

National Superconducting Cyclotron Laboratory

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Abstract

Transition rates from the ground to selected states in ¹⁹Ne have been measured by their gamma yield following intermediate-energy radioactive ion beam Coulomb excitation. These are compared to corresponding transitions in ¹⁹F and to shell model calculations. An upper limit on the cross-section of the 4.033 MeV state places a limit on the transition rate and hence on total electromagnetic decay width Γ_{γ} of this state, which is of astrophysical interest. Combining the results with an upper limit on the lifetime of this state and shell model calculations gives an estimate of its width. PACS numbers: 26.50+x, 21.10.Ky, 25.70.De, 27.20.+n

Typeset using REVTEX

Electromagnetic transitions rates in ¹⁹Ne are of both theoretical and astrophysical interest (see Figure 1). A comparison with ¹⁹F provides a test of isospin symmetry in a situation where detailed *s*-*d* shell calculations are tractable [1]. Furthermore, the transition rates can be directly related to level widths that help determine the astrophysical reaction rate of the ¹⁵O(α,γ)¹⁹Ne reaction. This rate determines the conditions of temperature and density for break-out of the hot CNO cycle in explosive burning scenarios such as those that occur in nova explosions or in X-ray bursts. Such a break-out leads to a flow process through proton rich nuclei and results in an increased rate of energy production [2].

The 4.033 MeV $3/2^+$ state dominates this rate owing to its proximity to energy threshold and that it can be reached from the ¹⁵O $1/2^-$ ground state by an angular momentum of l = 1. The gamma width Γ_{γ} for the 4.033 MeV state is much larger than the alpha width Γ_{α} [3–5]. In this circumstance the reaction rate depends only on the excitation energy of the state, which is well known, and on Γ_{α} , which is poorly known. Given the value of Γ_{γ} , one could obtain Γ_{α} from a measurement of the branching ratio $\Gamma_{\alpha}/\Gamma_{\gamma}$. Neither of these quantities is known at present, and estimates of the rate are based on the value of Γ_{α} for the analog of the 4.033 MeV state, located at 3.908 MeV in ¹⁹F [5]. It has been argued that such estimates are uncertain by as much as an order of magnitude [6].

We have determined reduced transition probabilities involving four excited states in ¹⁹Ne from their γ yields following intermediate-energy Coulomb excitation of radioactive ¹⁹Ne. The results are compared to corresponding states in the mirror nucleus ¹⁹F and to modern *p-s-d* shell model calculations. The measurements yield an upper limit on the reduced transition probability for the 4.033 MeV $3/2^+$ state, and combining this result with an upper limit on the lifetime of the state and with the shell-model calculation yields a gamma width of 12^{+9}_{-5} meV.

The experiment was typical of radioactive-beam Coulomb excitation experiments at the National Superconducting Cyclotron Laboratory (NSCL) [7]. A primary beam of ²⁰Ne at 80 MeV/nucleon from the K1200 cyclotron impinged on a 200 mg/cm² ⁹Be target. The fragmentation products were analyzed with the A1200 fragment separator [8], which provided

 3.5×10^{4} ¹⁹Ne ions per second at an energy of 55.0 ± 0.3 MeV/nucleon. The beam was then delivered to a 518 mg/cm² Au target located at the focus of the NSCL position-sensitive NaI(Tl) array [9]. A fast-slow phoswich detector was placed downstream for positive identification of ¹⁹Ne ions deflected to $\theta_{lab} < 5.0$ deg; this arrangement selects ions with a minimum impact parameter $b_{min} = 13$ fm (17.5 fm) at the upstream (downstream) face of the target. The NaI(Tl) array detected de-excitation γ rays following inelastic scattering in coincidence with the identified ¹⁹Ne particles. The position information from the NaI array was used for relativistic Doppler correction of the measured photon energy.

A beam-frame photon spectrum, gated on ¹⁹Ne particles, prompt γ -ray times for background reduction, and photon multiplicity of one, is shown in Figure 2. The de-excitation photon spectrum is complicated, owing to two factors. First, the decay of the individual states often involves non-negligible branches to other excited states, rather than directly the ground state. Second, for the roughly 4 MeV photons emitted from high-lying states of interest, there is a high probability for escape of annihilation photons following pair production.

