that fluctuate by factors of two to three [7]. Similarly, one can find published values from different authors for the spectroscopic factor of a given reaction that agree within uncertainties even though the data used to extract them are not in agreement. Some of the difficulties in the past extractions of spectroscopic factors have been associated with ambiguities in the optical model parameterizations used in the reaction models, different normalizations, or different assumptions used in the analysis [7, 9]. To allow comparisons of the experimental spectroscopic factors with theoretical predictions over a broad range of nuclei, we have adopted a systematic and consistent approach involving minimal assumptions and have reanalyzed existing transfer reactions data. Aspects of this minimal approach can hopefully be extended to nuclei far from stability.

In a large-scale survey of 80 nuclei studied via the transfer (p,d) and (d,p) reactions [10], we extracted the ground state spectroscopic factors using the adiabatic three-body model. Most of the extracted SF values agree with the predicted SFs from large-basis shell-model (LB-SM) calculations within the experimental and theoretical uncertainties [10]. These spectroscopic factors that we obtained over a wide range of nuclei can provide important benchmarks for comparison with more advanced reaction models for single nucleon transfer reaction mechanisms [11-12]. It is therefore important to know which sets of data are more reliable and should be included in future analysis where gaps in knowledge may lie [12].

The data analyses presented in ref. [10] were performed using transfer reaction measurements that have been performed over the past 40 years. One purpose of this paper is to set forward the criteria that we used in our data evaluation and the quality control measures that we applied to select the 235 reactions out of a larger set of 430 reactions that have been measured by many research groups [21-243,256-258]. In addition, we explain the procedure we used to extract a consistent set of spectroscopic factors from (p,d) and (d,p) transfer reactions. As described in ref. [10], the set of spectroscopic factors obtained agree well with the modern day shell model predictions and can be viewed as benchmarks for other analysis with different input or analysis criteria.

This paper is organized as follows. We begin in Section II with a brief description of the input parameters used in JS three-body adiabatic reaction model. This is important because spectroscopic factors are usually extracted by dividing the measured differential cross-sections by theoretical cross-sections, which is predicted by a reaction model. We then explain in Section III how the data have been compiled and the uncertainties introduced in the process. We explain in Section IV the procedure for extracting the SFs. Problems with consistencies between measurements are discussed in Section V-VII. Section VIII deals with the internal consistency of the approach. As the pickup (p,d) reaction is the inverse of the stripping (d,p) reaction, ground state SFs obtained separately by the (p,d) and (d,p) reactions should be the same within experimental uncertainties. We use this fact in Section VIII to assess the consistency of our method and to assign uncertainties to the extracted SFs. Section IX compares some of our SF values with those compiled by Endt [9]. Due to recent interest in the neutron spectroscopic

factor of ^{15}C , Section X discusses the challenges and problems of the reaction, $^{14}\text{C}(d,p)^{15}\text{C}$. Recently, it has been observed in nucleon-knockout reactions that spectroscopic factors are suppressed with respect to the LB-SM values with increasing nucleon separation energy [244,245]. Section XI discussed whether there is evidence for such trend in the transfer reaction data we analyzed. Section XII summarizes our findings.

II. Reaction model

For the JS three-body adiabatic model, we have adopted parameters that have been widely used in the literature for neutron-transfer reactions. The transfer cross-sections are calculated within the Johnson-Soper (JS) adiabatic approximation [8], which approximates the full many-body system by a three-body system consisting of a neutron, a proton, and an inert core. The core would be the target in a (d,p) reaction or the final nucleus in a (p,d) reaction. The phenomenological nucleon-nucleus optical model potentials (CH89) [13] are folded to construct the deuteron optical potential that is used in the DWBA integral. By using the folded potential instead of a phenomenological deuteron optical potential, one includes the main corrections to the transfer cross-section from the breakup of the deuteron in the field of the target.

Even though the breakup effect is mainly important for energies above 15 MeV per nucleon, to be consistent, we constructed the deuteron potential using the Soper-Johnson approach at all incident energies. (At low incident energies, the results obtained by using the Soper-Johnson approach are similar [7, 20] to those obtained by using the global deuteron potential of Daehnick [14].) The potential binding of the transferred neutron to the inert core was chosen to be Woods-Saxon in shape with a fixed radius parameter of 1.25 fm and a diffuseness parameter of 0.65 fm [7]. The depths of the central potential wells are adjusted to reproduce the experimental binding energies. Consistent with the findings of Ref. [15], we find that the surface properties of the neutron bound-state wave-function are dominated by the central potential. Thus, we have neglected for simplicity the spin-orbit interaction in constructing the valence neutron wavefunction. All calculations make the local energy approximation (LEA) for finite range effects [16] using the Zero-range strength ($D_0^2=15006.25 \text{ MeV}^2 \text{ fm}^3$) and range ($\beta=0.7457 \text{ fm}$) parameters of the Reid soft-core $^3\text{S}_1$ - $^3\text{D}_1$ neutron-proton interaction [17]. Nonlocality corrections with range parameters of 0.85 fm and 0.54 fm are included in the

proton and deuteron channels, respectively [18]. The same set of input parameters is used for all the reactions analyzed here. We label our SF values as SF(JS) in our figures, to distinguish them from other SF values obtained when different input parameters or potentials are used. The transfer reaction calculations were carried out using a version of the code TWOFNR [19] which respects the detailed balance between (p,d) and (d,p) reactions that connect the same states. The code TWOFNR is chosen mainly for convenience as it contains all the input options discussed below. With the same input parameters, we have employed two other widely used reaction model codes, DWUCK5 and FRESCO, and find that they provide predictions that are basically the same as those provided by TWOFNR [11, 12, 20].

III. Compilation and digitization of angular distribution data

For the present work, we mainly focus on the transfer reaction $A(d,p)B$ and its inverse reaction $B(p,d)A$ where the nucleus B is considered to be composed of the core A plus the valence neutron n . To avoid confusion, we adopt the convention that the extracted neutron spectroscopic factors always refer to nucleus B which would be the residue in a (d,p) reaction and the target in a (p,d) reaction. Table 1 contains 430 reactions that we have examined.

Nearly all the angular distributions from the published references listed in Table I have been digitized from the published figures. The few exceptions are those found in the Nuclear Science References (NSR) database of the National Nuclear Data Center (NNDC) [246]. The data from NSR are in tabulated form and the sources of these data came from the Former Soviet Union or Japan whose journals are not widely available in the United States. These non-US and non-European data complement our search in the Physical Review, Physical Review Letters, Nuclear Physics and occasionally in Physics Letters and Journal of Physics G. While we have made an effort to find nearly all the relevant experiments that published the absolute differential cross-sections, we could have missed some reactions especially if the incident energy is below 10 MeV and above 70 MeV. Except when noted, the table does not include reactions with cross-sections published in arbitrary units. The data and calculations are posted in a website [247]. Eventually, we hope all the digitized data used in this work will be adopted by the NSR.

By checking some of the data carefully and sometimes repeating the digitization several times, we estimate the uncertainties introduced by the digitization process to be less than 0.5 deg in determining the angles and less than 10% in extracting the differential cross-sections. For illustration, we use the data for the reaction $^{14}\text{N}(\text{d},\text{p})^{15}\text{N}$ at $E_d=12$ MeV [23, 84]. This set of data was first published in tabulated form in ref. [23]. The tabulated data are plotted as closed points in Figure 1. Later the authors in ref. [84] plotted the data in a figure, which we digitized. We compare our digitized data (open points) with the tabulated data (closed points) in Figure 1. We see a difference of less than 10% between the two sets of data. Of course, the digitization errors also depend on the actual size of the graphs available in the original literature. As described later, generally, errors introduced by digitization are relatively small compared to the uncertainties in the absolute cross-section measurements.

IV. Extraction of spectroscopic factors

For nearly all the nuclei we study, we use the ground state ℓ values determined from the angular distributions and the \mathbf{j}^π values of the valence neutron ground states found in the isotope tables [248]. In general, the experimental angular distributions at larger angles are more sensitive to details of the optical potential, the effects of inelastic couplings and other higher-order effects are not well reproduced by most reaction models. Furthermore, discrepancies between the shapes from calculations and experiment are much worse at the cross-section minimum, which could give these points an unduly large weight in a least squares minimization procedure. Thus, we follow the procedures used by many groups in the past 40 years that the spectroscopic factor is extracted by fitting the reaction model predictions to the angular distribution data at the first peak, with emphasis on the maximum. The accuracy in absolute cross-section measurements near the peak is most important. When possible, we take the mean of as many points near the maximum as we can to extract the spectroscopic factors. We will use the angular distributions of $^{14}\text{N}(\text{d},\text{p})^{15}\text{N}$ shown in Fig 1 to illustrate the procedure we adopt to extract the spectroscopic factors.

In Figure 1, the first three data points with $\theta_{\text{cm}} < 25^\circ$ have been used to determine the ratios of the measured and calculated differential cross-sections. The mean of these three ratios is adopted as the spectroscopic factor. For example, for the two sets of data

plotted in Figure 1, the spectroscopic factors are 1.1 and 1.2 for tabulated data [23] and digitized data [84] respectively. The difference in the spectroscopic factors represents the uncertainties introduced by digitization. The theoretical angular distributions, obtained from TWOFNR have been multiplied by the spectroscopic factor, 1.1, and plotted as the solid curve in the figure.

In cases when a “first peak” is not obvious or that the angular distributions of the forward angles are nearly flat, e.g. in the reaction of $^{44}\text{Ca}(p,d)^{43}\text{Ca}$ at $E_p=40$ MeV [177] as shown in Figure 2, we find that fitting the shoulder gives more consistent results. In general, the agreement of the measured shape of the angular distributions in the vicinity of the first peak or the shoulder to the shape predicted by the transfer model gives some indication as to the quality of the spectroscopic information that can be extracted by comparing the model to data. When there are more than one set of data that can be used to determine a given spectroscopic factor, we use the number of measured data points from a given measurement that lie in the peak or shoulder region where data and theory are in good agreement to assign a relative weight for the SF extracted from that measurement. Various SF’s extracted from different measurements are combined in a weighted average to compute the mean spectroscopic factors presented here.

V. Evaluation of the angular distribution measurements

Even though most papers state the uncertainties of their cross-section measurements to be 10-20%, the actual disagreements between experiments are often larger than the quoted uncertainties. An example is illustrated in the reactions $^{11}\text{B}(d,p)^{12}\text{B}$ reactions. From the conventional literature, we find two measurements: one measurement at deuteron incident energy of 11.8 MeV [47] and another measurement at 12 MeV [23]. Since the incident deuteron energy is nearly the same, one would expect the angular distributions from the two data sets plotted in Figure 3 to be the same within experimental error. Ref. [23] (open circles) stated that the accuracy of the absolute cross-section measurements is 15% while ref. [47] (closed circles) quoted an error of 6%, which is smaller than the symbols in Fig 3. Not only do the cross-sections differ sometimes by a factor of two, the shapes of the distributions (especially the first peak) are not even the same. In this case, the shape of the angular distributions in ref. [47] agrees with the calculation (solid curve) better than that measured in ref. [23]. Fortunately for

this reaction, we are able to find another measurement in the NNDC database [48] (open diamonds). Near the peak at forward angles, this latter angular distribution agrees with ref. [47] and so we disregard the measurements of ref [23]. Data in ref. [47] were measured nearly 40 years later than data in ref. [23] and one might be tempted to attribute the difference to the availability of better beam quality and detection systems for the measurements. However, when another reaction, $^{12}\text{C}(\text{d,p})^{13}\text{C}$ at $E_d=11.8$ MeV from ref. [47] (closed circles) is compared to three other published angular distributions in Figure 4 at $E_d=11.8$ MeV (closed diamonds) [32], 12 MeV (open circles) [23], 12 MeV (open diamonds) [61], the cross-sections in the first peak measured in ref. [47] is consistently low. No uncertainties in the measurements are given in ref. [32] and ref. [61] but it is clear that data in ref. [47] do not agree with the other measurements, especially in the most forward angle region. Thus we disregard the SF values derived from ref. [47] in our compilation of $^{12}\text{C}(\text{d,p})^{13}\text{C}$ reactions. The authors of ref [47] cannot explain the discrepancies described here [249]. In general, data taken by the same group with the same setup sometimes have similar systematic errors that lead to rejection of the entire data set. When there are independent measurements available for comparison, however, cross comparisons to other data can allow one to be more selective. The existence of confirming data, allowed us to keep $^{11}\text{B}(\text{d,p})^{12}\text{B}$ data and discard the $^{12}\text{C}(\text{d,p})^{13}\text{C}$ data even though both sets of data come from ref [47].

Cross comparisons of angular distributions sometimes help to establish common systematic problems when one set of measurements was performed by the same group with the same set up. An example is illustrated in the $^{40}\text{Ca}(\text{d,p})^{41}\text{Ca}$ reactions in ref. [184] where the ground state angular distributions of ^{41}Ca at $E_d=7, 8, 9, 10, 11$ and 12 MeV have been measured. Figure 5 shows the extracted spectroscopic factors (labeled as SF(JS)) as a function of incident deuteron energy for all the $^{40}\text{Ca}(\text{d,p})^{41}\text{Ca}$ reactions. For clarity in presentation, no error bars are plotted. Except for the point at $E_d=7$ and 12 MeV, the extracted spectroscopic factors from ref. [184] (open circles) are consistently larger than the spectroscopic factors extracted from other experiments that probed the same reaction at the same energy. Detailed comparisons of the angular distribution data show essentially the same effect, that the differential cross-sections measured in ref. [184] are systematically higher than the other measurements [32, 181, 185-194] measured

by different groups. Clearly, there must be some problems in the determination of the absolute cross-sections in ref. [184]. As it is not possible to find the cause of this discrepancy after so many years, we disregard the spectroscopic factor values determined in ref. [184] in our review of the data.

Similarly we disregard the data in ref. [31] for the ${}^9\text{Be}(d,p){}^{10}\text{Be}$ reaction as most of the data in ref. [31] are low when compared to the available data from other measurements. There are other examples. All the SF values not used are listed in Column 5 of Table I. In general, a brief comment follows in the last column of Table I if the data set is considered to be problematic.

The disagreements between data sets generally exceed the quoted uncertainties of the experimenters. Indeed, we have found that the most important aspect of quality control of the data is to have as many independent measurements as possible. Comparisons of different measurements help to identify problematic measurements. The large number of measurements compiled in Table I have helped to improve the quality of the spectroscopic factors extracted in the present work.

VI. Transfer reactions at high and low energy

When Q-value, the momentum transfer or angular momentum transfer are not well-matched or there are significant contributions from the compound nucleus, the shape of the experimental angular distributions may be poorly described by theory. We find better agreement for ground state transfers at incident energies of around 10-20 MeV and poorer agreement at very low or high (> 50 MeV) beam energies. Figure 6 shows the angular distributions of protons emitted from the ${}^{40}\text{Ca}(d,p){}^{41}\text{Ca}$ (g.s) reaction from $E_d=4.7$ to 56 MeV. Only one angular distribution is shown at each incident energy. The agreement between data and prediction for the first peak improves with increasing energy. At very low incident energy, the shapes of the measurements and the calculated transfer cross-sections do not agree. This phenomenon is also seen in other reactions. The spectroscopic factors as a function of incident energy are shown in Figure 5. The increase of spectroscopic factors at $E_d < 10$ MeV has been observed before [7, 23] and has been attributed to the resonance structures in the elastic scattering of the deuterons [250]. As explained in the last section, the open points based on the data from ref. [184] are discarded. Between 10 to 56 MeV, we find that the mean spectroscopic factor, $1.01 \pm$

0.06 shown by the solid line in Figure 5, describes the data at all energies within experimental errors.

