SPECTROSCOPY OF RADIOACTIVE BEAMS FROM SINGLE-NUCLEON KNOCKOUT REACTIONS: APPLICATION TO THE $sd$ SHELL NUCLEI $^{25}_{\text{Al}}$ AND $^{26,27,28}_{\text{P}}$


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Spectroscopy of Radioactive Beams from Single-Nucleon Knockout Reactions: Application to the $^{25}$Al and $^{26,27,28}$P

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Measurements of de-excitation $\gamma$-rays in coincidence with the momentum distribution of the projectile residues produced in reactions of the type $^9$Be($^{28}$P,$^{27}$Si+\gamma)X at energies around 65 MeV/u are used to study single nucleon stripping to individual states. The cross sections are compared with calculations based on a eikonal model description of the reaction and the shell model. The measurements indicate that the halo character of the ground state and other detailed spectroscopic information can be derived using knockout reactions in inverse kinematics.

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A new and general method applicable to nuclear spectroscopy of radioactive beams is presented. The method is based on obtaining partial cross sections from the measured $\gamma$-ray intensities (identifying the individual final states) arising from the decay of states populated in the projectile residue in single-nucleon removal reactions. An extension [1] of the eikonal model is used for translating the measured cross sections into spectroscopic factors. A signature of the orbital angular momentum involved in the reaction is provided by the longitudinal momentum distribution of the projectile residue observed in coincidence with the de-excitation $\gamma$-rays.

Direct nuclear reactions [2] have for many years been one of the most powerful tools for the study of nuclear structure; the current experiment is a variation on this theme. The advantages of the technique described in this article relate to the large nucleon knockout cross sections (more than 10 mb for a typical nucleus and over 100 mb for very weakly bound nuclei). The technique is applicable at energies greater than approximately 50 MeV/u, characteristic of radioactive beams produced in projectile fragmentation [3,4]. More traditional $(d,p)$-type stripping reactions can provide equivalent information, but at energies above 20 MeV/u the proton angular distributions lose most of their characteristic $l$-dependence and the magnitudes of the cross sections drop sharply with increasing energy [2,5]. These $(d,p)$ reactions, also performed in inverse kinematics, require targets more than an order of magnitude thinner than for the technique described here and the identification of the states in the residual nuclei is limited by the energy and angular resolution of the proton detectors. In the present method the use of $\gamma$-ray detection allows states in the final nucleus to be determined, in principle, with high resolution.

The study of momentum distributions in one-nucleon removal reactions goes back to the early work on quasi-free scattering using $(p,2p)$ reactions [6]. This technique identifies nucleons removed from the inner shells of light and medium mass nuclei and the linear-momentum (or angular) distribution of the knocked out nucleon is a measure of its orbital angular momentum. Recent measurements utilize elastic and inelastic electron scattering for probing the spatial and momentum distributions of a single nucleon deep inside the nucleus [7]. Studies using electrons are not yet possible with radioactive beams.

The narrow momentum distribution of the projectile residue associated with the stripping of a halo nucleon is a direct measure of the large spatial extent of the halo [8]. A closer analysis [9] shows that these measurements are insensitive to the part of the halo wave function lying in the shadow of the projectile core. In the present work we extend the observations to more deeply bound states in the projectile residue. The observed momentum distributions then reflect essentially the momentum content on the nuclear surface [10]. This requires a more detailed treatment of the target-core interpenetration [1].

The present work is motivated by a search for changes in nuclear structure in the $sd$ shell due to the predicted existence of proton halos in the nuclei $^{26,27,28}$P. These isotopes have proton separation energies of $0.14(20)$, $0.897(35)$ and $2.066(4)$ MeV respectively: The phosphorus isotopes are the lightest nuclei expected to have a ground state with a dominant contribution of a $\pi s_{1/2}$ orbital. The halo character is expected to manifest itself through relatively large stripping cross sections and narrow longitudinal momentum distributions. The shell-model structure and properties of these nuclei have been discussed in a recent paper [11]. Large halos, strictly
speaking, are only possible for neutrons in s and p states, and the effect of the Coulomb barrier will always make a proton halo less extended [12]. Even in the limit of zero binding energy the halo is of finite size. Due to the effect of the Coulomb barrier, the proton halo for an s state and a core charge 14 is expected to be of relatively modest size compared with the corresponding neutron case. The present measurements were extended to include $^{25}$Al ($S_p = 2.27$ MeV) for a comparative study of proton removal from a nucleus differing only by a few nucleons from the phosphorus isotopes but expected to have a negligible $\pi s_{1/2}$ component [13].

Radioactive beams of $^{26}$Al and $^{26,27,28}$P with energies of approximately 65 MeV/u and momentum spreads of 0.5% were produced in fragmentation reactions using a 100 MeV/u $^{36}$Ar beam on a 470 mg/cm$^2$ Be target and were purified using the A1200 fragment separator at the National Superconducting Cyclotron Laboratory [14].