To determine excitation probabilities, GEANT simulations [10] were performed for the γ rays that were expected to be observed in the experiment. These simulations included intrinsic detector energy and position resolution and Doppler effects. The simulations of stationary source data closely reproduced the measured photopeak efficiency and adequately described the spectral shape [11]. The decay from a given state was modeled by taking the appropriate linear combinations of the simulated spectra using experimental branching ratios reported for ¹⁹Ne in Ref. [3]. These branching ratios themselves have measurement uncertainties, but the errors are correlated since the sum of the branching ratios must add up to 1. An error in the branching ratios, then, would simultaneously overpredict one branch and underpredict another, the net result being a second-order systematic effect which is much smaller than the statistical uncertainties in our measurement. The normalizations of these summed, simulated spectra for each state were then treated as free parameters in a MINUIT [12] χ^2 minimization to best-fit the observed γ -ray spectrum. The simulated spectra

for the decay of the 1.536, 1.616, 4.033, and 4.600 MeV states were used. All of these states could be excited by E1, E2 or M1 modes. The 4.549 MeV state could be populated by E1 excitation, but it was not included in the fit because the data for the analog state in ¹⁹F indicated it would have a cross section much smaller than the experimental sensitivity. The fit included two exponential functions to model backgrounds. A broad Gaussian near 5.3 MeV was also required to fit the data; it may describe unresolved decay from $E_x > 5$ MeV states for which little γ spectroscopic information is known [3].

The best fit spectrum is shown in Figure 2, and the results of the analysis are reported in Table I. All cross sections are corrected for photon angular acceptance bias by integrating the angular distributions calculated [13] for the dominant peak in the de-excitation spectrum. Based on the data for the 1.554 MeV mirror state in ¹⁹F, it was expected that the M1 contribution to the excitation cross section for the ¹⁹Ne 1.536 MeV state would be three orders of magnitude lower than that for E2 excitation [1,3]. Mixing ratios for de-excitation $\Delta J = 1, \Delta \pi = 0$ transitions are not known. For the 1.536 MeV state, this introduces a systematic ±13% limit uncertainty. A further correction is needed for the α decay branch of the 4.600 MeV state, for which $\Gamma_{\alpha}/\Gamma_{tot} = 0.25 \pm 0.04$ [4]. Nucleon or light-ion decay modes are not energetically possible from this state and β decay would be negligible, so the α/γ branching ratio can be determined from this value.

To extract the $B(\sigma\lambda, 1/2_{g.s.}^+ \to J^{\pi})$ reduced transition probability, given in Table I, the formalism of Winther and Alder [13] as implemented in the RELEX code [14] was used to calculate the expected cross section for unit $B(\sigma\lambda)$ values, and this was then compared to the measured values. Mid-target kinematic parameters of $\beta = 0.307$, $\theta_{cm} < 5.48$ deg and $b_{min} = 15.3$ fm were used in these calculations. To account for uncertainties in this procedure and in the experimental parameters, an additional 10% systematic uncertainty is assigned to the reduced transition probabilities.

These transition rate measurements are compared to existing data for ¹⁹Ne and also to analog states in the mirror nucleus ¹⁹F in Table I. Data for ¹⁹Ne only exists for the ¹⁹Ne 1.616 MeV state [3], and the lifetime measurements of this state following (α ,n) [18] and (p,n) [18,19] reactions are inconsistent with one another. These Doppler-shift attenuation measurement (DSAM) experiments following light-ion fusion-evaporation reactions would be unable to account for the effective lifetime of the gamma ray cascade feeding the states of interest, which would result in a larger apparent lifetime for the state. Hence, these transition rates should be regarded as lower limits.

Table I also includes full *s*-*d* shell model calculations for ¹⁹Ne that are similar to those used in the analysis of ¹⁹F(*e*, *e'*) data [1], which used effective M1 and E2 operators as discussed in Ref. [20]. The agreement with the data is quite good. In particular the calculated B(E2) values are larger in ¹⁹Ne than ¹⁹F for *s*-*d* shell dominated transitions, which both agrees with experiment and with what one would expect since ¹⁹Ne has two valence protons whereas ¹⁹F has just one.