In reactions which have large negative Q values such as $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}$ ($Q = -16.5$ MeV), the center of mass energy available in the exit channel is very small even at ~ 20 MeV proton incident energy [40]. The validity of the calculated angular distribution is questionable at these energies and we discard these data. For other reactions measured at low incident energy (< 10 MeV), the data could be dominated by compound nucleus emissions, or resonances in the low energy elastic scattering [250]. When possible, we exclude spectroscopic factors obtained with incident beam energy less than 10 MeV when computing the mean values of the spectroscopic factors. These “excluded” spectroscopic factors are listed in Column 5 of Table I.

Even though we exclude data with incident energy lower than 10 MeV from the calculation of the mean SF, these low energy data are still valuable. In cases where very few (sometimes only one) measurements with incident energy greater than 10 MeV are available, they provide checks for consistency of the measurements. Examples are $^{49}\text{Ti}(\text{p},\text{d})^{48}\text{Ti}$ and $^{48}\text{Ti}(\text{d},\text{p})^{49}\text{Ti}$ reactions [149, 214, 221, 222]. In the $^{43}\text{Ca}(\text{d},\text{p})^{44}\text{Ca}$ reaction, only data at 8.5 MeV [201] are available. Similarly, we only have data at 7.5 MeV for the $^{50}\text{V}(\text{d},\text{p})^{51}\text{V}$ reaction [224] and at 7.83 MeV for the $^{23}\text{Na}(\text{d},\text{p})^{24}\text{Na}$ reaction [112]. We adopt these results despite their low incident energies.

At high energies, momentum transfer and angular momentum transfer are mismatched so conditions may not be optimized to extract reliable spectroscopic factors. Furthermore, the global nucleon-nucleus potentials (CH89) [13] are fitted only to 65 MeV for protons and to 26 MeV for neutrons. Thus, we do not include data from reactions at incident energy greater than 65 MeV in this work. In examining data over a wide range of d or p incident energies, we find that the optimum beam energies for studying transfer reactions lie between 10-20 MeV per nucleon.

VII. Nuclei with small spectroscopic factors compared to Independent Particle Model predictions

For the $^{50}\text{Cr}(\text{p},\text{d})^{49}\text{Cr}$ reactions, there are two measurements at beam energy of 17.5 and 55 MeV [227, 228]. In each case, the predicted and measured angular distributions are different as shown in Figure 7 with closed circles for 17.5 MeV [227]

data and open circles for 55 MeV data [228]. From the magnitude of the measured cross-sections, a spectroscopic factor value of 0.11 is derived. The extracted spectroscopic factor is very low especially for an even-even nucleus. It is reasonable to speculate that there is considerable configuration mixing of the valence nucleus. When very low SF values compared to values predicted by the Independent Particle Model [3-5] are obtained for ground state transitions, sometimes, we find that the predicted shape of the angular distributions may not agree well with that of the data. This may indicate that one step transfer amplitudes are not dominant and comparison of data to such calculations may be unreliable. Other examples are ^{20}F , ^{21}Ne , ^{22}Ne , ^{24}Mg , ^{35}Cl , ^{45}Sc , ^{47}Ti , ^{48}Ti , ^{50}Cr , and ^{51}V nuclei.

In the case of the $^{46}\text{Ti}(d,p)^{47}\text{Ti}$ reaction [217, 281, 219], both measurements at $E_d=7$ and 10 MeV are very different from the predicted cross-sections and disagree with each other in shape and absolute cross-sections. We did not extract spectroscopic factors for this nucleus.

VIII. Comparison of Spectroscopic factors obtained from (p,d) and (d,p) reactions

The neutron pickup (p,d) and neutron stripping (d,p) reactions are inverse reactions, both of which connect the ground states of the nuclei in the entrance and exit channels. They should yield the same values for the spectroscopic factors. From Table I, we select the nuclei, which have been studied reasonably well by both neutron pick-up and stripping reactions to the ground state. The averaged SF values are listed in the 2nd and 4th column of Table II. The numbers of measurements contributing to the averages are listed next to the mean values in the 3rd and 5th column.

There are strong correlations between the spectroscopic factors determined from the (p,d) and (d,p) reactions as shown in Figure 8. The solid line corresponds to perfect agreement. These are independent values determined using the procedure outlined above. The scatter of the data points about the solid line can be used to determine an overall uncertainty for such analyses. As explained in Section V, the quoted experimental uncertainties are not always reliable. In the absence of a completely independent criterion that can be applied to each data set without comparison to others, we assume the uncertainty of each measurement to be the same, even though certain experiments may actually be more accurate than others. If we require the chi-square per degree of freedom

of the scatter data shown in Figure 8 to be unity, we can extract a random uncertainty of 20% for a given measurement. The obtained uncertainty of 20% is consistent with comparisons with analysis on systems that have large number of measurements such as $^{12}\text{C}(d,p)^{13}\text{C}$, $^{16}\text{O}(p,d)^{15}\text{O}$, $^{16}\text{O}(d,p)^{17}\text{O}$, $^{40}\text{Ca}(d,p)^{41}\text{Ca}$ and other reactions. Examinations of large number of measurements in Table I suggest that the uncertainties in the extraction of the spectroscopic factors are largely limited by the disagreement between measurements. In Table II and Figure 8, we have excluded measurements for ^7Li , ^{34}S and ^{10}Be nuclei due to large errors associated with either the (p,d) or (d,p) measurements. If we include these three measurements, the estimated uncertainty in a given measurement increases to 28%

Finally, we can compute the spectroscopic factor values and the associated uncertainties. These values are listed in Table III. We list the SF values that are obtained from the weighted average of independent measurements from both the (p,d) and (d,p) reactions in Table I. In these weighted averages, the low energy (<10 MeV) data and the inconsistent data (nominally marked with asterisks) that differ significantly from other sets of data are excluded. For values determined from only one measurement without the consistency checks provided by other independent measurements, an associated uncertainty of 28% is assigned. For values determined by more than one measurement (N), we take into account the distribution of the SF's around the mean. Figure 9 illustrates this procedure. The open stars in Figure 9 represent the spectroscopic factors extracted from the good measurements of the calcium isotopes. However, the spread of the data are more than 20% for the ^{44}Ca and ^{48}Ca nuclei even though three “good” measurements are found for each of these nuclei. For these nuclei, it is more realistic to assign the uncertainty using the standard deviations of the mean of the data points. Each of the associated uncertainties listed in Table III is determined by adopting either the standard deviation of the mean or an uncertainty of $20\%/\sqrt{N}$, depending on which of the two uncertainties is larger. For comparison, the mean SF values with the associated uncertainties are plotted as the solid stars with error bars in Figure 9.

IX. Comparison with Endt's “best values”

In 1977, Endt compiled a list of the “best” spectroscopic factor values for the sd-shell nuclei [9]. For the neutron spectroscopic factors, Endt compiled the published

spectroscopic factors from (d,t), (p,d), ($^3\text{He},\alpha$) and (d,p) reactions. An uncertainty of 25% is assigned to the values. (When only the (p,d) and (d,p) reactions are studied, Endt assigned a 50% uncertainties.) Endt's best values are listed in Table III. Figure 10 compares the spectroscopic factors determined by Endt and the present work (SF(JS)). There are strong correlations between the two procedures even though the values scatter around the dashed line, which indicates perfect agreement. From the consistency check with (p,d) and (d,p) reactions, we expect that our values should have smaller random uncertainties because a systematic approach is used to extract the SF values directly from the measured angular distributions while Endt's compilation depended on the analysis by different authors and relied on the communication with the authors concerning the normalizations of the spectroscopic factors. We also have the advantage that many more measurements are included in Table I than those that were available for Endt's compilations.

X. $^{14}\text{C}(\text{d,p})^{15}\text{C}$ reactions

The $^{14}\text{C}(\text{d,p})^{15}\text{C}$ reaction is an important reaction because ^{15}C has a loosely bound halo neutron. It has been used to provide cross-comparisons between the spectroscopic factors obtained from one-nucleon knock-out and transfer reactions [251]. In addition, this reaction is a good candidate to extract spectroscopic factors using the combined asymptotic normalization coefficient (ANC) method [252].

For the $^{14}\text{C}(\text{d,p})^{15}\text{C}$ reaction, there are three measurements [76, 77 and 73] with $E_d=14, 16, \text{ and } 17 \text{ MeV}$. When data from these references are plotted in Figure 11, they do not agree with each other within a factor of two even though the spectroscopic factors quoted in the original references are within 20% of each other (0.88 [76], 0.99 [77], 1.03 [73]). This underscores the importance of analysis with a systematic and consistent approach as studied here.

Since we generally exclude data that do not measure the first forward angle peak, data taken at 16 MeV (closed squares) and 17 MeV (open circles) [77, 73] are discarded. The predicted angular distribution shape (solid curve) shows good agreement with data at 14 MeV [76] at angles less than 15° . Based on the criterion outlined above, we extracted the SF from this data set. However for such an important nucleus, a second independent

measurement with data at forward angles would be desirable to determine the spectroscopic factor of the loosely bound neutron ($S_n=1.22$ MeV).

XI. Dependence of spectroscopic factors on neutron separation energy

Recent measurements of spectroscopic factors from single-nucleon “knock-out” reactions with radioactive and stable nuclei show increasing quenching of the spectroscopic factor values with nucleon separation energy [244, 245]. The wide range of isotopes studied in this work and listed in Table III includes nuclei with neutron-separation energies ranging from 0.5 to 19 MeV. To examine any quenching trend, we compute the neutron spectroscopic factors using Oxbash, a large-basis shell model code [253, 254]. The model space and the interactions used in the calculations are listed in Table III. Using truncated model space, we are able to obtain more spectroscopic factors (^{37}S , ^{38}Cl , ^{39}Ar , ^{40}Ar , ^{41}Ar , ^{40}K , ^{41}K , and ^{42}K) than those published in Ref. [10]. Due to the amount of CPU times involved, we cannot compute the SF values from Oxbash for every nucleus. Attempts are being made to extend Oxbash shell model calculations to Ti and Cr isotopes using high performance computing facilities [255].

Figure 12 shows the ratio of the experimental SF values to the LB-SM values from Oxbash as a function of the neutron separation energy. Within the experimental uncertainties, we do not see the systematic quenching of the spectroscopic factors with increasing nucleon separation energy reported for measurements of nucleon knockout reactions induced by radioactive beams. Rather, there seems to be some indication that the trend is the opposite, i.e., the SF values are smaller than the predicted values for nuclei with small neutron separation energy. This trend persists in a smaller subset of the nuclei such as the Ca isotopes plotted as solid stars.

The structures of the neutron rich nuclei with small neutron separation energy are of general interest. For loosely bound nuclei, knockout reactions with radioactive beams suggest no quenching. In our data set, there are seven nuclei with $S_n < 4$ MeV, ^8Li , ^9Be , ^{11}Be , ^{12}B , ^{15}C , ^{16}N , and ^{19}O . Except for ^{15}C , which was discussed in previous section, the fits and quality of the data are comparable to that of the other data we have examined. However, the experimental SF values for these nuclei are consistently smaller than the large-basis shell-model predictions. (If we relax the criterion to $S_n < 5$ MeV, the conclusion is similar.) To be sure, we do not have many nuclei and they are all light

nuclei with $Z \leq 8$. Furthermore, the suppression ratios vary from 0.44 to 0.79 for the six nuclei we examined. Excluding ^{15}C , the average quenching factor is 0.6. The SF values (as a group) do not agree with the LB-SM predictions. These results may indicate that the standard global potential [13] may not be appropriate to describe the scattering of these weakly bound nuclei with diffuse surfaces. Furthermore, target break-up may have to be explicitly taken into account when calculating transfer processes involving nuclei with very small neutron separation energies (< 2 MeV). Further study with improved theoretical inputs is needed to understand these nuclei with loosely bound neutrons.

XII. Summary

In summary, we have evaluated angular distribution measurements from past (p,d) and (d,p) transfer reactions using targets ranging from Li to Cr isotopes. Problems with past measurements are discussed and resolved mainly by comparing the data of several independent measurements. We observe problems with the consistencies between measurements. We expect such problems are not limited to the data studied here. The procedure developed to monitor the quality control of the data sets should be applicable to other analysis with large number of data sets. Based on the analysis of the evaluated data and a reaction model with minimum assumptions, we develop a consistent approach to extract spectroscopic factors. Comparisons between spectroscopic factors obtained from (p,d) and (d,p) reactions, suggest that most of the extracted values have uncertainties less than 20%. Thus our SF values have smaller random uncertainties than the values compiled by Endt. Furthermore, the method should be applicable to other stable beams and maybe rare isotope beam experiments. The present compilation of the neutron ground state spectroscopic factors of 80 nuclei provides important reference points for more sophisticated theoretical work on transfer reactions and development in nuclear structure model. For most nuclei, the agreement between data and LB-SM predictions is within 20%. Even though most of the nuclei studied are close to the valley of stability, the nuclei studied here range in neutron separation energy from 0.5 to 19 MeV. The present work does not support the observation that spectroscopic factors are suppressed with increasing neutron separation energy as found in nucleon knockout reactions.

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Table I: List of reactions studied in this work. SF(JS) stands for spectroscopic factors extracted in the present work. Not all the SF(JS) values extracted are used in computing the averages of the spectroscopic factor for a specific nucleus. The extracted values not used are listed in the 5th column. Most of these include reactions at low beam energy ($E_{\text{beam}} < 10$ MeV). Those values marked with * are obtained from data which are determined to be problematic. Listed in the last column are abbreviated comments, BS (bad shape), BD (bad data), AU (arbitrary unit), No (Normalization problem), NP (missing first peak), and QV (low Q-values).

