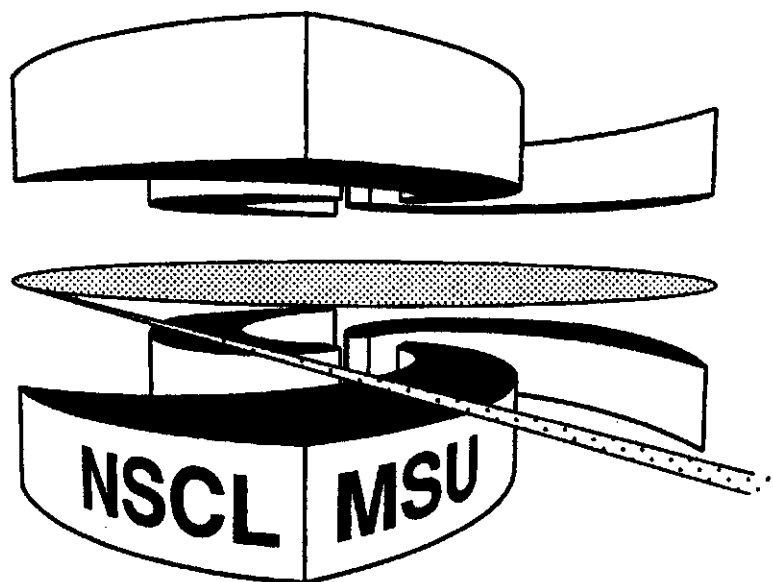


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National Superconducting Cyclotron Laboratory

**TRANSITION TO THE “ISLAND OF INVERSION”: FAST-BEAM
 γ -RAY SPECTROSCOPY OF $^{28,29,30}\text{Na}$**

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Abstract

The technique of intermediate-energy heavy-ion scattering with exotic beams was used to measure the excitation cross sections to the first collective excitations in $^{28,29,30}\text{Na}$. The trends in the deduced intrinsic electromagnetic quadrupole moments obtained in the present study and a previous study of ^{31}Na suggest that the ground state of ^{31}Na is dominated by intruder configurations, while the lighter sodium isotopes are not. This conclusion is supported

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The “island of inversion” phenomenon in neutron-rich exotic nuclei near $N = 20$ is providing a rigorous challenge for our understanding of the evolution of shell structure in isotopes far from stability. This phenomenon, in which several $N = 20$ nuclei (^{30}Ne , ^{31}Na , ^{32}Mg) have strongly deformed ground state shapes despite having a “magic number” of neutrons (for example, see [1–9]), appears to represent a particularly interesting case of shape coexistence, which occurs throughout the nuclear chart. Shape coexistence at shell closures, which has been observed in nuclei as heavy as the lead isotopes [10], can be described in the following way: The “normal” spherical configuration of a nucleus having a closed shell or nearly closed shell lies close in energy to a deformed “intruder” configuration which is formed by promoting a pair of nucleons across the shell closure. Generally, the ground state is dominated by the spherical configuration because energy is required to promote the pair of nucleons across the shell gap. The deformed configurations in ^{30}Ne , ^{31}Na , ^{32}Mg and several $N = 21, 22$ neighbors result from promotions of neutrons across the $N = 20$ shell closure. The “inversion”, in which the deformed configuration becomes the ground state, has been attributed to strong interactions between the promoted neutrons and valence protons, interactions between the promoted neutrons themselves, and shifts in single particle energies [1,7].

In the present work, we report an experimental study of the transition from “normal” to “inverted” configurations in isotopes of sodium with $N < 20$. We measured low-lying collective excitations of the $N = 17 - 19$ isotopes $^{28,29,30}\text{Na}$ using intermediate energy heavy-ion scattering, which allows the determination of electromagnetic matrix elements. An examination of the present results, a study of ^{31}Na previously reported [9], and available information on masses demonstrates that the ground states of the $N = 17 - 19$ Na isotopes are *not* “inverted” as in ^{31}Na , and so should not be included in the “island of inversion”.