The 2σ upper limit of the reduced transition probabilities for excitation of the 4.033 MeV $3^{\prime}2^{+}$ state from the ground state can be used to place an upper limit on the width for the γ branch to the ground state, $\Gamma_{\gamma,g.s.}$. Knowing the measured γ branching ratios to excited states [3], the total gamma width Γ_{γ} can be calculated¹. Since the decay is dominantly electromagnetic, $\Gamma \simeq \Gamma_{\gamma}$. The upper limit on the excitation cross section yields upper limits Γ_{γ} of 430 meV (0.34 meV) for excitation and subsequent decay by pure M1 (E2) transitions. The mixing ratio δ , where $\delta^2 \propto (B(E2)/B(M1))E_{\gamma}^2$ is the ratio of E2 and M1 partial transition rates, is not known. However, M1 dominance ($\delta \sim 0$) is consistent with DSAM, where a reported 2σ upper limit on lifetime corresponds to a $\Gamma_{\gamma} > 6.6$ meV [16]. By contrast, E2 dominance ($|\delta| \sim \infty$) is inconsistent with the DSAM data. Figure 3 demonstrates how the upper limit on Γ_{γ} for the ¹⁹Ne 4.033 MeV $3/2^+$ state varies depending on the mixing ratio δ . The gamma width is compared to the DSAM measurement. E2 excitation generally

¹The uncertainties in branching ratios are correlated and would introduce an additional $\sim 10\%$ statistical uncertainty in the present measurement. Since the current data provide an upper limit, this effect is neglected in the discussion.

dominates intermediate-energy Coulomb excitation, so even a small E2 admixture would decrease the total Γ_{γ} that would be consistent with the current measurement. For example, for $|\delta| = 0.03$, the upper limit on Γ_{γ} is 1/2 that for $\delta = 0$, and for $|\delta| = 0.23$ the upper limit is the same as the lower limit derived from the DSAM measurement [16]. From a different point of view, our results restrict this mixing ratio to $|\delta| < 0.23$ for the decay of the 4.033 MeV state to the ground state.

Before further discussion of our experimental results on the 4.033 MeV 3/2⁺ state in ¹⁹Ne, it is worth noting that this state and its analog in ¹⁹F have long eluded a straightforward shell-model description. In the original analysis of Ref. [1], it was concluded that the second $3/2^+$ state in ¹⁹F at 3.908 MeV did not have a three-particle (3p) s-d shell configuration but was more likely a five-particle, two-hole (5p-2h) configuration with two nucleons excited from the p shell. In the present work, the energy of the 5p-2h configuration for the A = 19mirror nuclei was calculated using the WBP Hamiltonian of Warburton and Brown [21]. The lowest eigenstate of the 5p-2h configuration indeed has $J^{\pi} = 3/2^+$ and an excitation energy of 4.50 MeV, which is in reasonable agreement with the experimental excitation energies of 4.033 and 3.908 MeV in ¹⁹Ne and ¹⁹F, respectively. However, the B($\sigma\lambda$) values for pure 3p to 5p-2h excitations vanish since they cannot be connected by a one-body electromagnetic operator. Mixing between the 5p-2h and 3p configurations was calculated using the Kuo-Brown G matrix for the off-diagonal interaction as a perturbation, and the reduced transition probabilities reported in Table I were extracted from the matrix elements calculated for the resulting mixed wave function. It should be noted that for these reduced transition probabilities, the M1 Coulomb excitation probability in this experiment would be only 5% that of the E2 excitation probability, but the corresponding partial gamma decay width would be 50 times greater. The 5p-2h calculations also yield matrix elements for decay of this $3/2^+$ state to the first excited $5/2^+$ and $3/2^+$ states. These branches would be 20% and 55% as intense as the decay directly to the ground state in ¹⁹Ne, and 30% and 63%in ¹⁹F. These compare well to the measured branching ratios [3], suggesting that the present model is reasonable and can be used to describe the second $3/2^+$ state in the A = 19 mirror

nuclei.