B	A(d,p)B or B(p,d)A	E_{beam} (MeV)	Reference	SF(not used)	SF(JS)	$\langle \text{SF}(J, S) \rangle$	# of points	Comment
⁶ Li	⁶ Li(p,d) ⁵ Li	33.6	[21]		1.12	1.12	3	
⁷ Li	⁶ Li(d,p) ⁷ Li	4.5	[22]	1.59			2	
⁷ Li	⁶ Li(d,p) ⁷ Li	4.75	[22]	1.81			2	
⁷ Li	⁶ Li(d,p) ⁷ Li	5	[22]	1.90*			2	BS
⁷ Li	⁶ Li(d,p) ⁷ Li	5.25	[22]	1.78			3	
⁷ Li	⁶ Li(d,p) ⁷ Li	5.5	[22]	1.70			3	
⁷ Li	⁶ Li(d,p) ⁷ Li	12	[23]		1.85	1.85	2	
⁷ Li	⁷ Li(p,d) ⁶ Li	30.3	[24]	0.34*			3	BS
⁷ Li	⁷ Li(p,d) ⁶ Li	33.6	[21]	0.86*			3	BS
⁸ Li	⁷ Li(d,p) ⁸ Li	12	[23]		0.62	0.62	3	
⁹ Li	⁸ Li(d,p) ⁹ Li	10.7	[??]	0.56			2	BS
⁹ Li	⁸ Li(d,p) ⁹ Li	19.1	[25]		0.98	0.98	5	
⁹ Be	⁹ Be(p,d) ⁸ Be	5	[26]	0.43			7	
⁹ Be	⁹ Be(p,d) ⁸ Be	6	[26]	0.47			4	
⁹ Be	⁹ Be(p,d) ⁸ Be	7	[26]	0.45			3	
⁹ Be	⁹ Be(p,d) ⁸ Be	8	[26]	0.51			3	
⁹ Be	⁹ Be(p,d) ⁸ Be	9	[26]	0.53			2	
⁹ Be	⁹ Be(p,d) ⁸ Be	10	[26]		0.46		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	11	[26]		0.46		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	14.3	[27]		0.41		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	15	[28]		0.42		3	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	17	[29]		0.51		3	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	21	[29]		0.50		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	25	[29]		0.43		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	26.2	[27]	0.35*			1	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	29.1	[29]		0.48		2	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	33.6	[21]		0.44		1	BS
⁹ Be	⁹ Be(p,d) ⁸ Be	46	[30]		0.49	0.45	1	BS
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	4.5	[22]	2.44			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	4.75	[22]	2.11			3	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	5	[22]	2.14			2	

¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	5.25	[22]	2.06			3	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	5.5	[22]	2.01			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	5.75	[22]	1.83			3	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	6	[22]	2.01			3	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	6.5	[31]	1.55			5	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	7	[31]	1.48			4	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	7.5	[31]	1.07			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	8	[31]	1.05			1	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	8.5	[31]	1.11			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	9	[31]	1.10			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	9.5	[31]	1.03			2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	10	[31]	1.10*			2	NP
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	10.5	[31]	1.18*			2	NP
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	11	[31]	1.17*			2	BD
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	11.8	[23]		1.49		3	BD
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	11.8	[32]		1.42		2	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	12.5	[33]		1.72		4	NP
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	15	[34]		1.75		4	
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	15.3	[35]		1.40	1.58	4	NP
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	17.3	[36]	0.99*			3	BS
¹⁰ Be	⁹ Be(d,p) ¹⁰ Be	28	[37]	2.26*			2	BS
¹⁰ Be	¹⁰ Be(p,d) ⁹ Be	49.8	[38]	2.96*			10	BD
¹¹ Be	¹⁰ Be(d,p) ¹¹ Be	12	[28]		0.44		3	
¹¹ Be	¹⁰ Be(d,p) ¹¹ Be	25	[39]		0.53	0.49	3	
¹¹ Be	¹¹ Be(p,d) ¹⁰ Be	35.3	[40]		0.57	0.57	2	
¹⁰ B	¹⁰ B(p,d) ⁹ B	33.6	[41]		0.57		4	
¹⁰ B	¹⁰ B(p,d) ⁹ B	49.5	[42]		0.43	0.50	3	
¹¹ B	¹⁰ B(d,p) ¹¹ B	4.5	[22]	1.11			2	
¹¹ B	¹⁰ B(d,p) ¹¹ B	4.75	[22]	1.06			3	
¹¹ B	¹⁰ B(d,p) ¹¹ B	5	[22]	0.92			2	
¹¹ B	¹⁰ B(d,p) ¹¹ B	5.25	[22]	0.85			2	
¹¹ B	¹⁰ B(d,p) ¹¹ B	5.5	[22]	0.81			2	
¹¹ B	¹⁰ B(d,p) ¹¹ B	8.2	[43]	5.05			3	AU
¹¹ B	¹⁰ B(d,p) ¹¹ B	10.1	[44]	1.00*			4	BD
¹¹ B	¹⁰ B(d,p) ¹¹ B	12	[23]		1.25		2	BS
¹¹ B	¹⁰ B(d,p) ¹¹ B	13.5	[45]		1.68		5	
¹¹ B	¹⁰ B(d,p) ¹¹ B	15.5	[43]	1.50*			6	AU
¹¹ B	¹⁰ B(d,p) ¹¹ B	21.5	[43]	0.32*			9	AU
¹¹ B	¹⁰ B(d,p) ¹¹ B	28	[37]		1.52	1.55	2	
¹¹ B	¹⁰ B(d,p) ¹¹ B	28	[43]	0.06*				AU
¹¹ B	¹¹ B(p,d) ¹⁰ B	19	[46]	3.16*			3	BD
¹¹ B	¹¹ B(p,d) ¹⁰ B	33.6	[41]		1.29	1.29	3	

¹¹ B	¹¹ B(p,d) ¹⁰ B	44.1	[38]	1.05*			2	BD
¹² B	¹¹ B(d,p) ¹² B	11.8	[47]		0.44		5	
¹² B	¹¹ B(d,p) ¹² B	12	[48]		0.47	0.45	3	
¹² B	¹¹ B(d,p) ¹² B	12	[23]	0.35*			1	BS
¹² C	¹² C(p,d) ¹¹ C	19.3	[49]					QV
¹² C	¹² C(p,d) ¹¹ C	19.5	[49]					QV
¹² C	¹² C(p,d) ¹¹ C	20	[49]					QV
¹² C	¹² C(p,d) ¹¹ C	30.3	[50]		2.68		3	
¹² C	¹² C(p,d) ¹¹ C	39.8	[51]	5.50*			4	No
¹² C	¹² C(p,d) ¹¹ C	61	[52]		3.36		6	
¹² C	¹² C(p,d) ¹¹ C	65	[53]		3.07	3.12	3	
¹² C	¹² C(p,d) ¹¹ C	65	[54]	3.03*			1	BS
¹³ C	¹² C(d,p) ¹³ C	4	[55]	0.64			3	
¹³ C	¹² C(d,p) ¹³ C	4.5	[55]	0.67			2	
¹³ C	¹² C(d,p) ¹³ C	4.5	[56]	0.59			2	
¹³ C	¹² C(d,p) ¹³ C	4.5	[57]	0.43			2	
¹³ C	¹² C(d,p) ¹³ C	7.15	[58]	0.88			4	
¹³ C	¹² C(d,p) ¹³ C	8.9	[59]	0.92			6	
¹³ C	¹² C(d,p) ¹³ C	10.2	[60]		0.85		3	
¹³ C	¹² C(d,p) ¹³ C	11.8	[32]		0.82		3	
¹³ C	¹² C(d,p) ¹³ C	11.8	[47]	0.60*			2	BD
¹³ C	¹² C(d,p) ¹³ C	12	[61]		0.71		2	
¹³ C	¹² C(d,p) ¹³ C	12	[23]		0.87		3	
¹³ C	¹² C(d,p) ¹³ C	12.4	[60]		0.78		4	
¹³ C	¹² C(d,p) ¹³ C	14.7	[60]		0.72		3	
¹³ C	¹² C(d,p) ¹³ C	14.8	[62]		0.77		1	
¹³ C	¹² C(d,p) ¹³ C	15	[63]		0.68		2	
¹³ C	¹² C(d,p) ¹³ C	16.6	[64]		0.59		2	
¹³ C	¹² C(d,p) ¹³ C	19.6	[64]		0.61		2	
¹³ C	¹² C(d,p) ¹³ C	25.9	[65]		0.66		6	
¹³ C	¹² C(d,p) ¹³ C	30	[66]		0.62	0.73	2	BS
¹³ C	¹² C(d,p) ¹³ C	51	[38]					BD
¹³ C	¹² C(d,p) ¹³ C	56	[67]	0.99*			1	NP
¹³ C	¹³ C(p,d) ¹² C	35	[68]		0.79		2	BS
¹³ C	¹³ C(p,d) ¹² C	41.3	[69]		0.86		1	BS
¹³ C	¹³ C(p,d) ¹² C	48.3	[38]		0.90		5	BS
¹³ C	¹³ C(p,d) ¹² C	55	[70]		0.67	0.81	3	BS
¹³ C	¹³ C(p,d) ¹² C	65	[54]	1.61*			3	NP
¹⁴ C	¹³ C(d,p) ¹⁴ C	12	[23]		1.94		5	
¹⁴ C	¹³ C(d,p) ¹⁴ C	13	[71]		1.61	1.82	3	NP
¹⁴ C	¹³ C(d,p) ¹⁴ C	56	[67]	2.34*			2	NP
¹⁴ C	¹⁴ C(p,d) ¹³ C	14.5	[72]	0.88*			4	NP

¹⁴ C	¹⁴ C(p,d) ¹³ C	18.5	[46]		1.87		3	
¹⁴ C	¹⁴ C(p,d) ¹³ C	27	[73]		1.02		4	
¹⁴ C	¹⁴ C(p,d) ¹³ C	35	[74]		1.66	1.50	5	
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	2	[75]	1.07				
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	2.6	[75]	0.66				
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	3	[75]				2	
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	3.4	[75]				2	
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	14	[76]		1.12	1.12	1	
¹⁵ C	¹⁴ C(d,p) ¹⁵ C	16	[77]					NP
¹⁵ C	¹⁴ C	17	[73]	0.42*				BS
¹⁴ N	¹⁴ N(p,d) ¹³ N	14.5	[72]		0.68		5	
¹⁴ N	¹⁴ N(p,d) ¹³ N	18.5	[78]		0.76		3	
¹⁴ N	¹⁴ N(p,d) ¹³ N	21	[79]	0.60*			2	NP
¹⁴ N	¹⁴ N(p,d) ¹³ N	30.3	[80]		1.00	0.77	2	
¹⁴ N	¹⁴ N(p,d) ¹³ N	65	[53]	0.48*			2	NP
¹⁵ N		10	[81]					BD
¹⁵ N		10.03	[82]		1.66		2	
¹⁵ N		11.65	[82]					
¹⁵ N	¹⁴ N(d,p) ¹⁵ N	12	[23]		1.12		3	
¹⁵ N	¹⁴ N(d,p) ¹⁵ N	14.8	[83]				5	
¹⁵ N	¹⁴ N(d,p) ¹⁵ N	31	[84]			1.39	3	
¹⁵ N	¹⁴ N(d,p) ¹⁵ N		[84]	1.94*				BD
¹⁵ N	¹⁵ N(p,d) ¹⁴ N	18.6	[78]		1.76		4	
¹⁵ N	¹⁵ N(p,d) ¹⁴ N	39.8	[85]		1.43	1.65	2	
¹⁶ N	¹⁵ N(d,p) ¹⁶ N	14.8	[83]		0.42	0.42	4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	18.5	[46]	1.74*			4	BS
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	19	[46]	2.33*			5	BS
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	20	[46]		2.32		4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	21.27	[86]	1.69*			5	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	25.52	[86]		2.82		4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	30.3	[50]		2.31		4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	31.82	[86]		2.29		2	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	38.63	[86]		2.09		4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	39.8	[51]		2.59		2	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	45.34	[86]		2.70		4	
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	65	[53]	2.32*		2.46	1	NP
¹⁶ O	¹⁶ O(p,d) ¹⁵ O	65	[54]	2.75*			1	NP
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	1.3	[55]					
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	2.279	[87]					
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	2.582	[87]	1.54			1	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	2.864	[87]	1.54			1	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	3.155	[87]	1.56			1	

¹⁷ O	¹⁶ O(d,p) ¹⁷ O	3.49	[60]	2.57			2	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	4	[55]	2.39			4	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	4.11	[60]	2.11			2	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	6	[88]	1.24			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	6.26	[89]	1.17			3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	7.5	[88]	1.26			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	7.85	[88]	1.22			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	8	[90]	1.40			1	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	8.2	[88]	1.11			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	8.55	[88]	0.96			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	9	[60]	0.98			3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	9.3	[91]	0.88			3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	10	[88]		1.04		3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	10.2	[60]		0.78		2	BD
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	11	[88]		0.88		2	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	11.8	[32]	0.62*			3	BS
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	12	[92]	0.47*			4	BD
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	12.4	[60]		1.03		3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	13.3	[91]		1.13		5	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	14.8	[60]		0.98		2	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	15	[93]		1.02		3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	19	[60]	0.81*			1	BS
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	25.4	[94]		0.89		3	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	26.3	[95]	1.37*			6	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	36	[94]		0.87		4	
¹⁷ O	¹⁶ O(d,p) ¹⁷ O	63.2	[94]		1.07	0.99	3	
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	8.62	[96]	1.10			4	
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	9.56	[96]	1.01			2	BS
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	10.5	[96]		0.78		4	
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	11.16	[96]	0.70*			2	BS
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	11.44	[96]		0.74		4	
¹⁷ O	¹⁷ O(p,d) ¹⁶ O	31	[97]		0.99	0.81	2	
¹⁸ O	¹⁷ O(d,p) ¹⁸ O	18	[98]		1.80	1.80	3	
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	17.6	[46]		1.72		4	
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	18.2	[99]		1.43	1.60	3	
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	20	[100]	0.79*			2	BS
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	24.4	[100]	1.50*			2	BS
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	29.8	[100]	1.40*			3	BS
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	37.5	[100]	0.97*			1	NP
¹⁸ O	¹⁸ O(p,d) ¹⁷ O	43.6	[100]	1.01*			2	BD
¹⁹ O	¹⁸ O(d,p) ¹⁹ O	10	[101]	0.63*			1	NP
¹⁹ O	¹⁸ O(d,p) ¹⁹ O	14.8	[102]		0.47		4	

¹⁹O	¹⁸ O(d,p) ¹⁹ O	15	[103]		0.38	0.43	3	
¹⁹F	¹⁹ F(p,d) ¹⁸ F	18.5	[78]		1.62		4	
¹⁹F	¹⁹ F(p,d) ¹⁸ F	19.3	[104]		1.58	1.60	3	
²⁰F	¹⁹ F(d,p) ²⁰ F	12	[105]		0.013	0.013	3	
²⁰F	¹⁹ F(d,p) ²⁰ F	16	[106]					BD
²¹Ne	²⁰ Ne(d,p) ²¹ Ne	11	[107]		0.044		2	
²¹Ne	²⁰ Ne(d,p) ²¹ Ne	16.4	[108]		0.031	0.035	5	
²¹Ne	²¹ Ne(p,d) ²⁰ Ne	20	[109]		0.03	0.03	8	BS
²²Ne	²¹ Ne(d,p) ²² Ne	10.2	[109]					BD
²²Ne	²² Ne(p,d) ²¹ Ne	18.2	[110]		0.26		4	
²²Ne	²² Ne(p,d) ²¹ Ne	20	[111]		0.20	0.24	2	
²³Ne	²² Ne(d,p) ²³ Ne	12.1	[108]		0.24		6	
²³Ne	²² Ne(d,p) ²³ Ne	12.1	[110]		0.24	0.24	6	
²⁴Na	²³ Na(d,p) ²⁴ Na	7.83	[112]		0.59	0.59	2	
²⁴Mg	²⁴ Mg(p,d) ²³ Mg	27.3	[113]		0.39		4	
²⁴Mg	²⁴ Mg(p,d) ²³ Mg	33.6	[114]	0.34*			2	BD
²⁴Mg	²⁴ Mg(p,d) ²³ Mg	49.2	[115]		0.44	0.41	3	
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	5	[116]	0.75			6	
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	6	[116]	0.50			3	
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	10	[117]		0.28		3	
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	12	[118]		0.33		3	BS
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	14	[119]		0.27		3	
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	15	[119]	0.28*		0.29	1	BS
²⁵Mg	²⁴ Mg(d,p) ²⁵ Mg	56	[67]	0.49*			6	NP
²⁶Mg	²⁵ Mg(d,p) ²⁶ Mg	8	[120]	2.97			7	
²⁶Mg	²⁵ Mg(d,p) ²⁶ Mg	12	[121]		2.01	2.01	8	
²⁶Mg	²⁵ Mg(d,p) ²⁶ Mg	13	[122]	2.62*			7	BD
²⁶Mg	²⁶ Mg(p,d) ²⁵ Mg	20	[123]		2.01		2	
²⁶Mg	²⁶ Mg(p,d) ²⁵ Mg	23.95	[124]		3.06		4	
²⁶Mg	²⁶ Mg(p,d) ²⁵ Mg	35	[125]		2.97	2.80	3	BS
²⁷Mg	²⁶ Mg(d,p) ²⁷ Mg	5.07	[126]	1.03			1	
²⁷Mg	²⁶ Mg(d,p) ²⁷ Mg	12	[127]		0.45	0.45	2	
²⁷Al	²⁷ Al(p,d) ²⁶ Al	20	[128]		1.51		3	
²⁷Al	²⁷ Al(p,d) ²⁶ Al	35	[129]		1.32	1.40	4	
²⁸Al	²⁷ Al(d,p) ²⁸ Al	6	[130]	0.43			3	
²⁸Al	²⁷ Al(d,p) ²⁸ Al	12	[131]		0.60		3	
²⁸Al	²⁷ Al(d,p) ²⁸ Al	23	[132]		0.82	0.66	1	
²⁸Si	²⁸ Si(p,d) ²⁷ Si	27.6	[133]	15.44*			6	
²⁸Si	²⁸ Si(p,d) ²⁷ Si	33.6	[114]		4.40	4.40	4	