The technique of intermediate energy heavy-ion scattering has been used to determine excitation energies and electromagnetic matrix elements in exotic nuclei with masses as high as $A = 60$ (for a review, see [11]). In the region near the island of inversion, this technique has been utilized for studies of the $N = 20$ isotones ^{31}Na [9], ^{32}Mg [3,6,12], and ^{34}Si [4],

the even-even Ne and Mg isotopes in the $N = 16 - 18$ transition region [6], and several other isotopes of Si and P located around the boundary of this region [4,8]. The technique involves scattering a beam of exotic nuclei with energies greater than 30 MeV/nucleon from a heavy target. The exotic nuclei scattered into small angles are detected in coincidence with the prompt γ -rays de-exciting them. Small angles are selected to maximize the role of the Coulomb interaction in the inelastic scattering reaction. From a previous study of ^{31}Na [9] very similar to that reported here, we can estimate that the Coulomb interaction accounts for approximately 85% of the cross section in the present experiments. Detailed coupled-channels calculations for the isotopes studied here are described below.

The present measurements were performed at the National Superconducting Cyclotron Laboratory at Michigan State University. The ^{28}Na secondary beam was produced via fragmentation of a primary beam of ^{40}Ar at 90 MeV/nucleon from the K1200 cyclotron. The $^{29,30}\text{Na}$ beams came from fragmentation of a 80 MeV/nucleon primary beam of ^{48}Ca . The fragmentation of the primary beams took place in thick ^9Be targets ($> 370 \text{ mg/cm}^2$) located at the mid-acceptance target position of the A1200 fragment separator [13]. The energies of the secondary $^{28-30}\text{Na}$ beams produced in the fragmentation reactions were 43.1 MeV/nucleon, 60.0 MeV/nucleon, and 55.6 MeV/nucleon, respectively, in the middle of the secondary target.

Thick gold foils (518 mg/cm^2 for ^{28}Na , 702 mg/cm^2 for $^{29,30}\text{Na}$) were used as secondary targets. After passing through the foils, the secondary beam particles were stopped in a cylindrical fast-slow phoswich detector which provided nuclear charge identification. This charge identification, along with time-of-flight measurements in the beam line, gives positive isotope identification. For the ^{28}Na measurement, the phoswich detector provided coverage for laboratory frame scattering angles up to 3.96° ; for $^{29,30}\text{Na}$ the angle was 2.80° . The corresponding scattering angles in the center of mass were 4.52° , 3.21° , and 3.23° , respectively. The numbers of secondary beam particles collected for ^{28}Na , ^{29}Na and ^{30}Na were 8.2×10^7 , 1.3×10^7 , and 3.3×10^6 , respectively. The NSCL NaI(Tl) array [14] was used to detect γ -rays. The γ -ray spectra in coincidence with the detection of $^{28,29,30}\text{Na}$ are shown in Fig.

1. The energy spectra shown are Doppler-shifted event-by-event so they are seen as in the rest frame of the projectiles.

The γ -ray spectrum for ^{28}Na (Fig. 1a) shows a clear peak at 1240 ± 11 keV, for which the measured cross section is 26 ± 6 mb. Huber *et al.* [15] used laser spectroscopic techniques to determine the ground state spin to be $J = 1$. The neighboring even-even nuclei $^{26,28}\text{Ne}$ and $^{28,30}\text{Mg}$ all appear to be rotational [6], so we adopt a rotational interpretation for ^{28}Na as well. Hence, we propose that we are populating the first rotational excitation (with $J = 2$) of a $K = 1$ rotational band via an $E2$ excitation. Of course, this reaction certainly populates the $J = 3$ member of this rotational band by an $E2$ excitation as well. However if the 1240 keV γ -ray was the $J = 3 \rightarrow J = 1$ transition, the $J = 2 \rightarrow J = 1$ transition would have an energy less than 1240 keV and would be at least as intense. There is no evidence for such a transition in the spectrum. If the 1240 keV γ -ray was the $J = 3 \rightarrow J = 2$ transition, then the $J = 2 \rightarrow J = 1$ transition would have a smaller energy and a greater intensity. Once again, there is no evidence for such a transition. Our conclusion is that the 1240 keV γ -ray corresponds to the $J = 2 \rightarrow J = 1$ transition.