![Graph showing longitudinal momentum distributions](image)

**FIG. 1.** Longitudinal momentum distributions, in the laboratory frame, of the projectile residue formed in a one-proton removal reaction. The integrated total cross-sections are indicated. a)($^{25}$Al, $^{24}$Mg): the open (filled) circles are the distribution without (with) a coincident $\gamma$-ray from the $2^+ \rightarrow 0^+$ transition in $^{24}$Mg. The dotted line corresponds to a calculated momentum spectrum for an l=2 proton, using a black disk model (see text). The corresponding width is 265 MeV/c. b-d)($^{26,27}$P, $^{26,27}$Si): the continuous lines represent Lorentzian fits. The corresponding widths are 137(33), 116(8) and 143(14) MeV/c, respectively.

The large acceptance S800 superconducting spectrograph [15], operated in a dispersion matched mode, in conjunction with the focal plane detector setup were used to identify and measure the momentum distributions of the projectile residues produced in one-proton breakup reactions of the radioactive beams on a 14 mg/cm$^2$ Be target. Time-of-flight information over a distance of 70 m along with energy measurements obtained with a segmented ion chamber and a 5 cm thick plastic scintillator were used to identify and measure the yields of the fragments in the reaction. Two x/y position-sensitive cathode-readout drift chambers recorded the momentum and angle information of the fragments at the focal plane of the spectrograph. The momentum and scattering angle of the fragments after the reaction were then reconstructed from the known magnetic field and positions at the focal plane using the ion optics code COSY [16]. The measured parallel momentum distributions for $^{25}$Al and the $^{26,27,28}$P isotopes are shown in Fig. 1. Only statistical errors are shown.

The $\gamma$-rays in coincidence with the breakup events were measured using the NSCL position-sensitive NaI(Tl) array of 38 detectors [17] placed around the target chamber. The $\gamma$-ray spectra obtained in coincidence with $^{24}$Mg and $^{27}$Si projectile residues are shown in Fig. 2.

![Graph showing Doppler corrected $\gamma$-ray spectra](image)

**FIG. 2.** Doppler corrected $\gamma$-ray spectra obtained in coincidence with the residues a) $^{24}$Mg and b) $^{27}$Si. The broad peak at around 2.1 MeV in b) could have contributions from several unresolved transitions.

With the limited $\gamma$-ray data it was not possible to construct a complete input-output balance for each level. We have instead used known [18] level schemes and branching ratios together with the theoretical direct cross sections to construct the indirect feeding. The example of $^{28}$P is shown in Fig. 3.

The theoretical nucleon-knockout cross section leading
to a given final state \( n \) (parity and angular-momentum quantum numbers are implicit in our notation) can be written as a sum over the allowed angular momentum transfers \( j \)

\[
\sigma(n) = \sum_j C^2 S(j, n) \sigma_{sp}(j, B_n).
\]  

(1)

Each term in the sum in eq. (1) is a product of two factors. \( C^2 S(j, n) \), the spectroscopic factor of the removed nucleon with respect to a given core state, is calculated from the shell model [19] and accounts for the intrinsic structure. The reaction factor \( \sigma_{sp}(j, B_n) \), the cross section for the removal of a nucleon from a single particle state with total angular momentum \( j \), is calculated in the eikonal model. The assumed nucleon separation energy \( B_n \) is the sum of the nucleon separation energy for the ground state and the excitation energy of the state \( n \).

\[
P(n) = \langle \phi_{IM} | (1 - |S_n|^2) |S_C|^2 |\phi_{IM} \rangle,
\]

(2)

where the wave function is that of the initial \((C+N)\) state. The single-particle cross section is obtained by integrating over the impact parameter and averaging over \( M \) states. This expression has an intuitively simple interpretation: the first factor represents the probability that the nucleon interacts with the target and the second factor the associated probability that there be no interaction between the core and the target. The additional contribution to the one-nucleon removal cross section arising from diffractive dissociation was also included [1]. For halo states this is of comparable magnitude, but it becomes considerably smaller for states with higher angular momentum or binding energy. The profile functions were calculated using a parameterized nucleon-nucleon interaction [1] and Gaussian core and target densities consistent with electron scattering data.

FIG. 3. Simplified level scheme for the \(^{27}\text{Si}\) core based on [18]. The observed \( \gamma \)-rays are shown as thickened arrows and the experimental cross sections include both direct and indirect contributions. The calculated partial cross-sections are given alongside. The indirect feedings are obtained from the calculated direct feeding of the higher lying states and the known \( \gamma \)-ray branchings. The measured experimental cross section for the direct population of the ground state is obtained from the analysis of the momentum spectrum in Fig. 4b. The cross section for the 2164 keV level may include contributions from unresolved transitions.