²⁹ Si	²⁸ Si(d,p) ²⁹ Si	5	[134]	0.73			1	
²⁹ Si	²⁸ Si(d,p) ²⁹ Si	5.8	[135]	0.41			2	
²⁹ Si	²⁸ Si(d,p) ²⁹ Si	9	[90]	0.39			1	
²⁹ Si	²⁸ Si(d,p) ²⁹ Si	10	[136]		0.56		2	
²⁹ Si	²⁸ Si(d,p) ²⁹ Si	17.85	[137]		0.36		2	
²⁹ Si	²⁸ Si(d,p) ²⁹ Si	18	[138]		0.24	0.42	1	
²⁹ Si	²⁹ Si(p,d) ²⁸ Si	27.3	[139]	1.32*			2	NP
³⁰ Si	²⁹ Si(d,p) ³⁰ Si	10	[140]		0.93		1	BS
³⁰ Si	²⁹ Si(d,p) ³⁰ Si	12.3	[141]					NP
³⁰ Si	²⁹ Si(d,p) ³⁰ Si	16	[142]		0.64	0.79	1	
³⁰ Si	³⁰ Si(p,d) ²⁹ Si	27	[143]		0.87		3	
³⁰ Si	³⁰ Si(p,d) ²⁹ Si	27.3	[139]	0.87*		0.87	1	NP
³¹ Si	³⁰ Si(d,p) ³¹ Si	7	[144]	0.58			5	
³¹ Si	³⁰ Si(d,p) ³¹ Si	10	[144]		0.55		4	
³¹ Si	³⁰ Si(d,p) ³¹ Si	10	[145]		0.55		2	
³¹ Si	³⁰ Si(d,p) ³¹ Si	12.3	[141]		0.71		2	
³¹ Si	³⁰ Si(d,p) ³¹ Si	12.3	[146]		0.47		6	
³¹ Si	³⁰ Si(d,p) ³¹ Si	17	[141]		0.54	0.54	2	
³² P	³¹ P(d,p) ³² P	10	[147]		0.68		2	
³² P	³¹ P(d,p) ³² P	20	[148]		0.48	0.58	2	
³² S	³² S(p,d) ³¹ S	24.5	[149]	3.4*			1	NP
³² S	³² S(p,d) ³¹ S	33.6	[114]		1.51	1.51	2	NP
³³ S	³² S(d,p) ³³ S	18	[138]		0.70	0.70	4	
³⁴ S	³³ S(d,p) ³⁴ S	12	[150]		1.85		4	
³⁴ S	³³ S(d,p) ³⁴ S	12	[151]		1.23	1.58	3	
³⁴ S	³⁴ S(p,d) ³³ S	24.5	[149]		1.08	1.08	3	
³⁴ S	³⁴ S(p,d) ³³ S	35	[152]	3.30*			8	BS
³⁵ S	³⁴ S(d,p) ³⁵ S	10	[153]		0.30	0.30	5	
³⁵ S	³⁴ S(d,p) ³⁵ S	11.8	[154]		0.30		2	BS
³⁷ S	³⁶ S(d,p) ³⁷ S	12.3	[155]		0.88		4	
³⁷ S	³⁶ S(d,p) ³⁷ S	25	[156]		0.89	0.88	1	
³⁵ Cl	³⁵ Cl(p,d) ³⁴ Cl	40	[157]		0.35	0.35	4	
³⁶ Cl	³⁵ Cl(d,p) ³⁶ Cl	7	[158]	0.43			3	
³⁶ Cl	³⁵ Cl(d,p) ³⁶ Cl	12.3	[159]		0.68	0.68	1	
³⁷ Cl	³⁷ Cl(p,d) ³⁶ Cl	19	[128]	30.1*				AU
³⁷ Cl	³⁷ Cl(p,d) ³⁶ Cl	35	[160]		1.58		2	
³⁷ Cl	³⁷ Cl(p,d) ³⁶ Cl	40	[157]		0.66	0.97	4	
³⁸ Cl	³⁷ Cl(d,p) ³⁸ Cl	7.5	[161]	1.06*			3	BS
³⁸ Cl	³⁷ Cl(d,p) ³⁸ Cl	12	[162]		1.81	1.81	3	

³⁶ Ar	³⁶ Ar(p,d) ³⁵ Ar	27.5	[163]		4.32		5	
³⁶ Ar	³⁶ Ar(p,d) ³⁵ Ar	33.6	[114]		2.53	3.34	6	
³⁷ Ar	³⁶ Ar(d,p) ³⁷ Ar	9.162	[164]	0.29			6	
³⁷ Ar	³⁶ Ar(d,p) ³⁷ Ar	10.02	[165]		0.34		5	
³⁷ Ar	³⁶ ₃₇	18	[138]		0.37	0.36	5	
³⁸ Ar	³⁸ Ar(p,d) ³⁷ Ar	26	[166]		2.47	2.47	6	
³⁹ Ar	³⁸ Ar(d,p) ³⁹ Ar	10.064			0.87		3	
³⁹ Ar	³⁸ Ar(d,p) ³⁹ Ar	11.6	[168]		0.77		4	
⁴⁰ Ar	⁴⁰ Ar(p,d) ³⁹ Ar	27.5	[163]		1.08	1.08	5	
⁴⁰ Ar	⁴⁰ Ar(p,d) ³⁹ Ar	35	[169]	2.25*			4	BS
⁴¹ Ar	⁴⁰ Ar(d,p) ⁴¹ Ar	11.6	[168]		0.57		2	BS
⁴¹ Ar		14.83	[170]		0.54	0.55	3	
³⁹ K	³⁹ K(p,d) ³⁸ K	35	[171]		2.12		4	BS
⁴⁰ K	³⁹ K(d,p) ⁴⁰ K	12	[162]		1.71	1.71	5	
⁴¹ K	⁴¹ K(p,d) ⁴⁰ K	15	[172]		0.91	0.91	3	
⁴² K	⁴¹ K(d,p) ⁴² K	10	[173]		0.91			
⁴² K	⁴¹ K(d,p) ⁴² K	12	[174]		0.71	0.81	1	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	27.3	[175]		3.49		3	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	30	[176]		4.43		4	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	33.6	[114]		5.50		3	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	40	[177]		3.86		3	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	65	[178]		4.40	4.35	5	
⁴⁰ Ca	⁴⁰ Ca(p,d) ³⁹ Ca	65	[54]	5.00*			3	NP
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	4.13	[179]	1.36			1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	4.69	[179]	1.20			1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	5	[180]	1.62			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	5	[181]	1.40			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	6	[180]	1.33			1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	6	[182]	1.24			2	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	7	[183]	1.25			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	7	[184]	1.00			1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	7.2	[183]	1.27			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	8	[184]	1.17			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	9	[181]	1.05			5	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	9	[184]	1.19			3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	10	[185]		0.96		3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	10	[186]		0.96		1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	10	[184]	1.07*				BD
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[187]		1.00		3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[188]					NP
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[181]		0.99		4	

⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[189]		1.09		4	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[184]	1.43*			3	BD
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[190]		0.98		3	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11	[191]		1.02		2	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	11.8	[32]		0.99		1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	12	[188]		0.99		2	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	12	[192]		1.07		2	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	12	[184]	1.04*			3	BS
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	12.8	[193]		1.11		1	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	14.3	[194]		1.00		5	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	20	[195]		1.04	1.01	2	
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	56	[67]	0.76*			4	BS
⁴¹ Ca	⁴⁰ Ca(d,p) ⁴¹ Ca	56	[196]	1.07*			3	BS
⁴² Ca	⁴¹ Ca(d,p) ⁴² Ca	11	[189]		1.92		2	
⁴² Ca	⁴¹ Ca(d,p) ⁴² Ca	12	[192]		1.78		5	
⁴² Ca	⁴¹ Ca(d,p) ⁴² Ca	12	[197]		1.81	1.82	3	
⁴² Ca	⁴² Ca(p,d) ⁴¹ Ca	26.5	[198]		2.18		4	
⁴² Ca	⁴² Ca(p,d) ⁴¹ Ca	40	[177]		2.00	2.12	2	
⁴³ Ca	⁴² Ca(d,p) ⁴³ Ca	7	[183]	0.85			3	
⁴³ Ca	⁴² Ca(d,p) ⁴³ Ca	7.2	[183]	0.93			3	
⁴³ Ca	⁴² Ca(d,p) ⁴³ Ca	7.2	[199]	0.84			3	
⁴³ Ca	⁴² Ca(d,p) ⁴³ Ca	10	[185]		0.66		2	
⁴³ Ca	⁴² Ca(d,p) ⁴³ Ca	10	[186]		0.59	0.63	2	
⁴³ Ca	⁴³ Ca(p,d) ⁴² Ca	40	[200]		0.63	0.63	3	
⁴⁴ Ca	⁴³ Ca(d,p) ⁴⁴ Ca	8.5	[201]	5.14		5.14	3	
⁴⁴ Ca	⁴⁴ Ca(p,d) ⁴³ Ca	17.5	[202]		2.84		2	
⁴⁴ Ca	⁴⁴ Ca(p,d) ⁴³ Ca	26.5	[198]		5.34		4	
⁴⁴ Ca	⁴⁴ Ca(p,d) ⁴³ Ca	40	[177]		3.23	3.93	5	
⁴⁵ Ca	⁴⁴ Ca(d,p) ⁴⁵ Ca	7	[183]	0.55			3	
⁴⁵ Ca	⁴⁴ Ca(d,p) ⁴⁵ Ca	7	[203]	0.62			2	
⁴⁵ Ca	⁴⁴ Ca(d,p) ⁴⁵ Ca	7.2	[183]	0.54			2	
⁴⁵ Ca	⁴⁴ Ca(d,p) ⁴⁵ Ca	10	[185]		0.37		2	
⁴⁵ Ca	⁴⁴ Ca(d,p) ⁴⁵ Ca	10	[186]		0.37	0.37	2	
⁴⁷ Ca	⁴⁶ Ca(d,p) ⁴⁷ Ca	7	[183]	0.35			3	
⁴⁷ Ca	⁴⁶ Ca(d,p) ⁴⁷ Ca	7.2	[183]	0.29			3	
⁴⁷ Ca	⁴⁶ Ca(d,p) ⁴⁷ Ca	10	[185]		0.26		2	
⁴⁷ Ca	⁴⁶ Ca(d,p) ⁴⁷ Ca	10	[204]		0.26	0.26	4	
⁴⁸ Ca	⁴⁸ Ca(p,d) ⁴⁷ Ca	17.5	[202]		8.82		5	
⁴⁸ Ca	⁴⁸ Ca(p,d) ⁴⁷ Ca	18	[205]		5.51		4	
⁴⁸ Ca	⁴⁸ Ca(p,d) ⁴⁷ Ca	40	[177]		7.35	7.35	3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	4.5	[206]	0.77			4	

⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	5	[206]	0.76			3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	5.5	[206]	0.73			3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	7	[183]	0.81			3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	7	[206]	0.89			4	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	7	[207]	1.5			4	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	7.2	[183]	0.87			3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	10	[185]	0.79*			1	NP
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	10	[186]		0.63		2	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	11.9	[208]	0.61*			2	NP
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	13	[209]		0.77		3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	16	[209]		0.68		3	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	19.3	[209]		0.64	0.69	1	
⁴⁹ Ca	⁴⁸ Ca(d,p) ⁴⁹ Ca	56	[210]	0.66*			3	BS
⁴⁵ Sc	⁴⁵ Sc(p,d) ⁴⁴ Sc	17.5	[211]		0.30	0.30	3	BS
⁴⁶ Sc	⁴⁵ Sc(d,p) ⁴⁶ Sc	7	[212]	0.39			2	
⁴⁶ Sc	⁴⁵ Sc(d,p) ⁴⁶ Sc	12	[213]		0.51	0.51	2	
⁴⁶ Ti	⁴⁶ Ti(p,d) ⁴⁵ Ti	17.5	[214]		2.6		3	
⁴⁶ Ti	⁴⁶ Ti(p,d) ⁴⁵ Ti	26	[215]		2.29	2.423	4	
⁴⁶ Ti	⁴⁶ Ti(p,d) ⁴⁵ Ti	34.78	[216]	1.28*			3	
⁴⁷ Ti	⁴⁶ Ti(d,p) ⁴⁷ Ti	7	[217]		0.03		4	BS
⁴⁷ Ti		7	[218]		0.02	0.025	4	
⁴⁷ Ti	⁴⁶ Ti(d,p) ⁴⁷ Ti	10	[219]	0.01*			4	BD
⁴⁷ Ti	⁴⁶ Ti(d,p) ⁴⁷ Ti	10	[218]	0.01*			4	BD
⁴⁸ Ti	⁴⁷ Ti(d,p) ⁴⁸ Ti	13.6	[220]		0.14	0.14	1	BS
⁴⁸ Ti	⁴⁸ Ti(p,d) ⁴⁷ Ti	24.8	[216]	0.10*			4	BD
⁴⁸ Ti	⁴⁸ Ti(p,d) ⁴⁷ Ti	29.82	[216]	0.12*			3	BD
⁴⁸ Ti	⁴⁸ Ti(p,d) ⁴⁷ Ti	35.15	[216]		0.11		3	
⁴⁸ Ti	⁴⁸ Ti(p,d) ⁴⁷ Ti	39.97	[216]		0.11		3	
⁴⁸ Ti	⁴⁸ Ti(p,d) ⁴⁷ Ti	45.05	[216]			0.11	3	
⁴⁹ Ti	⁴⁸ Ti(d,p) ⁴⁹ Ti	6	[221]	0.3			4	
⁴⁹ Ti	⁴⁸ Ti(d,p) ⁴⁹ Ti	21.4	[222]		0.23	0.23	3	
⁴⁹ Ti	⁴⁹ Ti(p,d) ⁴⁸ Ti	17.5	[214]		0.25		4	
⁴⁹ Ti	⁴⁹ Ti(p,d) ⁴⁸ Ti	20.9	[149]		0.27	0.26	4	
⁵⁰ Ti	⁴⁹ Ti(d,p) ⁵⁰ Ti	13.6	[220]		6.23		4	
⁵⁰ Ti	⁴⁹ Ti(d,p) ⁵⁰ Ti	21.4	[222]		8	7.115	4	
⁵⁰ Ti	⁵⁰ Ti(p,d) ⁴⁹ Ti	17.5	[207]		5.98		4	
⁵⁰ Ti	⁵⁰ Ti(p,d) ⁴⁹ Ti	45.05	[216]		4.86	5.50	3	
⁵¹ Ti	⁵⁰ Ti(d,p) ⁵¹ Ti	6	[223]	0.53*			3	
⁵¹ Ti	⁵⁰ Ti(d,p) ⁵¹ Ti	21.4	[222]		1.25	1.25	5	
⁵¹ V	⁵⁰ V(d,p) ⁵¹ V	7.5	[224]		1.58	1.58	3	