Of course, it is quite likely that the $J = 3$ member of the rotational band is also populated in the present reaction, and that the $J = 3$ state decays to the $J = 2$ state. If the rotational band is strongly coupled, then the $J = 3 \rightarrow J = 2$ transition has an energy significantly larger than 1240 keV. The $J = 3 \rightarrow J = 2$ transition is not apparent in the spectrum, but there are two factors that would conspire to suppress this transition. First, the excitation cross section for populating the $J = 3$ state is likely to be smaller than that for the $J = 2$ state. Second, the γ -ray detection efficiency decreases as the γ -ray energy increases. If the band is strongly coupled, then the energy of the $J = 3 \rightarrow J = 2$ transition is near 1800 keV, for which the efficiency is significantly lower than for 1240 keV.

The only prior γ -ray spectroscopic study of ^{28}Na was performed via β -decay of ^{28}Ne [16]. Neither of the two γ -rays observed in that study (865 and 2063 keV) were observed here. However, this is not surprising since the β -decay of the $J^\pi = 0^+$ ground state of ^{28}Ne can only populate $J = 0$ and $J = 1$ states in the ^{28}Na daughter nucleus.

In the ^{29}Na spectrum (Fig. 1b), there is a broad peak centered near 500 keV. Most of the counts in this peak can be attributed to the excitation of the 547 keV state in the gold secondary target. In the projectile-frame spectrum shown in Fig. 1b, the peak from the gold target (which is emitted nearly at rest in the laboratory frame) is broader than it appears in the laboratory-frame spectrum. However, there are some excess counts on the higher energy side of this peak. A peak-fitting analysis of this complex structure yields an energy of 701 ± 20 keV and a cross section of 26 ± 21 mb for a transition corresponding to ^{29}Na .

The ground state of ^{29}Na was measured by Huber *et al.* [15] to have $J = 3/2$, so we suggest that the $J = 5/2$ member of the $K = 3/2$ rotational band built on the ground state has an energy of 701 ± 20 keV and is de-excited via the γ -ray observed here. We cannot exclude the possibility that the 701 keV γ -ray is actually the $J = 7/2 \rightarrow 5/2$ transition instead of the $J = 5/2 \rightarrow 3/2$ transition. If this is the case, the $J = 5/2 \rightarrow 3/2$ transition would likely have an energy of less than 700 keV and might be obscured by the broad peak from excitation of the gold target. Prior to this study, there was no information in the literature regarding excited states in ^{29}Na .

There are two strong peaks in the ^{30}Na spectrum (Fig. 1c) at 433 ± 16 keV and 701 ± 20 keV. The apparent peak near 500 keV is quite likely to be an artifact of the 547 keV peak from the gold target. The cross sections for the two peaks are comparable (42 ± 14 mb for the 433 keV γ -ray, 39 ± 18 mb for the 701 keV γ -ray). The most straightforward explanation for this spectrum is that the 701 keV γ -ray is from ^{29}Na and is produced via single neutron stripping from the ^{30}Na beam particle, while the 433 keV γ -ray de-excites the $J = 3$ member of the ground state $K = 2$ rotational band (the ground state spin of $J = 2$ was determined by Huber *et al.* [15]). The energy spectrum from the phoswich detector in which the beam is stopped provides evidence to support the assertion that at least some of the 701 keV γ -ray counts result from single neutron stripping to ^{29}Na : the centroid of phoswich total energy signals in coincidence with the 701 keV γ -ray is lower than the centroid of ^{30}Na energies without the γ -ray gate. Stripping cross sections of this size have been observed for single neutron stripping reactions previously [4]. However, the $J = 4 \rightarrow J = 3$ transition between