The single-particle cross sections entering eq. (1) have been calculated by Tostevin [1], extending the methods of [20] to estimate the required integrated partial cross sections. Expressed in terms of the profile functions \( S_C \) and \( S_N \) for the core \((C)\) and nucleon \((N)\) interactions with the target, the probability of stripping [21] becomes

\[
\sigma^{(a)} = \sigma \times \frac{\langle |S_C|^2 |\phi_{IM} \rangle}{\langle |S_n|^2 |\phi_{IM} \rangle}.
\]

(3)

FIG. 4. Longitudinal momentum spectra for \(^{27}\text{Si}\) projectile residues. a) The open (filled) circles correspond to the absence (presence) of coincident \( \gamma \)-rays in the NaI(Tl) array. b) Derived longitudinal momentum spectrum corresponding to the ground (open) and excited states (filled) in the projectile residue \(^{27}\text{Si}\) obtained from Fig. 4a. The continuous and dashed lines are calculated longitudinal momentum distributions with widths 93 and 248 MeV/c, in the laboratory frame, for the \( s \) and \( d \) states, respectively.

The longitudinal momentum distributions were calculated in an extension of a model [9] that replaces the profile functions by a sharp cutoff (black disk) approximation. The cutoff radii were chosen to reproduce the core-target and nucleon-target total cross sections, and it was verified that with this choice, the stripping cross sections and their dependence on the separation energy agrees approximately with those calculated in [1]. The momentum distribution is obtained as the spatial integral
of the one-dimensional Wigner function. In the earlier calculation the wave function was approximated by its value along the trajectory of the target; in the present work the full three-dimensional integration was carried out. This modification has an appreciable effect on the cross section for deeply bound states or for a charged valence nucleon, but it is less important for the width of the momentum distribution. For a $\pi s_{1/2}$ state in $^{28}$P, the width in the c.m. system increases from 75 MeV/c [11] to 87 MeV/c. The figures show the distribution in the lab system, wider by the relativistic factor $\gamma$.

Fig. 1 clearly illustrates the variance in the shapes of the longitudinal momentum distributions for $^{26}$Al as compared to the phosphorus isotopes. The measured partial cross sections $\sigma$ and their distributions $d\sigma/dp_{\parallel}$ are compared with the theoretical approach presented earlier. For $^{25}$Al, the longitudinal momentum spectra as seen from Fig. 1a have the same $d$-wave shape for the ground and excited states. The dominance of $d$-wave removal is predicted by theory [13,16] and leads to the following cross sections in mb with the experimental values given in brackets: total, $47 \pm 13$; $4^+ \rightarrow 2^+$, $9 \pm 4$; $2^+ \rightarrow 0^+$, $36 \pm 10$. The excited states in this case are mainly fed indirectly, i.e. via unobserved higher states. The three phosphorus isotopes have momentum distributions (Fig.1b-d) that are expected to be a mixture of $s$ and $d$ components. The total cross sections are $82 \pm 11$ for $^{27}$P and $54 \pm 70(11)$ for $^{28}$P.

For the $^{28}$P case, cross sections for the two lowest excited states, which are not expected to have appreciable indirect feeding agree well with the measurements as seen from Fig. 3. The cross section to the ground state was extracted from the measured momentum distributions with and without $\gamma$-rays in coincidence with the projectile residue ($^{24}$Si). A linear combination of the two measured momentum spectra of Fig. 4a along with an estimate for the background and the $\gamma$-efficiency were used to construct the individual components shown in Fig. 4b. The two extracted momentum distributions are representative of the ground state and the sum of all the transitions to excited states. This confirms the shell model predictions that the ground state has a dominant $s$ component whereas the excited states involve $d$ components. From such a procedure, we obtain a ground state probability of $30(6)$%, in good agreement with the theoretical direct component given in Fig. 3 and $30(10)$% in the case of $^{27}$P compared with a theoretical prediction of 28%. These large cross sections and narrow momentum widths for the ground-state structure are evidence for the proton halo structure discussed in [11].

In summary, a new method for extracting spectroscopic information in experiments using fast radioactive beams has been reported. Its application to several cases in the $sd$ shell demonstrates that valuable nuclear-structure and angular-momentum information can be obtained from measurements of partial cross sections and momentum distributions in single-nucleon removal reactions. The important role of the $\pi s_{1/2}$ orbital in the predicted halo structure of the neutron-deficient phosphorus isotopes has been confirmed. At present, intensity and $\gamma$-ray resolution seriously limit the technique, but the higher beam intensities and improved detection techniques expected to be available within the next few years will offer interesting possibilities for studying nuclei far from the valley of stability.

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[21] The word "stripping" is here used in the sense in which it was coined to describe the breakup of 90 MeV/u deuterons, see the comment by R. Serber, Ann. Rev. Nucl. Part. Sci. 44, 1 (1994).