⁵¹ V	⁵¹ V(p,d) ⁵⁰ V	18.5	[225]		1.33		3	BS
⁵¹ V	⁵¹ V(p,d) ⁵⁰ V	51.9	[226]		0.75	1.098	2	BS
⁵⁰ Cr	⁵⁰ Cr(p,d) ⁴⁹ Cr	17.5	[227]	0.11*			5	BS
⁵⁰ Cr	⁵⁰ Cr(p,d) ⁴⁹ Cr	55	[228]		0.11	0.11		BS
⁵¹ Cr	⁵⁰ Cr(d,p) ⁵¹ Cr	6.6	[229]	0.62			2	
⁵¹ Cr	⁵⁰ Cr(d,p) ⁵¹ Cr	7.5	[230]	0.67			2	
⁵¹ Cr	⁵⁰ Cr(d,p) ⁵¹ Cr	10	[231]	2.83*			3	AU
⁵¹ Cr	⁵⁰ Cr(d,p) ⁵¹ Cr	12	[232]		0.30	0.30	3	
⁵² Cr	⁵² Cr(p,d) ⁵¹ Cr	17.5	[227]		6.55		6	
⁵² Cr	⁵² Cr(p,d) ⁵¹ Cr	18.5	[225]		5.87	6.24	5	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	5.41	[233]	0.67			3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	5.72	[233]	0.57			4	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	6	[234]	0.46			4	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	6.02	[233]	0.53			2	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	6.33	[233]	0.49			3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	7.5	[235]	0.54			3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	9.14	[236]	0.36			3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	10	[219]		0.43		2	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	10	[237]		0.42		2	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	10	[238]		0.39		1	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	10	[239]		0.33		1	BD
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	10.15	[236]		0.37		3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	11.18	[236]		0.36		3	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	12	[240]		0.42		4	
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	20	[257]		0.35			
⁵³ Cr	⁵² Cr(d,p) ⁵³ Cr	22	[241]		0.36	0.39	2	
⁵³ Cr		16.6	[149]		0.37	0.37	2	
⁵⁴ Cr	⁵³ Cr(d,p) ⁵⁴ Cr	12	[258]		0.71	0.71	2	
⁵⁵ Cr	⁵⁴ Cr(d,p) ⁵⁵ Cr	8	[242]		0.63		2	
⁵⁵ Cr	⁵⁴ Cr(d,p) ⁵⁵ Cr	10	[243]	0.42*			2	NP
⁵⁵ Cr	⁵⁴ Cr(d,p) ⁵⁵ Cr	10		0.87*		0.63	3	BD

Table II List of nuclei with spectroscopic factors obtained from both (p,d) and (d,p) reactions. N_{pd} and N_{dp} denote the number of (p,d) and (d,p) independent measurements included in the analysis.

B	B(p,d)A	N_{pd}	A(d,p)B	N_{dp}
^{11}Be	0.57	1	0.49	2
^{11}B	1.29	1	1.55	3
^{13}C	0.81	4	0.73	12
^{14}C	1.50	3	1.82	2
^{15}N	1.65	2	1.39	4
^{17}O	0.81	3	0.99	10
^{18}O	1.60	2	1.80	1
^{21}Ne	0.03	1	0.04	2
^{26}Mg	2.80	3	2.01	1
^{30}Si	0.87	1	0.79	2
^{42}Ca	2.12	2	1.82	3
^{43}Ca	0.63	1	0.63	2
^{44}Ca	3.93	3	5.14	1
^{48}Ti	0.11	3	0.14	1
^{49}Ti	0.26	2	0.23	1
^{50}Ti	5.50	2	7.12	2
^{51}V	1.10	2	1.58	1
^{53}Cr	0.37	1	0.39	8

Table III: List of isotopes with the extracted spectroscopic factors, SF(JS) and other information such as the mass number (A), charge number (Z) and neutron number (N) for the nuclei. j^π , T and S_n are the spin and parity, isospin and neutron separation energy of the nuclei. For completeness, we list the root mean square radii of the neutron wavefunctions. Endt compiled values are also listed when available. The model space and interactions used in Oxbash [251] are listed together with the predicted SF values labeled as LB-SM.

B	A	Z	N	j^π	T	S_n	rms	Endt	SF (JS)	LB-SM	Model Space	Interaction
⁶ Li	6	3	3	1/2 ⁻	0	5.66	2.91		1.12 ± 0.32	0.68	PPN	CKPPN
⁷ Li	7	3	4	1/2	1/2	7.25	2.81		1.85 ± 0.37	0.63	PPN	CKPPN
⁸ Li	8	3	5	1/2 ⁻	1	2.03	3.66		0.62 ± 0.18	1.09	PPN	CKPPN
⁹ Li	9	3	6	1/2 ⁻	3/2	4.06			0.98 ± 0.28	0.81		CKPPN
⁹ Be	9	4	5	3/2 ⁻	1/2	1.67	3.86		0.45 ± 0.03	0.57	PPN	CKPPN
¹⁰ Be	10	4	6	3/2 ⁻	1	6.81	2.96		1.58 ± 0.15	2.36	PPN	CKPPN
¹¹ Be	11	4	7	1/2 ⁺	3/2	0.50	7.11		0.51 ± 0.06	0.74	SPSDPF	WBP
¹⁰ B	10	5	5	3/2 ⁻	0	8.44	2.85		0.50 ± 0.07	0.60	PPN	CKPPN
¹¹ B	11	5	6	3/2 ⁻	1/2	11.45	2.73		1.48 ± 0.19	1.09	PPN	CKPPN
¹² B	12	5	7		1	3.37	3.46		0.45 ± 0.06	0.83	PPN	CKPPN
¹² C	12	6	6	3/2 ⁻	0	18.72	2.53		3.12 ± 0.36	2.85	PPN	CKPPN
¹³ C	13	6	7	1/2 ⁻	1/2	4.95	3.26		0.75 ± 0.10	0.61	PPN	CKPPN
¹⁴ C	14	6	8	1/2 ⁻	1	8.18	3.00		1.63 ± 0.33	1.73	PPN	CKPPN
¹⁵ C	15	6	9	1/2 ⁺	3/2	1.22	5.51		1.12 ± 0.32	0.98	SPSDPF	WBP
¹⁴ N	14	7	7	1/2 ⁻	0	10.55	2.87		0.77 ± 0.12	0.69	PPN	CKPPN
¹⁵ N	15	7	8	1/2 ⁻	1/2	10.83	2.89		1.48 ± 0.24	1.46	PPN	CKPPN
¹⁶ N	16	7	9	3/2 ⁺	1	2.49	4.26		0.42 ± 0.12	0.96	SPSDPF	WBP
¹⁶ O	16	8	8	1/2 ⁻	0	15.66	2.74		2.46 ± 0.26	2.00	PPN	CKPPN
¹⁷ O	17	8	9	5/2 ⁺	1/2	4.14	3.48		0.94 ± 0.13	1.00	SD	USD
¹⁸ O	18	8	10	5/2 ⁺	1	8.04	3.24		1.66 ± 0.19	1.58	SD	USD
¹⁹ O	19	8	11	5/2 ⁺	3/2	3.95	3.57		0.43 ± 0.06	0.69	SD	USD
¹⁹ F	19	9	10	1/2 ⁺	1/2	10.43	2.66		1.60 ± 0.23	0.56	SD	USD
²⁰ F	20	9	11	3/2 ⁺	1	6.60	3.39		~0.01	0.02	SD	USD
²¹ Ne	21	10	11	3/2 ⁺	1/2	6.76	3.41	0.01	0.03 ± 0.01	0.03	SD	USD
²² Ne	22	10	12	3/2 ⁺	1	10.36	3.27	0.19	0.24 ± 0.03	0.13	SD	USD
²³ Ne	23	10	13	5/2 ⁺	3/2	5.20	3.58	0.24	0.24 ± 0.03	0.32	SD	USD
²⁴ Na	24	11	13	1/2 ⁺	1	8.87	3.49	0.30	0.59 ± 0.17	0.39	SD	USD
²⁴ Mg	24	12	12	3/2 ⁺	0	16.53	3.13		0.41 ± 0.06	0.41	SD	USD
²⁵ Mg	25	12	13	5/2 ⁺	1/2	7.33	3.50	0.37	0.29 ± 0.03	0.34	SD	USD
²⁶ Mg	26	12	14	5/2 ⁺	1	11.09	3.35	1.80	2.43 ± 0.50	2.51	SD	USD
²⁷ Mg	27	12	15	1/2 ⁺	3/2	6.44	3.90	0.58	0.45 ± 0.13	0.46	SD	USD
²⁷ Al	27	13	14	5/2 ⁺	1/2	13.06	3.31	1.10	1.40 ± 0.20	1.10	SD	USD
²⁸ Al	28	13	15	1/2 ⁺	1	7.73	3.78	0.50	0.66 ± 0.10	0.60	SD	USD
²⁸ Si	28	14	14	5/2 ⁺	0	17.18	3.22		4.40 ± 1.24	3.62	SD	USD
²⁹ Si	29	14	15	1/2 ⁺	1/2	8.47	3.73	0.55	0.42 ± 0.13	0.45	SD	USD

³⁰ Si	30	14	16	1/2 ⁺	1	10.61	2.87	0.89	0.84 ± 0.10	0.82	SD	USD
³¹ Si	31	14	17	3/2 ⁺	3/2	6.59	3.70	0.75	0.54 ± 0.07	0.58	SD	USD
³² P	32	15	17	1/2 ⁺	1	7.94	3.64	0.80	0.58 ± 0.10	0.60	SD	USD
³² S	32	16	16	1/2 ⁺	0	15.04	3.40		1.51 ± 0.43	0.96	SD	USD
³³ S	33	16	17	3/2 ⁺	1/2	8.64	3.63	0.70	0.70 ± 0.20	0.61	SD	USD
³⁴ S	34	16	18	3/2 ⁺	1	11.42	3.53	1.90	1.43 ± 0.35	1.83	SD	USD
³⁵ S	35	16	19	3/2 ⁺	3/2	6.99	3.77	0.38	0.30 ± 0.09	0.36	SD	USD
³⁷ S	37	16	21	7/2 ⁻	5/2	4.30	4.02		0.88 ± 0.12	0.92	SDPF	SDPFNOW
³⁵ Cl	35	17	18	3/2 ⁺	1/2	12.64	3.51		0.35 ± 0.10	0.32	SD	USD
³⁶ Cl	36	17	19	1/2 ⁺	1	8.58	3.70	1.20	0.68 ± 0.19	0.77	SD	USD
³⁷ Cl	37	17	20	1/2 ⁺	3/2	10.31	3.64	0.95	0.97 ± 0.43	1.15	SD	USD
³⁸ Cl	38	17	21	1/2 ⁻	2	6.11	3.94	0.78	1.81 ± 0.51	0.95	SDPF	SDPFNOW
³⁶ Ar	36	18	18	3/2 ⁺	0	15.26	3.45		3.34 ± 0.89	2.06	SD	USD
³⁷ Ar	37	18	19	3/2 ⁺	1/2	8.79	3.71	0.49	0.36 ± 0.05	0.36	SD	USD
³⁸ Ar	38	18	20	3/2 ⁺	1	11.84	3.60	2.50	2.47 ± 0.70	3.04	SD	USD
³⁹ Ar	39	18	21	7/2 ⁻	3/2	6.60	3.94	0.64	0.81 ± 0.11	0.83	SDPF	SDPFNOW
⁴⁰ Ar	40	18	22	7/2 ⁻	2	9.87	3.83	1.20	1.08 ± 0.31	1.91	SDPF	SDPFNOW
⁴¹ Ar	41	18	23	7/2 ⁻	5/2	6.10	4.01	0.47	0.55 ± 0.08	0.65	SDPF	SDPFNOW
³⁹ K	39	19	20	3/2 ⁺	1/2	13.08	3.58	2.00	2.12 ± 0.60	1.72	SD	USD
⁴⁰ K	40	19	21	5/2 ⁻	1	7.80	3.90	0.94	1.71 ± 0.48	0.98	SDPF	SDPFNOW
⁴¹ K	41	19	22	5/2 ⁻	3/2	10.10	3.84	0.56	0.91 ± 0.26	1.06	SDPF	SDPFNOW
⁴² K	42	19	23	1/2 ⁻	2	7.53	3.96	0.34	0.81 ± 0.11	0.88	SDPF	SDPFNOW
⁴⁰ Ca	40	20	20	3/2 ⁺	0	15.64	3.81		4.35 ± 0.62	4.00	SD	USD
⁴¹ Ca	41	20	21	7/2 ⁻	1/2	8.36	3.90	0.85	1.01 ± 0.06	1.00	FPPN	FPBPPN
⁴² Ca	42	20	22	7/2 ⁻	1	11.48	3.82	1.60	1.93 ± 0.17	1.81	FPPN	FPBPPN
⁴³ Ca	43	20	23	7/2 ⁻	3/2	7.93	3.97	0.58	0.63 ± 0.07	0.75	FPPN	FPBPPN
⁴⁴ Ca	44	20	24	7/2 ⁻	2	11.13	3.87	3.10	3.93 ± 1.08	3.64	FPPN	FPBPPN
⁴⁵ Ca	45	20	25	7/2 ⁻	5/2	7.41	4.03		0.37 ± 0.05	0.50	FPPN	FPBPPN
⁴⁷ Ca	47	20	27	7/2 ⁻	7/2	7.28	4.08		0.26 ± 0.04	0.26	FPPN	FPBPPN
⁴⁸ Ca	48	20	28	7/2 ⁻	4	9.95	3.99		7.35 ± 1.42	7.38	FPPN	FPBPPN
⁴⁹ Ca	49	20	29	3/2 ⁻	9/2	5.15	4.59		0.69 ± 0.07	0.92	FPPN	FPBPPN
⁴⁵ Sc	45	21	24	3/2 ⁻	3/2	11.32	3.89	0.34	0.30 ± 0.08	0.35	FPPN	FPBPPN
⁴⁶ Sc	46	21	25	1/2 ⁻	2	8.76	4.00		0.51 ± 0.14	0.37	FPPN	FPBPPN
⁴⁶ Ti	46	22	24	7/2 ⁻	1	13.19	3.85		2.42 ± 0.34	2.58	FPPN	FPBPPN
⁴⁷ Ti	47	22	25	5/2 ⁻	3/2	8.88	4.01		0.03 ± 0.01			
⁴⁸ Ti	48	22	26	5/2 ⁻	2	11.63	3.94		0.11 ± 0.01			
⁴⁹ Ti	49	22	27	7/2 ⁻	5/2	8.14	4.08		0.25 ± 0.03			
⁵⁰ Ti	50	22	28	7/2 ⁻	3	10.94	4.00		6.36 ± 1.10			
⁵¹ Ti	51	22	29	3/2 ⁻	7/2	6.37	4.46		1.25 ± 0.35			
⁵¹ V	51	23	28	5/2 ⁻	5/2	11.05	4.01		1.28 ± 0.32			
⁵⁰ Cr	50	24	26	5/2 ⁻	1	13.00	3.94		0.11 ± 0.02			
⁵¹ Cr	51	24	27	7/2 ⁻	3/2	9.26	4.08		0.30 ± 0.08			
⁵² Cr	52	24	28	7/2 ⁻	2	12.04	4.00		6.24 ± 0.88			
⁵³ Cr	53	24	29	3/2 ⁻	5/2	7.94	4.34		0.39 ± 0.03			
⁵⁴ Cr	54	24	30	3/2 ⁻	3	9.72	4.22		0.71 ± 0.20			
⁵⁵ Cr	55	24	31	3/2 ⁻	7/2	6.24	4.53		0.63 ± 0.13			

Figure 1: (Color online) Comparison of tabulated data (closed points) [23] and digitized data (open points) [84] from the same measurement of the angular distributions of the protons obtained in the $^{14}\text{N}(d,p)^{15}\text{N}$ reaction at incident deuteron energy of 12 MeV. The curve is the predicted angular distributions from the code TWOFNR as described in the text, multiplied by 1.12 which is the spectroscopic factor.