members of the ground state rotational band may also have an energy close to 700 keV. If the energy of the $J = 3$ state is 433 keV, the strong coupling model would give a $J = 4 \rightarrow J = 3$ transition energy of 577 keV. Hence, the 700 keV peak may also include the $J = 4 \rightarrow J = 3$ transition in addition to the ^{29}Na γ -ray from single-neutron stripping.

It is important to note that the cross sections quoted here for production of γ -rays in $^{28,29,30}\text{Na}$ are almost certainly not equal to cross sections for directly populating the first excited states. While multiple excitation (coupled channels effects) are small in these reactions [11], the second excited states in the rotational bands ($J = 3$ in ^{28}Na , $J = 7/2$ in ^{29}Na , and $J = 4$ in ^{30}Na) can be excited via single-step $E2$ excitations. Therefore, the feeding of the first excited states by the second excited states must be considered in extracting electromagnetic matrix elements.

To obtain the electromagnetic matrix elements for populating excited states in $^{28,29,30}\text{Na}$, we used the coupled channels code ECIS88 [17], which takes into account *both* electromagnetic and nuclear contributions to the scattering reactions. The secondary beams lost significant amounts of energy in the gold target, so the analyses were performed assuming the mid-target beam energies. We used standard axially symmetric deformed rotational form factors. The optical model parameters used here were obtained by Barrette *et al.* for the scattering of ^{17}O from ^{208}Pb at a laboratory energy of 84 MeV/nucleon [18].

There are two deformation parameters involved in each ECIS calculation. The ‘‘Coulomb deformation’’ β_C reflects the deformation of the proton density in the nucleus and yields the electromagnetic matrix element $B(E2; I_{gs} \rightarrow I_f)$ via the equations [19]

$$B(E2; I_i \rightarrow I_f) = Q_0^2 e^2 \frac{5}{16\pi} \langle I_i K 2 0 | I_f K \rangle^2 \quad (1)$$

and

$$Q_0 = \left(\frac{16\pi}{5} \right)^{1/2} \frac{3}{4\pi} Z R_0^2 \beta_C, \quad (2)$$

where Q_0 is the intrinsic quadrupole moment and $R_0 = r_0 A^{1/3}$ with $r_0 = 1.20$ fm. The ‘‘nuclear matter deformation’’ β_A is used to determine the nuclear force contribution to

the scattering reaction and involves transition matrix elements for both the neutrons and protons. To fit the cross section data in a unique way, we must specify the relationship between β_C and β_A . We do this using a simple collective model picture. In such a picture, the deformation lengths $\delta_C = \beta_C R_C$ and $\delta_A = \beta_A R_A$ are equal [20]. In these definitions of deformation lengths, $R_C = r_C A^{1/3}$ and $R_A = r_A A^{1/3}$, with r_C and r_A being the Coulomb radius and real nuclear radius parameters, respectively, in the optical model potentials. Deviations from the simple collective model picture are frequently observed in single-closed-shell nuclei [20,21], but are highly unlikely in rotational nuclei. The direct determination of a deviation from the simple collective model picture would require a measurement using a second experimental probe, such as inelastic proton scattering (for examples of inelastic proton scattering by exotic beams, see [22–26]).

As mentioned above, it is almost certain that the second rotational excited states in each nucleus were populated in these experiments, even though γ -rays de-exciting them may not have been observed. In our ECIS analyses, we have assumed that these second rotational states ($J = 3$ in ^{28}Na , $J = 7/2$ in ^{29}Na , and $J = 4$ in ^{30}Na) occur at energies which are given by the strong coupling limit. We constrain the deformation parameters for excitations of the first and second rotational states to be equal since they are assumed to be members of the same rotational bands. The experimental uncertainties we quote take into account that the second excited state in the rotational band may decay to the first excited state anywhere from 0% to 100% of the time.