The results of the 5p-2h calculations may now be compared to our experimental results on the ¹⁹Ne $3/2^+$ state at 4.033 MeV. Taking the calculated matrix elements for the 5p-2h state and the observed excitation energy and γ branching ratios, $\Gamma_{\gamma,5p2h} = 22$ meV and $\delta_{5p2h} = +0.14$. This point is plotted on Figure 3. Furthermore, one may use the calculated value of the mixing ratio δ along with the measured Coulex cross sections to better constrain the upper limit on Γ_{γ} . As indicated in Table I, for the value of δ_{5p2h} from the calculations, the present experiment would limit B(M1)< 0.035 $\mu_{\rm N}$ and B(E2)< 0.61 e^2 fm⁴, with a resulting limit of $\Gamma_{\gamma} < 17$ meV. For the decay of the corresponding 3.908 MeV state in ¹⁹F, the 5p-2h calculations yield $\Gamma_{\gamma} = 28$ meV and $\delta = -0.18$. The gamma width of this state in ¹⁹F has been reported as $\Gamma_{\gamma} = 75^{+100}_{-25}$ meV [17], while angular distribution measurements [22] are stated to be consistent with $\delta \sim 0$, although this depends on an assumption that the feeding transition is itself a pure dipole transition.

While the current measurement on its own only provides an upper limit on Γ_{γ} , it can be considered with other data to provide an estimate of Γ_{γ} . The present upper limit on the gamma width, $\Gamma_{\gamma} \pm \sigma_{\Gamma}$, and the DSAM measurement of the lifetime, $\tau \pm \sigma_{\tau}$, are two independent data points. If the width of the state is treated as a free parameter $\Gamma_{\gamma p}$, then there is an associated goodness-of-fit function $\chi^2(\Gamma_p) = [(\Gamma_{\gamma p} - \Gamma_{\gamma})/\sigma_{\Gamma}]^2 + [(\hbar/\Gamma_{\gamma p} - \tau)/\sigma_{\tau}]^2$ indicating how well that parameter fits the Coulomb excitation and DSAM data. Minimizing this function determines the best estimate of the width, and finding the points at the minimum plus one determines the 1 σ uncertainties. Using the Γ_{γ} upper limit fixed at $\delta = +0.14$ as calculated in the 5p-2h shell model, the best estimate of Γ_{γ} width of the ¹⁹Ne 4.033 MeV state is 12^{+9}_{-5} meV. Although this is the best estimate based on the available data, it does not take into account the uncertainty in the calculated mixing ratio δ . For a pure M1 transition ($\delta = 0$), the estimate becomes 45^{+200}_{-33} meV.

Measurements of the ¹⁵O(α, γ) reaction by accelerating radioactive ¹⁵O ions on a gaseous helium target, are being planned for various ISOL facilities [23]. However, these experiments will be extremely difficult, requiring high-intensity beams and extremely clean analysis systems. They are not assured of success. For this reason, there are attempts to measure the branching ratio $\Gamma_{\alpha}/\Gamma_{\gamma}$ for the decay of the 4.033 MeV state following its formation in a reaction [24]. These measurements are also difficult, and will still require the previously unknown value of Γ_{γ} to obtain Γ_{α} . The present data provide an estimate of Γ_{γ} that can be used along with branching ratio data to calculate the astrophysical reaction rate. In addition, the data provide guidance for future high-resolution γ spectroscopy studies. A measurement of the mixing ratio for the ¹⁹Ne 4.033 MeV γ -ray could further constrain the values of Γ_{γ} that are consistent with the Coulomb excitation and lifetime data. Also, the current measurement establishes a lower limit of 1.8 fs for the 4.033 MeV state that can be used to evaluate the feasibility of future DSAM experiments.

In conclusion, an intermiediate-energy Coulomb excitation measurement of the radioactive ¹⁹Ne nucleus has been performed. Reduced transition probabilities for excitations to selected states are reported and found to be in reasonable agreement with expectations based on isospin symmetry and *s*-*d* shell model calculations. The upper limit on the excitation cross section of the 4.033 MeV $3/2^+$ state yields an upper limit of 430 meV if the transition is pure magnetic dipole. Shell-model calculations with 5p-2h configurations yield $\Gamma_{\gamma,5p2h} = 22$ meV and $\delta_{5p2h} = +0.14$. Using the experimental cross sections from the current experiment, the calculated mixing ratio, and the limits from a prior DSAM experiment, the best estimate of the total gamma width is $\Gamma_{\gamma} = 12^{+9}_{-5}$ meV.

This work was supported by the National Science Foundation under contracts PHY-9528844, PHY-9875122, and PHY-9605207. G.H. also acknowledges support from the University of Kansas General Research Fund and the U.S. Department of Energy, Contract DE-FG03-96ER40981.