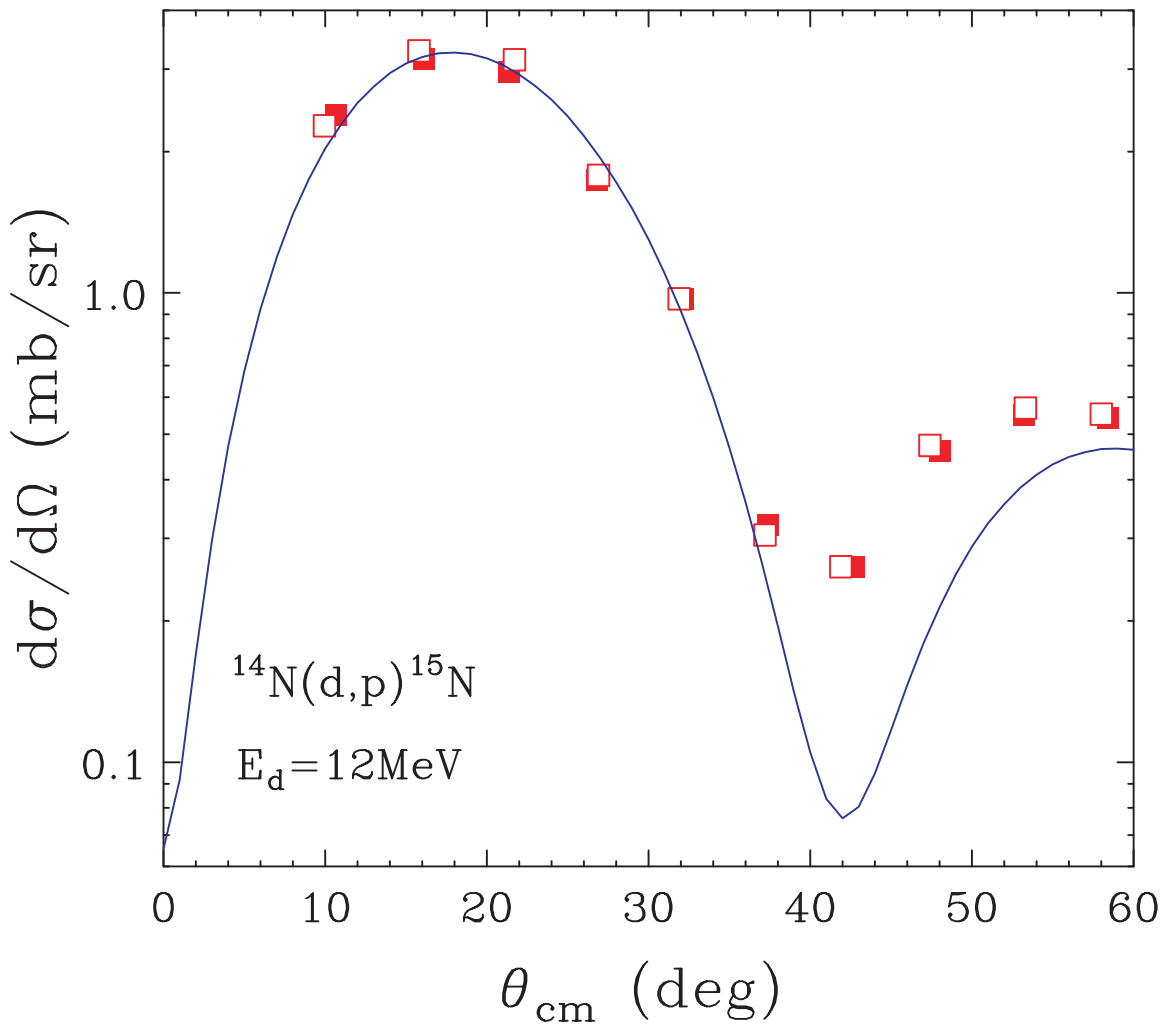


Figure 2: (Color online) The angular distributions of the deuteron obtained in the $^{44}\text{Ca}(p,d)^{43}\text{Ca}$ reaction at incident proton energy of 40 MeV [177]. The curve is the predicted angular distributions from the code TWOFNR as described in the text, multiplied by the spectroscopic factor.

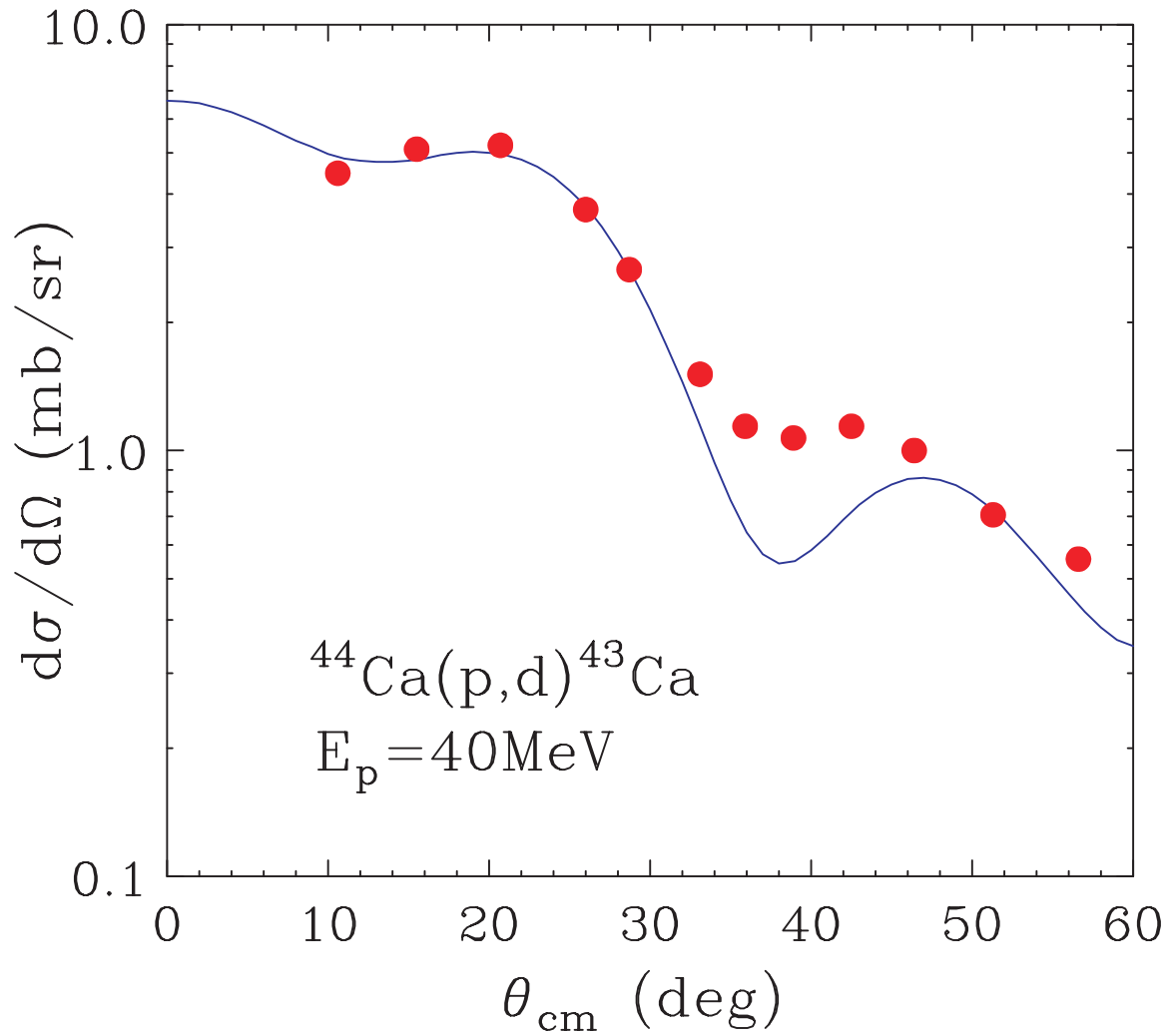


Figure 3: (Color online) Comparisons of the angular distributions of the proton measured in the $^{11}\text{B}(d,p)^{12}\text{B}$ reactions in three different experiments. Open circles, closed circles, open and closed diamonds represent data from refs. [23], [47] and [48] respectively. The curve is the predicted angular distributions from the code TWOFNR multiplied by the spectroscopic factor.

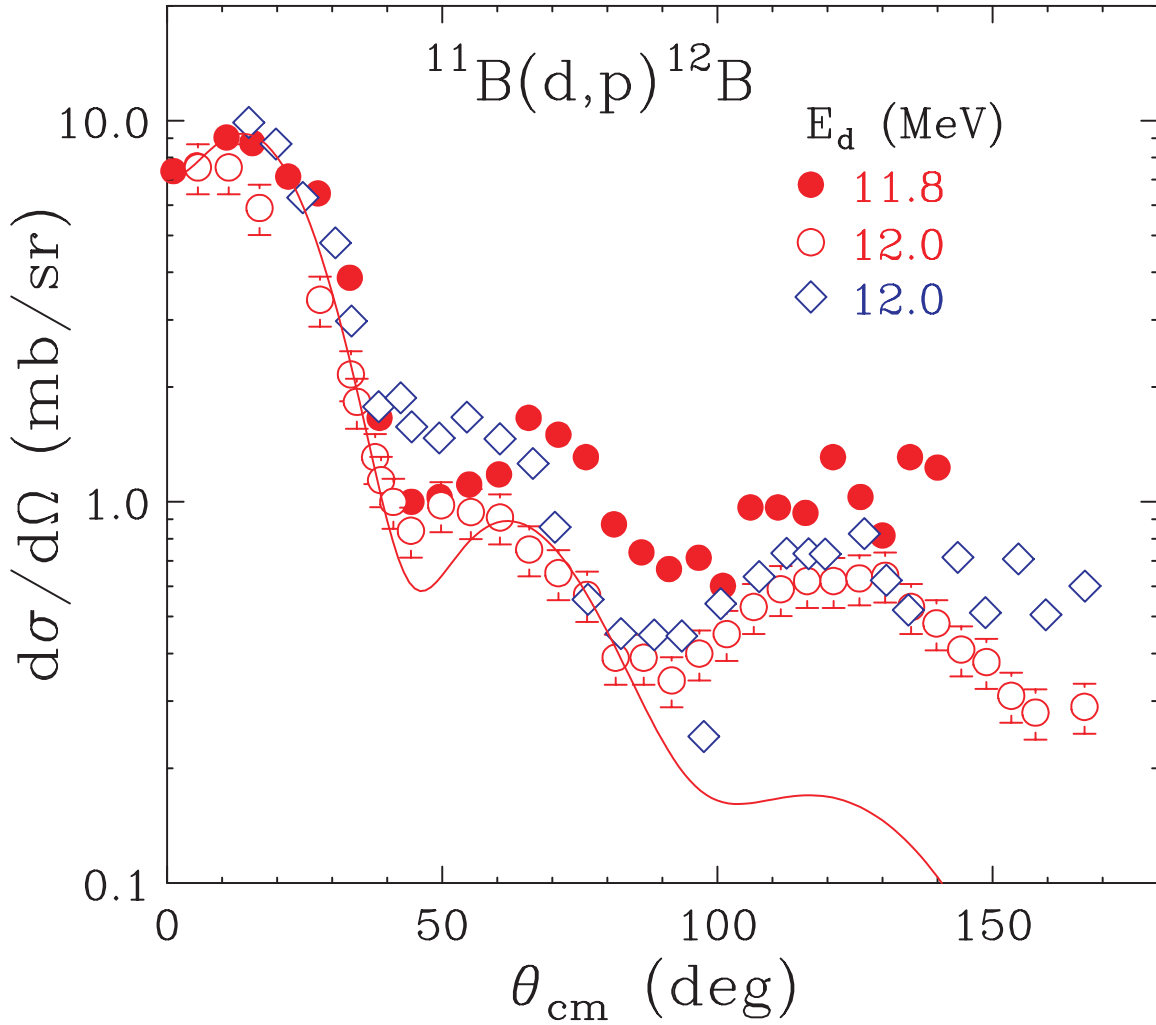


Figure 4: (Color online) Comparisons of the angular distributions of the proton measured in the $^{12}\text{C}(d,p)^{13}\text{C}$ reactions in four different experiments. Open circles and closed circles, open and closed diamonds represent data from refs. [23], [47], [61] and [32] respectively. The curve is the predicted angular distributions from the code TWOFNR multiplied by the spectroscopic factor.