The results of the ECIS analyses are given in Table I, which lists for each nucleus β_C and β_A deduced under the assumptions stated above, as well as the intrinsic quadrupole moments Q_0 and the reduced matrix elements $B(E2 \uparrow)$. Fig. 2a illustrates the evolution of the intrinsic quadrupole moments determined via intermediate energy heavy-ion scattering for the Na isotopes, including both the present study and the previously published study of ^{31}Na [9]. Fig. 2a also shows intrinsic electric quadrupole moments deduced from the β -NMR measurements of spectroscopic (laboratory-frame) quadrupole moments by Keim *et al.* [27]. The intrinsic quadrupole moment Q_0 can be obtained from the spectroscopic quadrupole

moment Q via the equation [19]

$$Q_0 = Q \frac{(J+1)(2J+3)}{3K^2 - J(J+1)}. \quad (3)$$

Keim *et al.* measured the spectroscopic quadrupole moments of the ground states; therefore, J and K in this equation are equal. The intrinsic quadrupole moments obtained from these two methods agree for all four nuclei shown in Fig. 2a. Despite the agreement for the individual nuclei, the trends in the two data sets lead to different conclusions about the dependence of Q_0 on the neutron number. The heavy-ion scattering results suggest an increase in Q_0 as N approaches 20 (^{31}Na) while the β -NMR results do not suggest this increase.

The first evidence for the existence of the “island of inversion” was the observation that experimental binding energies for several neutron-rich isotopes at and near $N = 20$ are larger than those calculated using the shell model with “normal” configurations, in which particles are *not* promoted across major shell gaps [1,28–31]. Fig. 2b shows where this deviation occurs for the Na isotopes by comparing the experimental binding energies [32] to the binding energies for normal configurations calculated by Warburton, Brown and Becker [1] for $^{29,30,31,32,33}\text{Na}$. This calculation reproduces the binding energies in $^{29,30}\text{Na}$, while $^{31,32}\text{Na}$ are clearly more bound than predicted by the calculation. The trend in Q_0 obtained in the present study supports the conclusion suggested by the binding energies - that ^{31}Na is in the “island of inversion” where the ground states are dominated by intruder configurations, while the lighter isotopes are not.

In summary, we have measured excitation cross section to low-lying collective states in $^{28,29,30}\text{Na}$ and we deduced electromagnetic transition matrix elements assuming the observed transitions are de-excitations of the lowest rotational excitations of $^{28,29,30}\text{Na}$. The trend in the intrinsic electric quadrupole moments of $^{28,29,30,31}\text{Na}$ measured using this method suggests that the ground state of ^{31}Na is dominated by intruder configurations, while the ground states of the lighter isotopes are not. This conclusion is supported by the binding energies.