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TABLES

TABLE I. Cross sections for excitation from the ground state and reduced transition probabilities measured in this experiment. Reduced transition probilities are reported in in units of $10^{-4} e^2 \text{fm}^2$ for E1, $e^2 \text{fm}^4$ for E2, and μ_N for M1 transitions. The 1 σ errors are statistical and systematic, respectively. For the 4.033 MeV state, the reported B($\sigma\lambda$) is the 2 σ upper limit. In the cross-section measurements, the dominant systematic error comes from ambiguous angular distributions from mixed M1/E2 transitions; only in the case of the 1.536 MeV state is this not negligible compared to the statistical error. Also shown are values from previous measurements for two low-lying states and data from analog transitions in ¹⁹F, see text for details.

¹⁹ Ne							¹⁹ F	
$E_{ m exc}$		$\sigma\lambda$	$\sigma_{ m exc}$	$\mathrm{B}(\sigma\lambda,\uparrow)$		$\mathrm{B}(\sigma\lambda,\uparrow)$		
(MeV)	J^{π}	exc.	(mb)	This Work	Other Meas.	Calc. ^a)	Meas.	Calc. ^{a)}
1 .536	$3/2^{+}$	E2	$23.6\pm0.3\pm3.1$	$79 \pm 1 \pm 18$		93.4	50 ^{b)}	49.6
1.616	$3/2^{-}$	E1	2.1 ± 0.3	$18\pm3\pm2$	$4.2 \pm 0.8 ~^{c,d)}$		9 ± 2 ^{c)}	
4.033	$3/2^{+}$	M1	-0.21 ± 0.19	$< 0.90^{~e)}$		0.045		0.044
		E2	-0.19 ± 0.17	< 0.64 $^{e)}$		0.80		1.28
4.600	$5/2^{+}$	E2	4.2 ± 0.3	$20\pm2\pm2$		24.4	8 ^{b)}	7.0
0.238	$5/2^{+}$	E2	<i>f</i>)	<i>f</i>)	123 ± 4 ^{c)}	132.8	64.3 ± 0.8 ^{c)}	68.9
0.275	$1/2^{-}$	E1	<i>f</i>)	<i>f</i>)	49 ± 2^{c}		55.3 ± 0.7 ^{c)}	

a) Calculated as discussed in text.

b) Derived from Ref. [1].

c) From Ref. [3].

d) Adopted value from DSAM experiments that are not in agreement; see discussion in text.

e) These 2σ limits assume unmixed transitions. For $\delta = +0.14$, the measured cross section

places simultaneous limits of $< 0.035 \ \mu_N$ on B(M1) and $< 0.61 \ e^2 \text{fm}^4$ on B(E2).

f) Not measurable in this experiment due to energy threshold effects.



FIG. 1. Partial schematic energy level diagram for ¹⁹Ne. Solid vertical arrows indicate the Coulomb excitation (up) and subsequent γ decay (down) observed in the experiment. The numbers in italics are the excitation cross sections measured in this experiment in mb; all other numbers (excitation energies in MeV, spins and parities, and gamma relative branching ratios normalized to 100 for the strongest transition) are taken from the references. Dashed vertical arrows for the 4.033 MeV state indicate that these transitions were not positively identified in this experiment. Dashed oblique arrows indicate the α decay branches to ¹⁵O; the present work did not measure these. Also shown are selected levels in the mirror nucleus ¹⁹F with dashed lines identifying their analog states in ¹⁹Ne. See text for uncertainties and further details.



FIG. 2. Data points: energy spectrum of ¹⁹Ne de-excitation γ rays following intermediate-energy Coulomb excitation observed in the beam frame of reference. Solid curve: best fit to data. Broken curves: contributions to best-fit from each of the four states included in the fit; for the 4.033 MeV state, the curve shows the 2σ upper-limit yield. See text for details.



FIG. 3. Curves delimit 2σ upper and lower limits on the total gamma width Γ_{γ} for the 4.033 MeV state from the present Coulomb excitation (Coulex) and lifetime (DSAM) data respectively as a function of the E2/M1 mixing ratio for transitions to or from the ground state. Hatched area indicates overlapping region of 2σ confidence from both measurements. The data point is the value expected for the matrix elements calculated as described in the text.