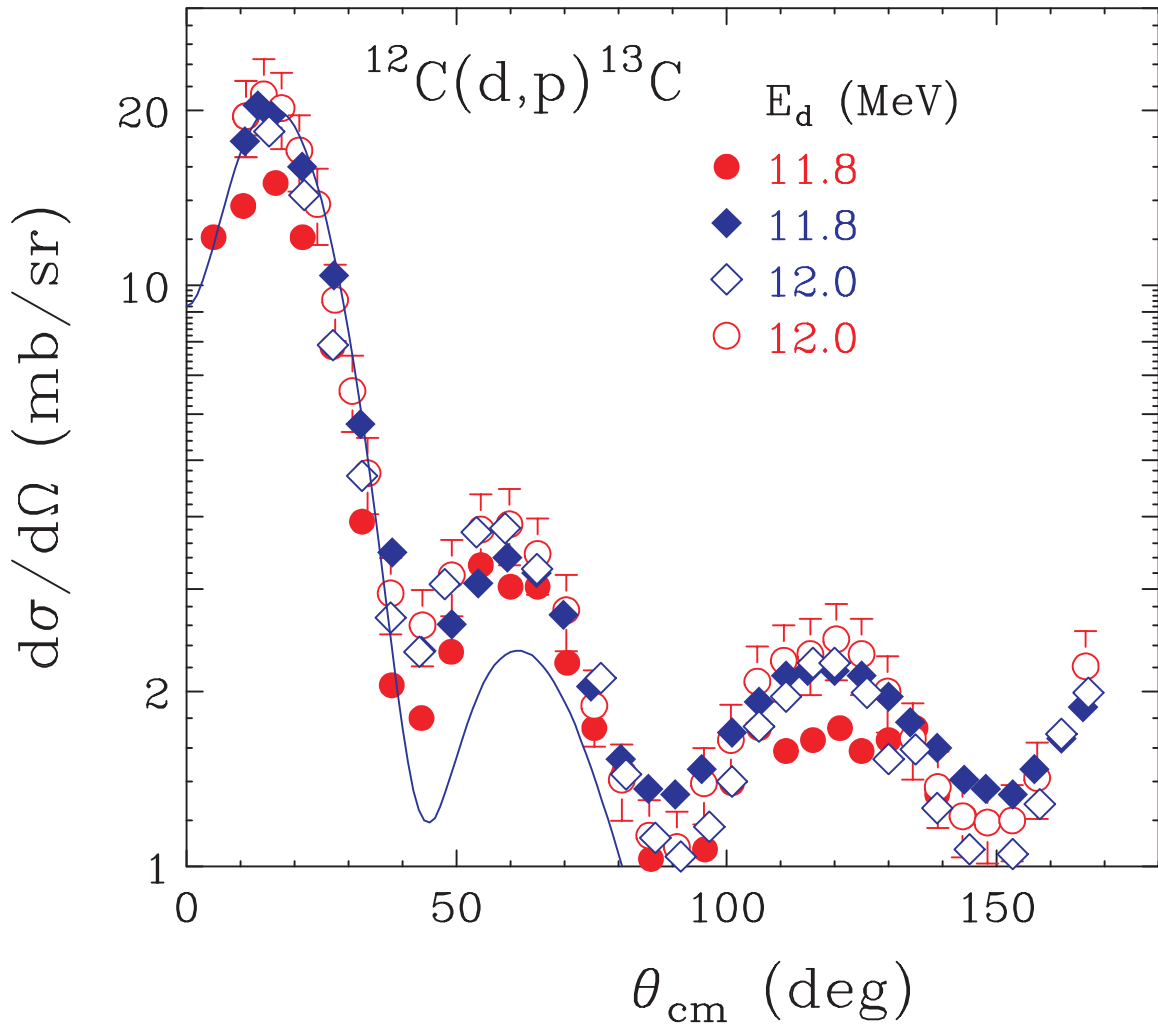


Figure 5: (Color online) Comparison of spectroscopic factors, $SF(JS)$, obtained from Ref. [184] (open circles) and from other measurements (closed circles). The increase of spectroscopic factors observed at $E_d < 10$ MeV has been observed before [20, 23] and has been attributed to the resonance structures in the elastic scattering of the deuterons [250]. The solid line is the mean $SF(JS)$ between 10 and 56 MeV.

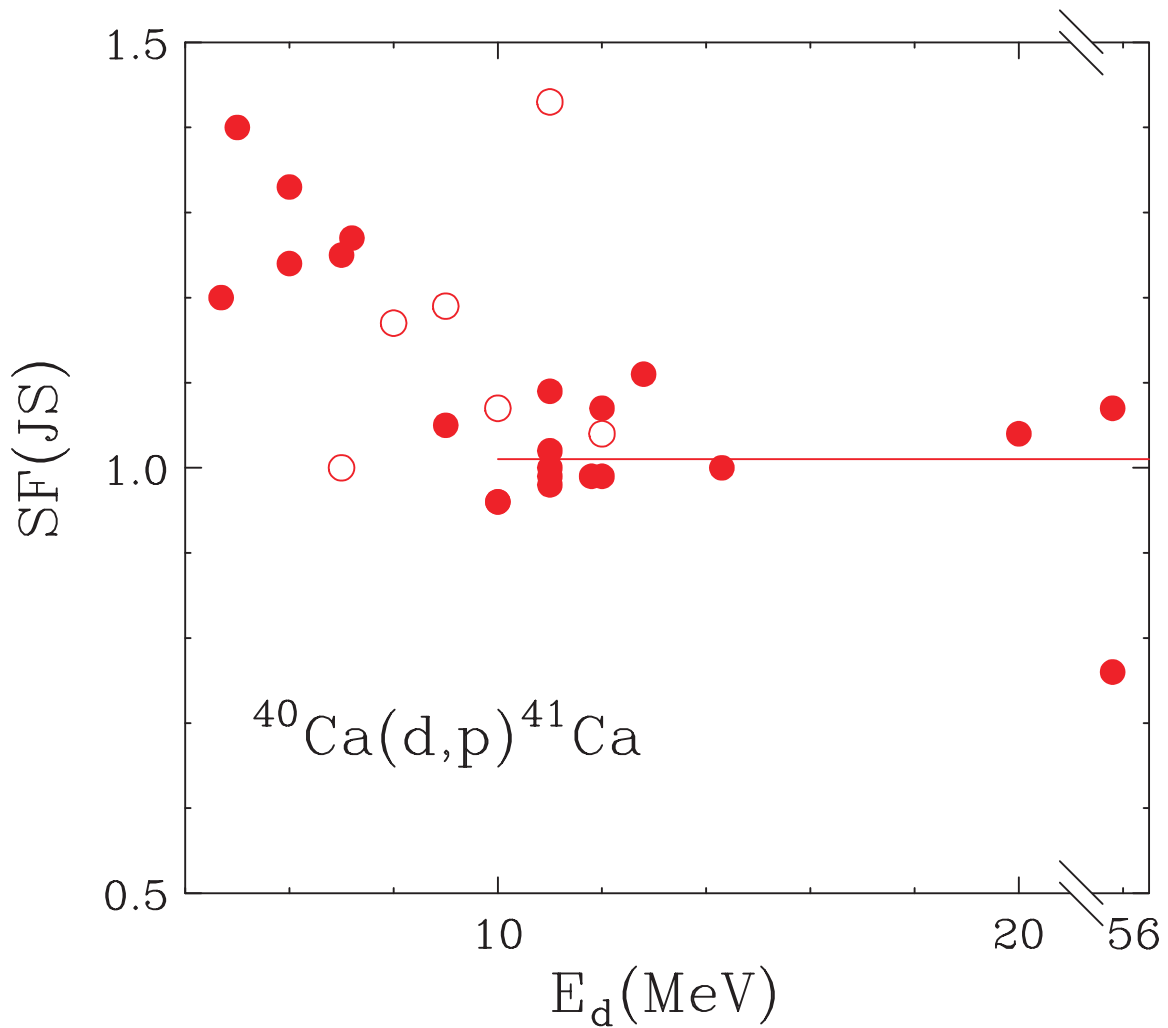


Figure 6: (Color online) Angular distributions for $^{40}\text{Ca}(d,p)^{41}\text{Ca}$ reactions for beam energy from 4.69 to 56 MeV. Each distribution is displaced by factors of 10 from adjacent distributions. The overall normalization factor is 10 for the 7.2 MeV data. References are listed in Table 1.

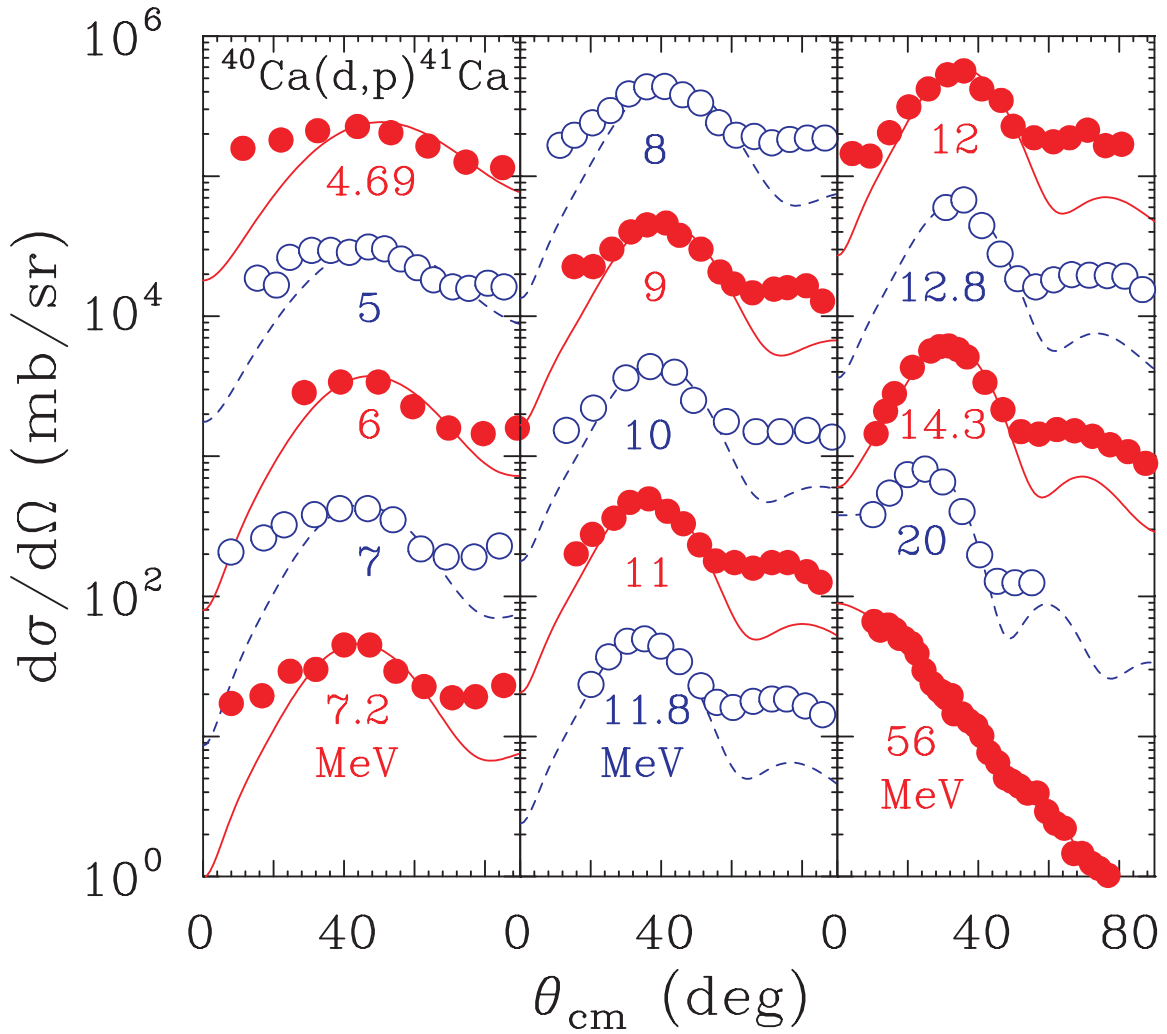


Figure 7: (Color online) Comparisons of the angular distributions of the deuteron measured in the $^{50}\text{Cr}(p,d)^{49}\text{Cr}$ reactions in two different experiments, closed and open circles are data from refs [227] and [228].

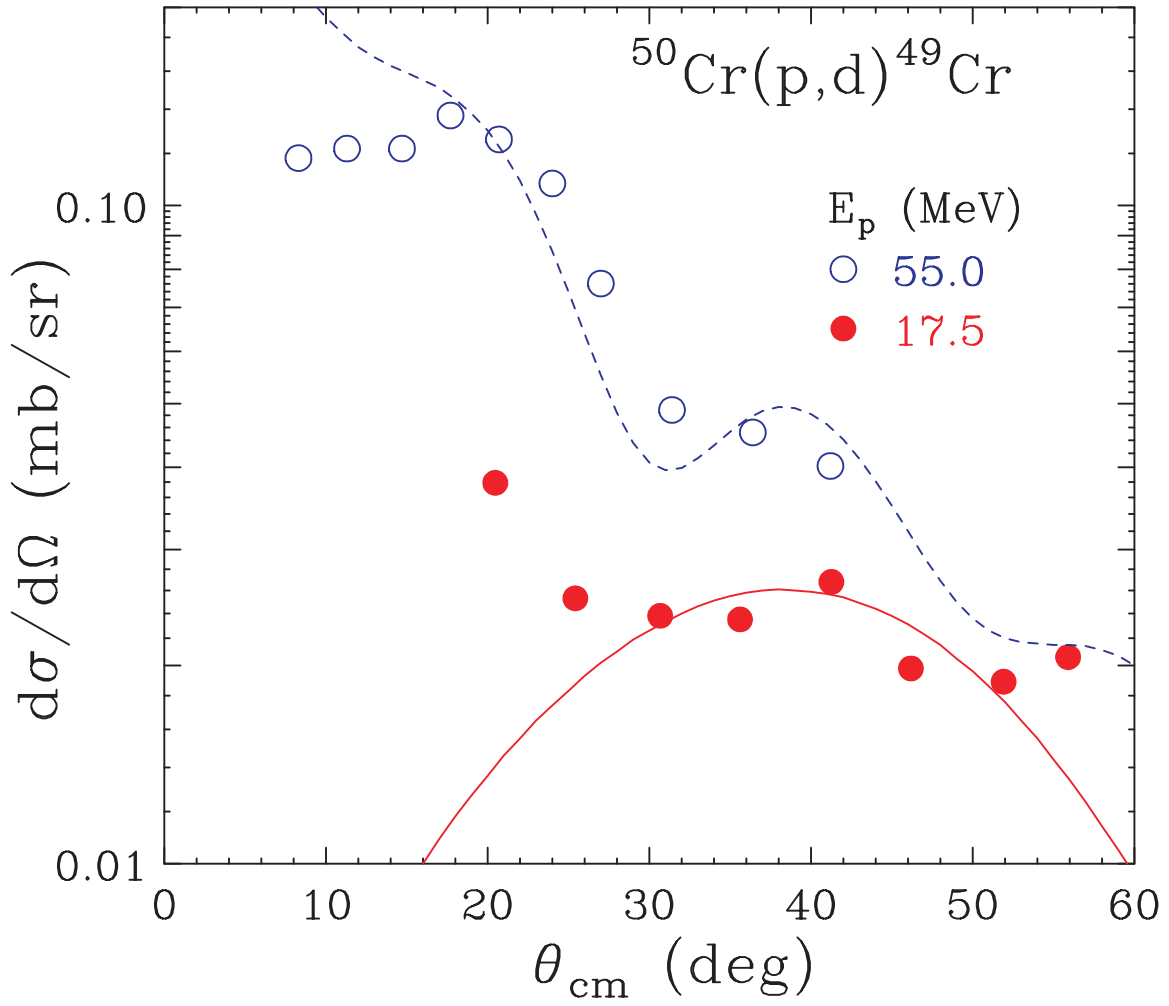


Figure 8: (Color online) Comparisons of spectroscopic factors obtained from (p,d) and (d,p) reactions as listed in Table II. The line indicates perfect agreement between the two values.