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REFERENCES

- [1] E.K. Warburton, J.A. Becker and B.A. Brown, *Phys. Rev.* **C41**, 1147 (1990).
- [2] A. Poves and J. Retamosa, *Nucl. Phys.* **A571**, 221 (1994).
- [3] T. Motobayashi *et al.*, *Phys. Lett. B* **346**, 9 (1995).
- [4] R.W. Ibbotson *et al.*, *Phys. Rev. Lett.* **80**, 2081 (1998).
- [5] E. Caurier *et al.*, *Phys. Rev.* **C58**, 2033 (1998).
- [6] B.V. Pritychenko *et al.*, *Phys. Lett. B* **461**, 322 (1999).
- [7] Y. Utsuno *et al.*, *Phys. Rev.* **C60**, 054315 (1999).
- [8] B.V. Pritychenko *et al.*, *Phys. Rev. C*, in press (2000).
- [9] B.V. Pritychenko, Ph. D. thesis, Michigan State University (2000).
- [10] J.L. Wood *et al.*, *Phys. Rep.* **215**, 101 (1992).
- [11] T. Glasmacher, *Ann. Rev. Nucl. Part. Sci.*, **48**, 1 (1998).
- [12] V. Chist'ye *et al.*, Nuclear Structure 2000 Proceedings, *Nucl. Phys. A*, in print (2000).
- [13] B.M. Sherrill *et al.*, *Nucl. Inst. and Meth.* **B56**, 1106 (1991).
- [14] H. Scheit *et al.*, *Nucl. Inst. and Meth.* **A422**, 124 (1999).
- [15] G. Huber *et al.*, *Phys. Rev.* **C18**, 2342 (1978).
- [16] A.T. Reed *et al.*, *Phys. Rev.* **C60**, 024311 (1999).
- [17] J. Raynal, *Phys. Rev.* **C23**, 2571 (1981).
- [18] J. Barrette *et al.*, *Phys. Lett. B* **209**, 182 (1988).
- [19] P. Ring and P. Schuck, *The Nuclear Many-Body Problem*, (Springer-Verlag, New York, 1980).

- [20] A.M. Bernstein, V.R. Brown, and V.A. Madsen, *Comments Nucl. Part. Phys.* **11**, 203 (1983).
- [21] A.M. Bernstein, V.R. Brown, V.A. Madsen, *Phys. Lett.* **103B** (1981) 255.
- [22] J.H. Kelley *et al.*, *Phys. Rev.* **C56** (1997) R1206.
- [23] J.K. Jewell *et al.*, *Phys. Lett. B* 454 (1999) 181.
- [24] L.A. Riley *et al.*, *Phys. Rev. Lett.* 82 (1999) 4196.
- [25] F. Maréchal *et al.*, *Phys. Rev.* C60 (1999) 034615.
- [26] H. Iwasaki *et al.*, *Phys. Lett. B* 481 (2000) 7.
- [27] M. Keim, *Proc. ENAM 98: Exotic Nuclei and Atomic Masses* (Traverse City, Michigan), AIP conference proceedings **455**, 50 (1998); M. Keim *et al.*, *Eur. Phys. J. A* **8**, 31 (2000).
- [28] C. Thibault *et al.*, *Phys. Rev.* **C12**, 644 (1975).
- [29] W. Chung and B.H. Wildenthal, *Phys. Rev.* **C22**, 2260 (1980).
- [30] C. Détraz *et al.*, *Nucl. Phys.* **A394**, 378 (1983).
- [31] D.J. Viera *et al.*, *Phys. Rev. Lett.* **57**, 3253 (1986).
- [32] G. Audi and A.H. Wapstra, *Nucl. Phys.* **A565**, 1 (1993).

TABLES

TABLE I. Results for deformation parameters, intrinsic quadrupole moments and reduced electromagnetic matrix elements.

	β_C	β_A	Q_0 (fm ²)	$B(E2 \uparrow)$ (e ² fm ⁴)
²⁸ Na	0.30(7)	0.34(8)	33(8)	54(26)
²⁹ Na	0.33(18)	0.37(20)	37(20)	70 ⁺¹⁰⁰ ₋₅₅
³⁰ Na	0.41(10)	0.46(11)	51(15)	130 ⁺⁹⁰ ₋₆₅