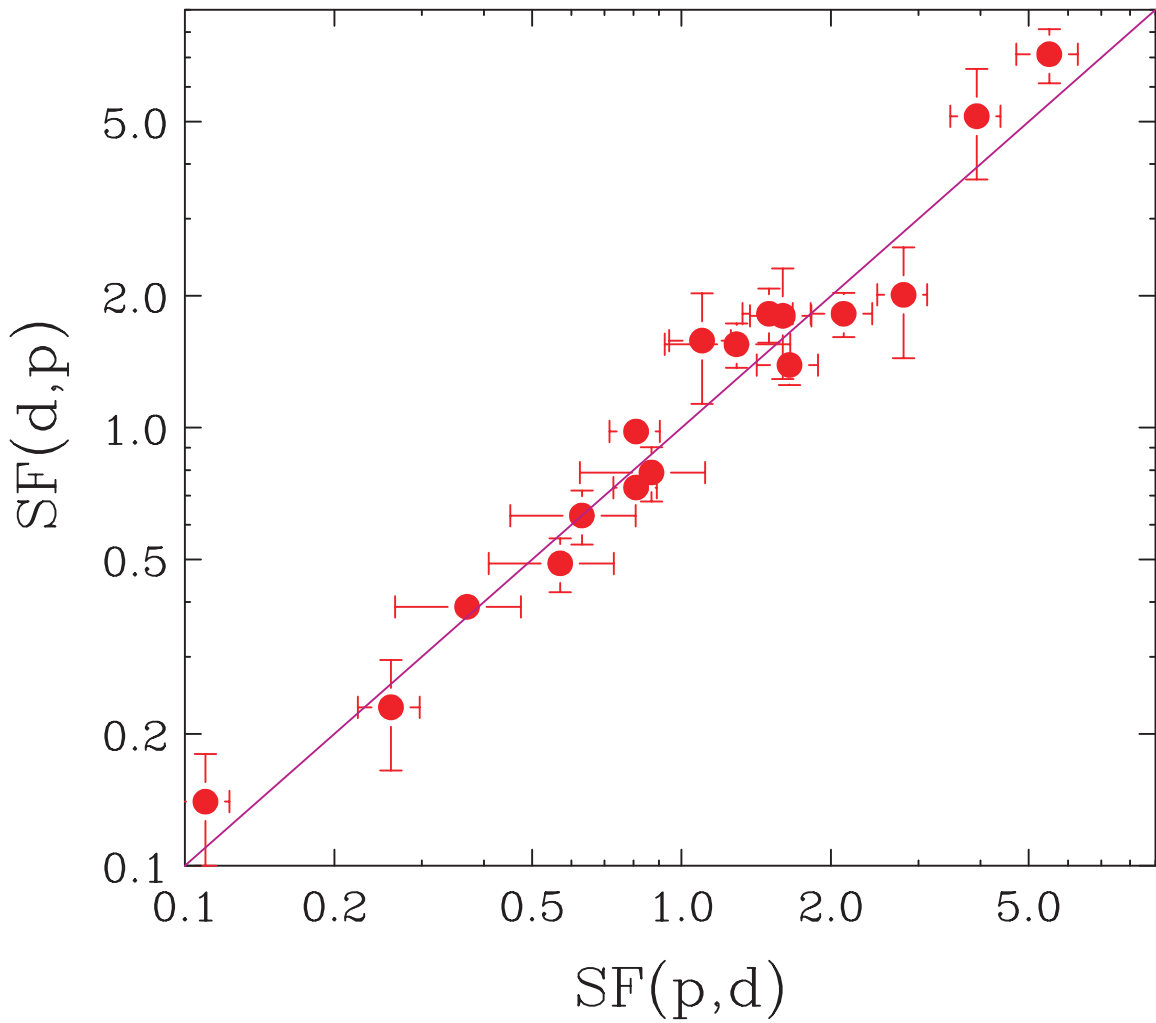


Figure 9: (Color online) Spectroscopic factors obtained for the Ca isotopes. The open stars represent individual measurements. The accompanying solid stars are the weighted averaged values with the associated uncertainties determined from the standard deviations or $20\%/\sqrt{N}$ of the mean SF values whichever is larger.

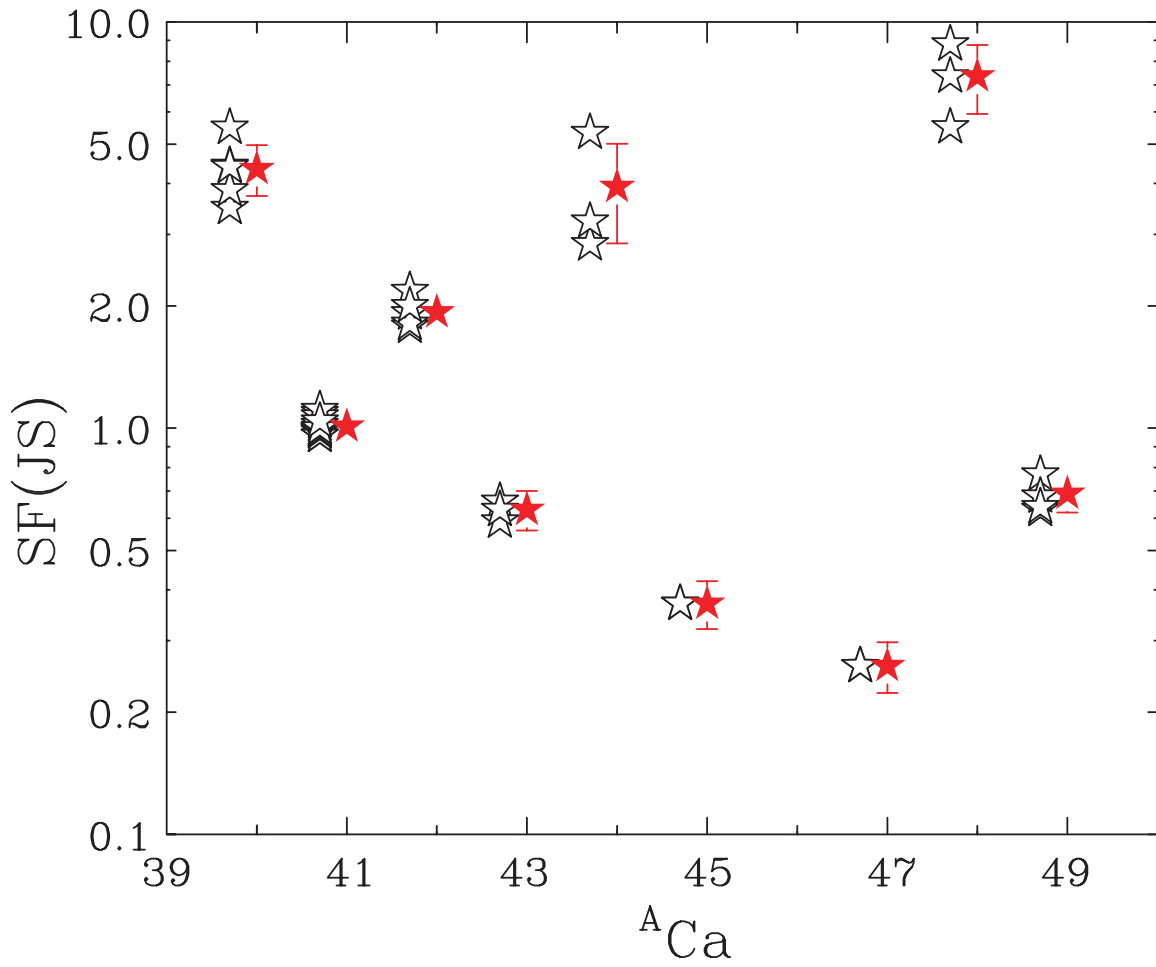


Figure 10: (Color online) Comparisons of spectroscopic factors obtained from this work SF(JS) and the compiled values of Endt [9]. All the values are listed in Table III. The line indicates perfect agreement between our values and Endt's compilation.

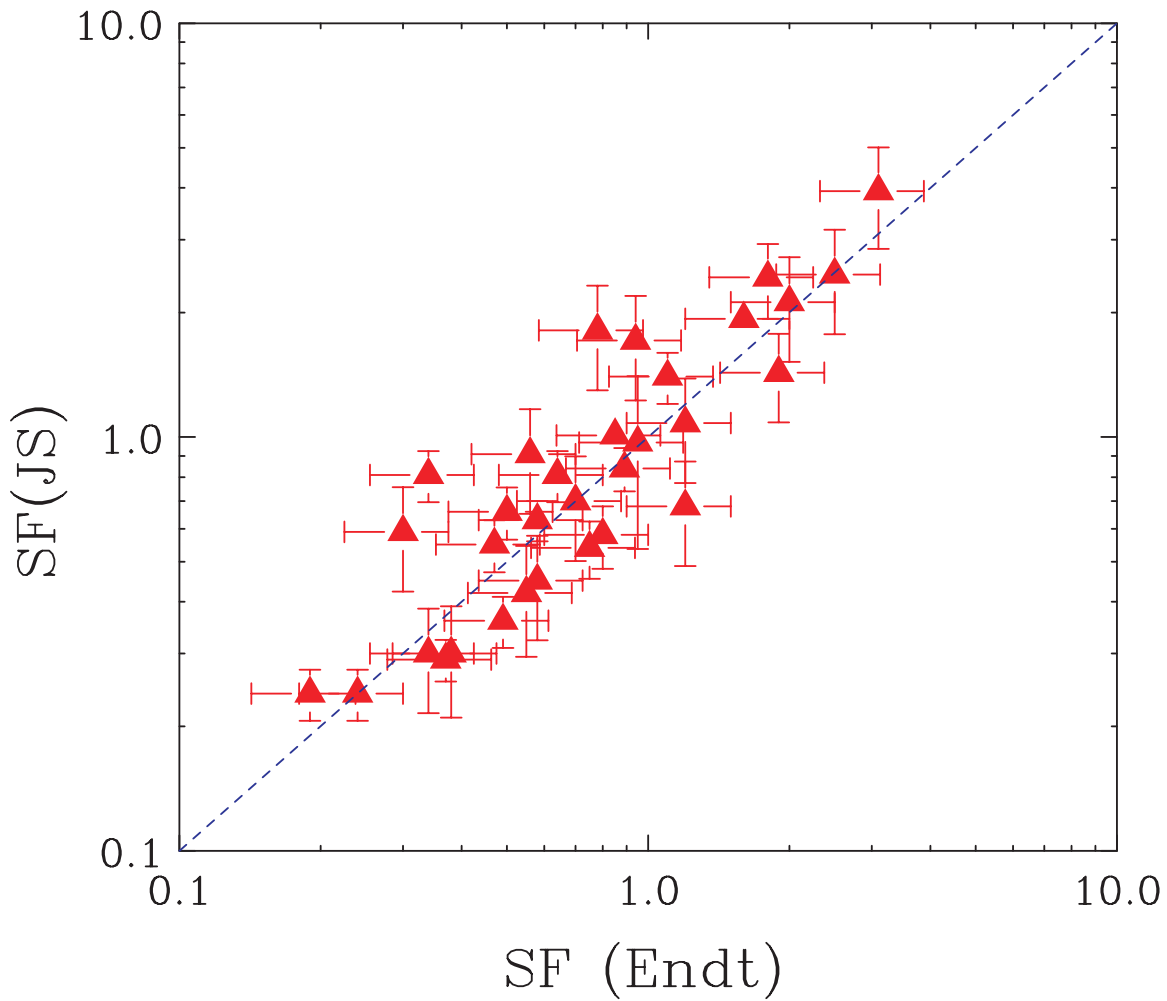


Figure 11: (Color online) Comparisons of three angular distributions of the deuteron measured in the $^{14}\text{C}(d,p)^{15}\text{C}$ reactions in three different experiments with incident deuteron energy of 14 MeV [76] (closed circles), 16 MeV [77] (closed squares) and 17 MeV [73] (open circles). The curve is the predicted angular distributions from the code TWOFNFR as described in the text, multiplied by the spectroscopic factor of 1.1 which fits the data of ref. [76], the only set of data with measurements at angles more forward than 15° .

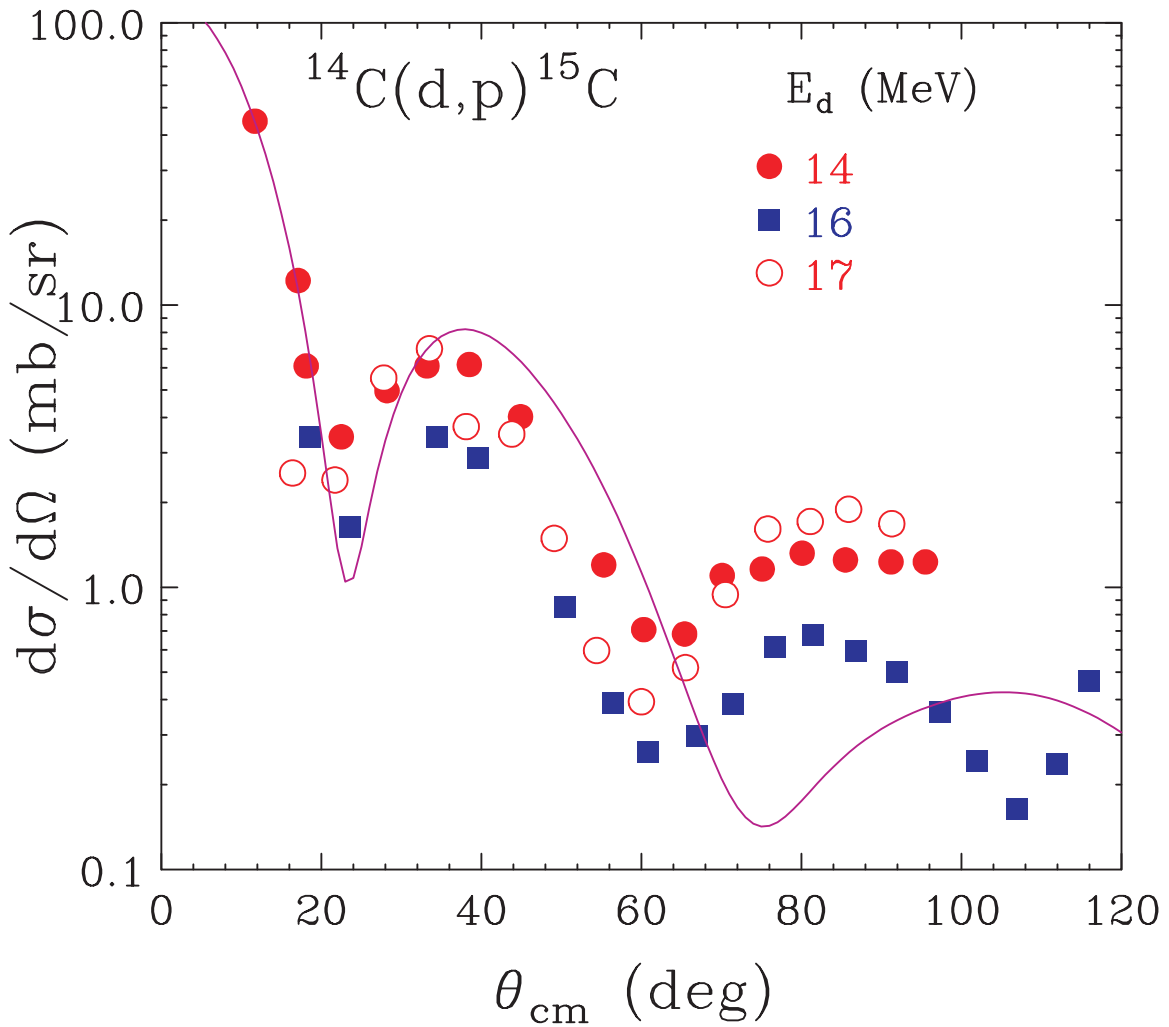


Figure 12: (Color online) Ratios of the SF values from the present work divided by the SF values predicted by the large basis shell model as a function of the neutron separation energy (S_n). Open and closed symbols denote elements with odd and even Z respectively.