FIGURES

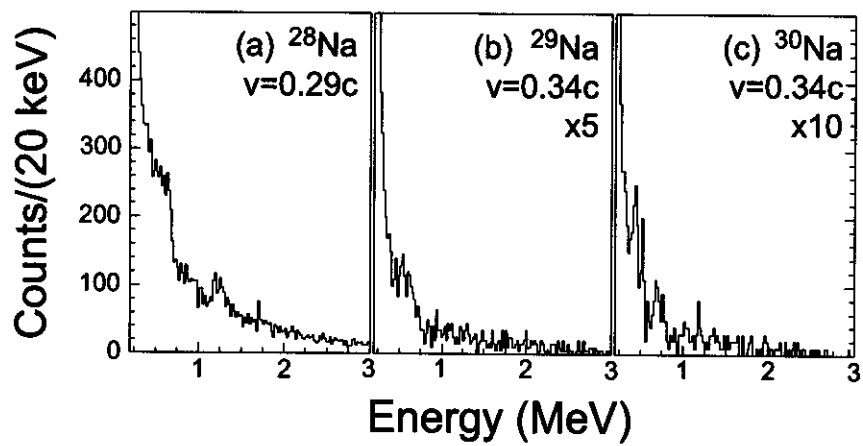


FIG. 1. Photon spectra gated on $^{28,29,30}\text{Na}$ beams in the projectile-frame.

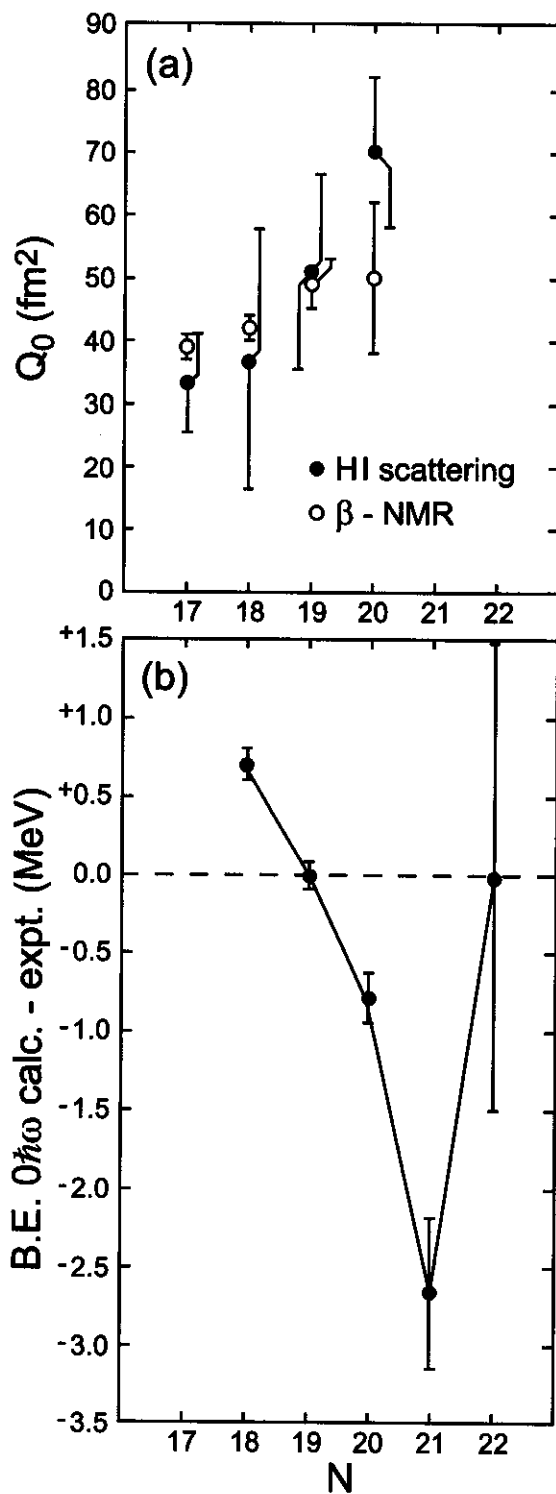


FIG. 2. (a) Intrinsic electric quadrupole moments determined in the present study and in Ref. [9] using intermediate energy heavy-ion scattering (solid shapes), and corresponding values determined in the study of Keim *et al.* [27]; (b) Deviation of experimental binding energies [32] from the calculation of Warburton, Brown and Becker [1] using “normal” configurations.